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Reliability Analysis of A Single Pile–Non Probabilistic Approach

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Abstract: Reliability analysis of structures has become important with the present-day emphasis on performance-based design because in structural engineering, uncertainties arise from different sources. Although probability theory has been traditionally used to represent all types of uncertainties, it may not be proper to use probability theory to represent uncertainties in the presence of limited knowledge. In the present study, an attempt has been made to perform reliability analysis in the context of fuzzy set theory and possibility theory. Two different methods of fuzzy reliability analysis, proposed in the literature, are identified. The performances of these methods are studied with the help of reliability analysis of a single axial pile considering different formats of limit state function. The effect of the variation in uncertainty of the input fuzzy variables on the reliability is studied. It is noted that the results obtained using both the methods of fuzzy reliability analysis are comparable. Since both the methods give same results, any of the methods can be used depending upon their applicability.

Keywords: fuzzy reliability, possibilistic reliability, failure possibility, reliability analysis.

I. INTRODUCTION

The evaluation of safety of structures is a task of much importance since the performance of the structure is assessed by its safety, service ability and economy. The safety of a structure depends on resistance, R of the structure and the action, S (load/ load effect) on the structure. The resistance or response of the structure depends on physical properties of material and geometrical properties of the structure and the action on the structure is a function of various types of loads like dead load, live load, wind load, etc. There will be inherent variations in the physical properties of materials, loads, occurrence of natural phenomena, etc. Thus the information about input variables is never certain, precise and complete. In the presence of these uncertainties, ensuring absolute safety of a structure is near to impossible. However, in the majority of texts and courses, the uncertainty is relegated to a minor position and the reason for this negligence ranges from the point it is easier to the fact that it is somewhat difficult to embrace uncertainty easily and directly. Till 1960, no serious attempt was made to consider explicitly the randomness of variables in the analysis, design and evaluation of safety; even though it was known that the above parameters are random. Later, engineers and research workers started realizing the need for the evaluation of safety taking into account the uncertainty in variables.

II. UNCERTAINTIES IN STRUCTURAL ENGINEERING

There are ranges of uncertainties that arise in structural engineering and in the case of real structures, uncertainties may be due to intrinsic variability of mechanical and physical properties as well as to the lack of knowledge when information are scarce and/or subject to some errors, for instance related to the test procedure. Uncertainties can be broadly classified into two categories namely aleatory and epistemic uncertainties [12], which must be treated in different ways. Depending on the type of uncertainty an appropriate theory should be used to model and process the same in engineering decision making. Although probability theory has been traditionally used to represent both types of uncertainties, various researchers have pointed out that it may not be proper to use probability theory to represent epistemic uncertainty in the presence of limited knowledge. A number of alternative theories, such as fuzzy set theory, evidence theory, convex modelling, and interval analysis, for modelling uncertainties have been proposed by various researchers. It is to be noted that selection of a particular uncertainty handling method depends upon the type and source of uncertainty.

III. CONCEPT OF RELIABILITY

A. Definition of reliability

The concept of reliability has been applied to many fields and has been interpreted in many ways. The most common definition is that “reliability is the probability of an item performing its intended function over a given period of time under operating conditions encountered” [9].

Reliability is always estimated corresponding to a performance or limit state function. Commonly used limit state functions can be broadly divided into two groups; the serviceability and the strength limit states. The probabilistic approach describes the resistances and the loads as random because their values are not perfectly known. Statistics is used to obtain, from the available set of data or measurements, parameters which define the occurrence properties of variables which are random in nature; probability converts these information to occurrence functions (probability density functions-PDFs and cumulative density functions-CDFs) and defines the general framework for reliability analysis, whose main objective is to obtain failure probabilities of the structural system response, which are compared with limit values to assess the reliability of the structure. Greater the importance of the structure to be designed, greater the demand of assuring small probability of failure.

IV. FUZZY METHOD OF RELIABILITY ANALYSIS

An attempt has been made to perform reliability analysis in the framework of fuzzy set and possibility theory. Fuzzy numbers are used to define an equivalence class of probability distributions compatible with available data and corresponding upper and lower cumulative density functions and to consider the variables involved in the civil engineering problems as fuzzy numbers. The method to carry out fuzzy reliability analysis mainly based on the formulations proposed by Barbara Ferracuti and Isaac Elishakoff [1]. The methodology is explained below;

Consider basic problem of strength of material in which a structural component subjected to load (action), P_s and the strength (resistance) of material of the component is P_r . For safety of the component, load P_s on the component should be less than strength P_r . In the simplest approximation it is considered the load as a fuzzy number P_s through membership function μ_s , while the strength P_r may still be considered as a deterministic quantity P_r . Necessity and possibility of an event that the fuzzy stress satisfies inequality $P_s \leq P_r$ represent the lower and upper bounds of the probability of the event [8]. Since the probability that the action less than the resistance R is reliability, we get,

$$N(P_s \leq P_r) \leq R_0 \leq \Pi(P_s \leq P_r) \quad \dots(1)$$

In other words, possibility and necessity of fulfilling the inequality $P_s \leq P_r$ are upper and lower bounds of reliability respectively, i.e.,

$$\begin{aligned} R_* &= N(P_s \leq P_r) \\ R^* &= \Pi(P_s \leq P_r) \end{aligned} \quad \dots(2)$$

Fig. 1 depicts the necessity and possibility functions that satisfy the inequality $P_s \leq P_r$ for a triangular fuzzy load, at $P = P_r$, necessity and possibility represent the lower and upper bounds of reliability. In other words, the upper and lower bound of reliability are the value of the possibility and necessity function at $z = 0$. The upper bound of reliability is not of much importance. The lower bound of reliability may be called as fuzzy reliability.

The possibility of failure then can be obtained as,

$$\begin{aligned} \Pi_f &= \Pi(P_s > P_r) \\ \Pi_f &= 1 - N(P_s \leq P_r) \\ \Pi_f &= 1 - R_* \end{aligned} \quad \dots(3)$$

The procedure for fuzzy set theory based reliability analysis can be represented by flowchart shown in Fig. 2.

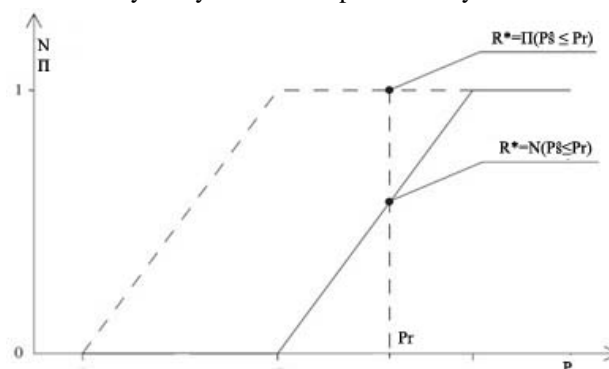


Fig. 1. Possibility and necessity functions that satisfy the inequality $\Sigma \leq \sigma$ for triangular fuzzy stress.

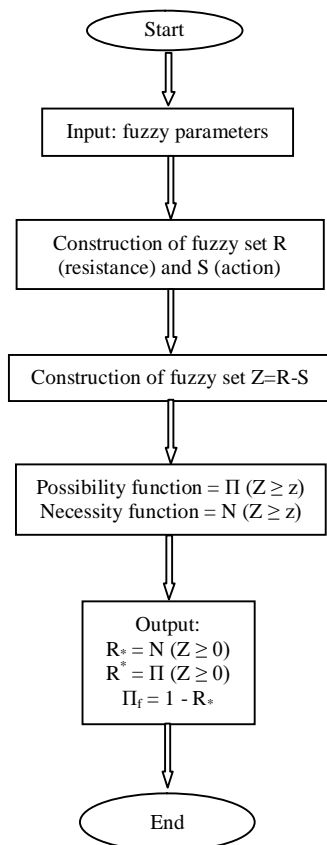


Fig. 2. Flowchart for fuzzy method of reliability analysis

V. POSSIBILITY METHOD OF RELIABILITY ANALYSIS

The method of possibilistic reliability analysis mainly based on the methodology proposed by C. Cremona and Y. Gao [3]. This method is an original alternative to the probabilistic reliability theory, keeping the same features regarding some theoretical concepts like design points, failure probability, reliability indices.

Let us consider a limit state function given by Equation (4), composed of non-interactive L-R fuzzy variables X_i . Like in probabilistic reliability theory, in this approach also the initial space composed of fuzzy numbers X_i is transformed into a particular space composed of special class of non-interactive fuzzy numbers expressed as L-R fuzzy intervals, generally Gaussian fuzzy numbers.

$$g(X_1, X_2, \dots, X_n) = 0 \quad \dots (4)$$

The possibilistic approach will try to evaluate safety in terms of possibility of failure, Π_f which is defined as the possibility that the value of limit state equation less than or equal to zero. In other words, failure possibility is equal to the degree of possibility of the limit state function $g(\{X\})$ at the value equal to zero. Mathematically, it is expressed as,

$$\Pi_f = \Pi(g(\{X\}) \leq 0) \quad \dots (5)$$

Now, it is necessary to transform the set of fuzzy variables, $\{X\}$ into set of fuzzy Gaussian numbers, $\{U\}$ using τ -transform and the τ -transform must verify the following property;

$$\pi_X(x) = \pi_U(\tau_X(x)) \quad \dots (6)$$

The τ -transform is invertible. The transformation for each variable becomes,

$$\left. \begin{aligned} \tau_{xi}(x_i) &= u_i = (L^*)^{-1}(L(x_i)) && \text{if } x_i < m_{xi} \\ \tau_{xi}(x_i) &= u_i = 0 && \text{if } m_{xi} \leq x_i \leq n_{xi} \\ \tau_{xi}(x_i) &= u_i = (R^*)^{-1}(R(x_i)) && \text{if } x_i > n_{xi} \end{aligned} \right\} \quad \dots (7)$$

The inverse transformation can be written as follows;

$$\left. \begin{aligned} \tau_{xi}^{-1}(u_i) &= x_i = m_{xi} - \alpha_{Lxi} L_i^{-1}(L^*(u_i)) & \text{if } u_i < 0 \\ \tau_{xi}^{-1}(u_i) &= x_i = x_i^* & \text{if } u_i = 0 \\ \tau_{xi}^{-1}(u_i) &= x_i = n_{xi} + \alpha_{Rxi} R_i^{-1}(R^*(u_i)) & \text{if } u_i > 0 \end{aligned} \right\} \dots (8)$$

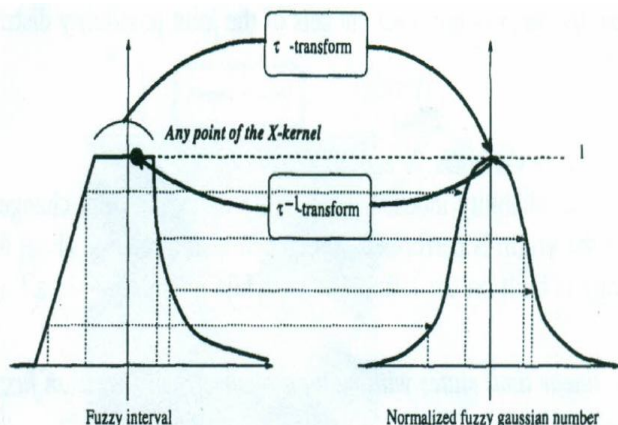


Fig. 3. τ -transform of fuzzy interval into normalized fuzzy Gaussian numbers

Once all the variables are transformed, the limit state function can be expressed in terms of fuzzy Gaussian numbers;

$$g(\{X\}) = (g(\tau^{-1}(\{U\}))) = g_U(\{U\}) \quad \dots (9)$$

With the help of rule of signs, choosing appropriate branch of each variable in the construction of limit state function g_U and using inverse transformation given in Equation (8) in Equation (9), the limit state function can be written as;

$$g_U(U) = g(\dots, m_{1i} - \alpha_{1Li} L_{1i}^{-1}(L^*(U)), \dots, n_{2j} + \alpha_{2Rj} R_{2j}^{-1}(R^*(U)), \dots)$$

Since $R^*(-U) = L^*(U)$ for fuzzy Gaussian numbers, we can write

$$g_U(U) = g(\dots, m_{1i} - \alpha_{1Li} L_{1i}^{-1}(L^*(U)), \dots, n_{2j} + \alpha_{2Rj} R_{2j}^{-1}(L^*(U)), \dots)$$

$$g_V(V) = g(\dots, m_{1i} - \alpha_{1Li} L_{1i}^{-1}(V), \dots, n_{2j} + \alpha_{2Rj} R_{2j}^{-1}(V), \dots)$$

The possibility of failure,

$$\Pi_f = \Pi(g_U(\{U\}) \leq 0)$$

$$\max(V) \text{ with } g_V(V) = 0 \text{ and } V < 1$$

which gives $\Pi_f = V$

The above solution scheme is made assuming the failure possibility less than one. Therefore, it is necessary to check initially if the failure possibility is smaller than one. For determining whether the failure possibility is less than one, it is sufficient to check

$$g(\dots, m_{xi}, \dots, n_{xj}, \dots) \leq 0 \quad \dots (10)$$

If the condition given in Equation (10) satisfies, possibility of failure is equal to one; otherwise failure possibility is less than one.

The possibilistic reliability index denoted by λ is the solution of the minimization problem expressed as follows;

$$\lambda = \min(\|U_\infty\|) \text{ according to: } g_U(U) = 0, \text{ and } |U_i| = |U_j|, \forall i, j.$$

$$\lambda = (L^*)^{-1}(\Pi_f) = \sqrt{-\ln(\Pi_f)}.$$

It should be noted that λ takes its values in R^+ . A possibility of failure equal to one corresponds to a reliability index of zero. Once we get the failure possibility, possibilistic reliability may be obtained as,

$$R_0 = 1 - \Pi_f$$

The procedure for fuzzy reliability analysis by possibilistic reliability theory can be represented by flowchart shown in Fig. 4.

VI. COMPARISION BETWEEN TWO METHODS OF RELIABILITY ANALYSIS

Comparison between the two methods for reliability analysis with their advantages and limitations are given in Table I. The two methods discussed are capable of estimating reliability of any component and can be used with their own applicability since both the methods have their own advantages and limitations. The possibility of failure and fuzzy reliability index can be obtained in the possibilistic method. The bounds of reliability can be obtained in the fuzzy set theory method. The computations involved in this method are comparatively simpler, and gives better results.

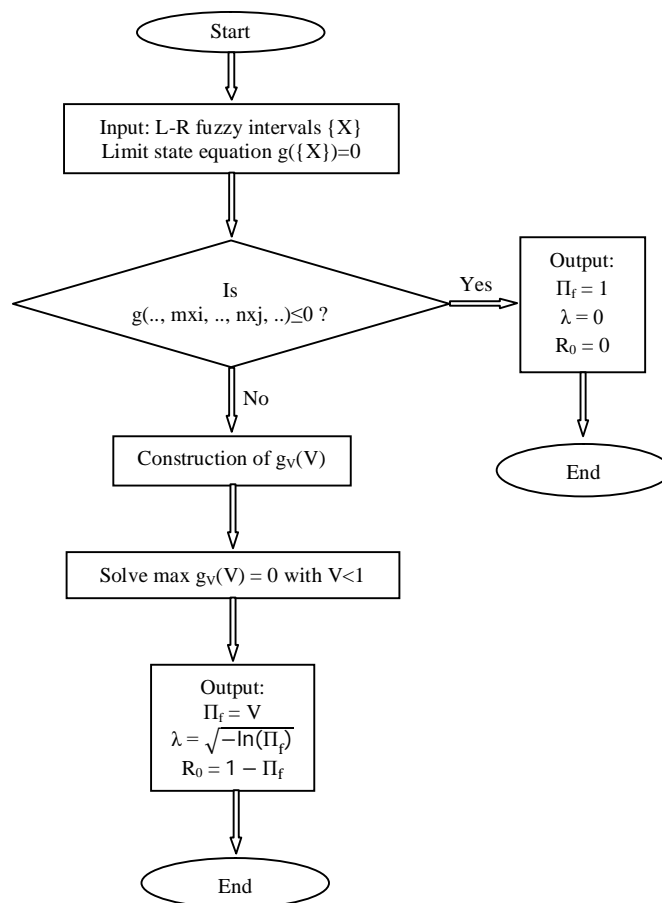


Fig. 4. Flowchart for possibilistic method of reliability analysis

A. Effect of variation of uncertainty on reliability

Variation in reliability when the fuzziness in the variables varied is studied. The fuzzy reliability and possibilistic reliability are estimated by varying the support of the fuzzy set for resistance (R) keeping the action on the structure deterministic. The plot of reliability values against variation in resistance is given in fig. 5.

The performances of the two methods for reliability analysis are studied in the next section through the reliability analysis of an axially loaded single pile.

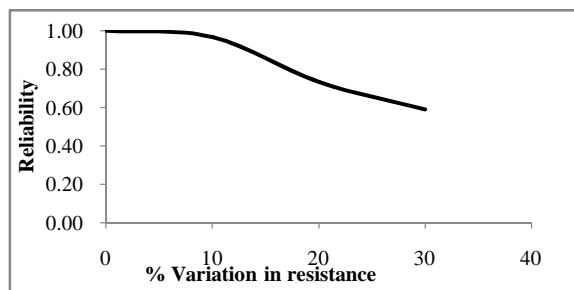


Fig. 5. Plot of reliability values against variation in resistance

TABLE I.
COMPARISON OF TWO METHODS OF FUZZY RELIABILITY ANALYSIS

Sl. no.	Aspect considered	Fuzzy set theory method	Possibilistic method
1	Possibility of failure	$\Pi_f = 1 - R_*$	$\Pi_f = \Pi(Z \leq 0)$
2	Reliability	Reliability bounds; $R_* = N(Z \geq 0)$ $R^* = \Pi(Z \geq 0)$	Reliability; $R_0 = 1 - \Pi_f$ Possibilistic reliability index; $\lambda = \sqrt{-\ln \Pi_f}$
3	Advantages	<ul style="list-style-type: none"> Bounds of reliability are defined. The method is simpler and computations involved are easier. The method can also be adopted when solution is not available in explicit/closed form to compute the parameters considered in performance function. The method can also be adopted when the membership function of fuzzy parameters are not defined by any function. 	<ul style="list-style-type: none"> The features are similar to probabilistic one and much easier in implementations. The method involves less computation. The safety index – possibilistic reliability index can be obtained. The possibilistic reliability index is an invariant.
4	Limitations	<ul style="list-style-type: none"> Even though the computations are easier, it may become time consuming if more number of variables involved in limit state function because more computation will be involved. The safety index cannot be obtained in this method. 	<ul style="list-style-type: none"> Applicable only for non-interactive fuzzy variables. Computations may be lesser but solving the equation $g_v(V)=0$ may become difficult if limit state function is non-linear with more number of variables. The results will be less accurate if closed form solution is not available in finding the parameters considered in the limit state equation. The method cannot be adopted when the membership function for input variables is not defined. If a variable appears more than once in limit state function, the possibility of failure will be over-estimated when the repeated variable is duplicated.

VII. ILLUSTRATION OF THE METHODS OF RELIABILITY ANALYSIS

Uncertainty associated with single pile-soil system is considered. Reliability analysis of an axially loaded single pile, with soil properties considered as fuzzy parameters, is performed using both the methods explained above. The possibilistic and fuzzy reliabilities against different limit states are determined.

A. Description of the problem

A single pile-soil system as shown in Fig. 6, is considered for the analysis. The pile is made of concrete with circular cross section subjected to an axial compressive load at the pile head. The soil profile has two sand layers; upper layer consists of loose sand and lower layer is dense sand-silt stratum. The geometrical and material properties of the pile, load, soil properties and the variations in load, pile properties are adopted from [6] and the variations of soil properties are considered as per [5].

B. Pile properties and load data:

The considered fuzzy variables in the analysis are given in Table 2 and deterministic parameters are given below;

Length of the pile: $L = 15$ m.

Diameter of the pile: $D = 30$ cms.

C. Soil properties

The soil characteristics and its behaviour can be modelled using load transfer curves; q - z and f - z (or t - z) as shown in Fig. 7 where q is unit tip resistance mobilized at tip settlement z and f is unit frictional resistance mobilized at pile shaft settlement z . The variations of these properties are assumed to be constant in each layer. The COV of the central values, spread and range of COV of soil properties are given in Table III.

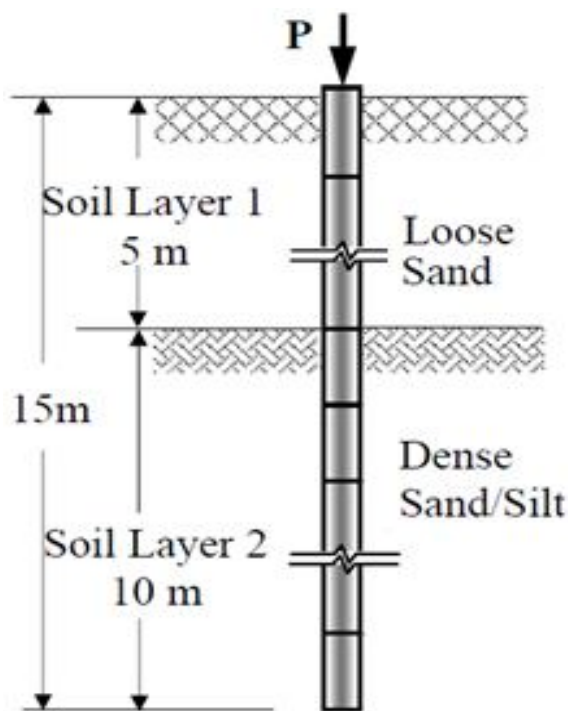


Fig. 6. Axially loaded single pile

From Fig. 7,

Critical pile tip movement $z_t = 3.0$ cms.

Critical pile shaft movement $z_s = 0.25$ cms in soil layers 1 and 2.

The q - z curve may be expressed as [10];

$$q = \begin{cases} q_{\max} \left(\frac{z}{z_t} \right)^{1/3} & \text{for } z \leq z_t \\ q_{\max} & \text{for } z > z_t \end{cases} \quad \dots (11)$$

The t - z curve for the given problem, as can be seen in Fig. 7, is linear and for calculation purpose, it may be expressed as [10];

$$f = \begin{cases} f_{\max} \left(\frac{z}{z_s} \right) & \text{for } z \leq z_s \\ f_{\max} & \text{for } z > z_s \end{cases} \quad \dots (12)$$

where,

f = unit shaft resistance at any pile shaft movement, z .

f_{\max} = unit shaft resistance mobilized at critical pile shaft movement, z_s .

q = unit base resistance for any pile tip movement, z .

q_{\max} = unit base resistance for critical pile tip movement, z_t .

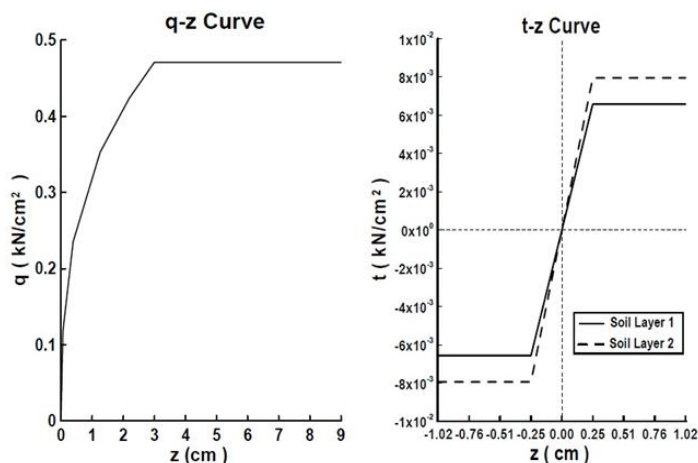


Fig. 7. q-z curve for layer 2 and t-z curves for layer 1 and 2

TABLE II.
PILE PROPERTIES AND LOAD DATA

Parameters involved	Central value (m_x)	COV (δ_x)	Variation (s_x)	Range ($\alpha_x=3^* s_x$)	Type of variable
Young's modulus of concrete (E , kN/cm ²)	2462	6.0	147.72	443.16	Triangular fuzzy set
Compressive strength of pile (σ_{ck} , kN/cm ²)	2.746	10.0	0.2746	0.8238	Triangular fuzzy set
Cross section area of the pile (A , cm ²)	706.90	5.0	35.345	106.035	Triangular fuzzy set
Axial load at the pile head (P , kN)	800	15.0	120	360	Triangular fuzzy set

D. Limit state functions

A pile-soil system can fail by excessive vertical movement of pile shaft, representing serviceability failure and also it can fail in strength. Each limit state needs to be considered separately. In the present study, three limit state functions for an axially loaded pile-soil system are considered;

E. Pile strength limit state

The strength parameters involved in pile compressive strength limit state are compressive strength of the concrete, σ_{ck} and cross sectional area, A of the pile and the axial compressive load, P is the action on the pile.

The limit state function is given by Equation (17) and all the three variables are considered as triangular fuzzy numbers.

$$g_{\sigma} = \sigma_{ck} - \frac{P}{A} \quad \dots (13)$$

F. Excessive settlement limit state

The limit state function in excessive vertical displacement at top of the pile is given by,

$$g_z = z_{allow} - z \quad \dots (14)$$

Where z_{allow} is the specified vertical displacement at top of the pile which is assumed to be 1.00 cm and z is the settlement at the top of the pile under applied load.

G. Soil resistance limit state

The soil resistance limit state function is given by Equation (15).

$$g_Q = (A_b q_{max} + A_s f_{max}) - (Q_p + Q_s) \quad \dots (15)$$

q_{\max} is unit base resistance mobilized at critical pile tip movement.

f_{\max} is unit shaft resistance mobilized at critical pile shaft movement.

A_b is area of the pile base.

A_s is circumferential area of the pile.

Q_p and Q_s are tip and friction reaction forces of the pile due to applied load.

TABLE III.
DATA OF SOIL PROPERTIES

Soil properties	m_x	δ_x	$\delta(m_x)$	$\delta(s_x)$	α_x	Type of variable
Unit tip resistance (q_{\max} , kN/cm ²)	0.4707	20	9	3	0.3078	Trapezoidal fuzzy set
Unit frictional resistance in layer 1 (f_{\max} , kN/cm ²)	6.571×10^{-3}	15	9	3	3.223×10^{-3}	Trapezoidal fuzzy set
Unit frictional resistance in layer 2 (f_{\max} , kN/cm ²)	7.944×10^{-3}	15	9	3	3.897×10^{-3}	Trapezoidal fuzzy set

For the reliability analysis in settlement and soil resistance limit states, the sectional area, material properties of pile and load are considered to be deterministic since they are not of much importance compared to the soil properties.

Prior to reliability analysis, the pile analysis is carried out to get the fuzzy sets for pile head settlement, reactive forces developed due to applied axial load, $P=800$ kN using load-transfer method[7]. Then fuzzy reliability analysis is performed using the two methods explained in the previous sections.

H. Results obtained for pile analysis using load-transfer method

The fuzzy sets obtained from load-transfer method for settlement z and reactive forces Q_p and Q_s are shown in Fig. 8, 9 and 10.

I. Results of reliability analysis of pile using possibilistic and fuzzy method

The results of reliability analysis of the single pile subjected to axial compressive load in three limit states considered are given in Table IV, it is noted that the reliabilities estimated using both the methods are same for all the three limit states considered. Reliability of pile against settlement limit state is 1.00 and also the safety index, λ is high, suggesting that the pile is safe against failure due to vertical settlement criteria. Reliability of the pile against pile strength limit state is also high compared to the reliability against soil resistance limit state.

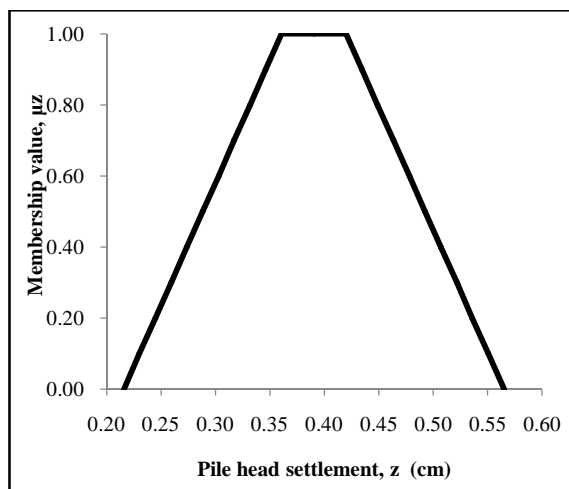


Fig. 8. Fuzzy set of pile settlement, z at top

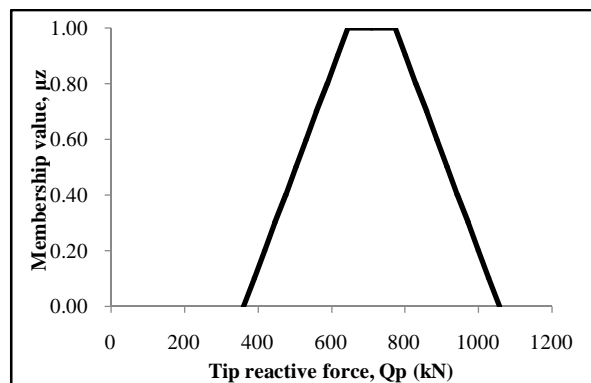
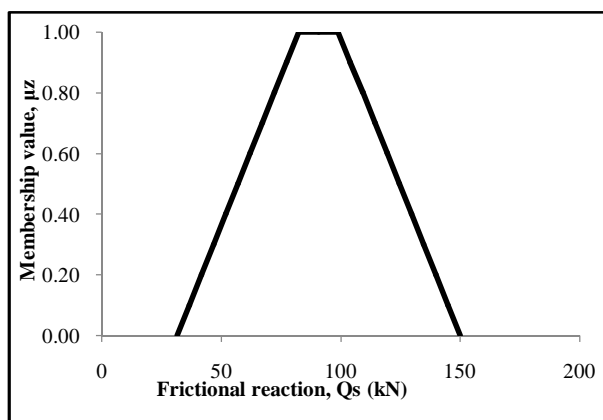

Fig. 9. Fuzzy set of reactive force, Q_p at pile tip

Fig. 10. Fuzzy set of frictional reaction, Q_s

TABLE IV.

RESULTS OF FUZZY RELIABILITY ANALYSIS OF AXIALLY LOADED SINGLE PILE

	Results of Fuzzy set theory method			Results of Possibilistic method		
	R^*	R_*	Π_f	Π_f	R_0	λ
Limit state						
Pile strength	1.00	0.995	0.00478	0.005	0.995	2.314
Settlement	1.00	1.000	0.00000	0.000	1.000	Indeterminate
Soil resistance	1.00	0.416	0.58396	0.584	0.416	0.733

VIII. CONCLUDING SUMMARY

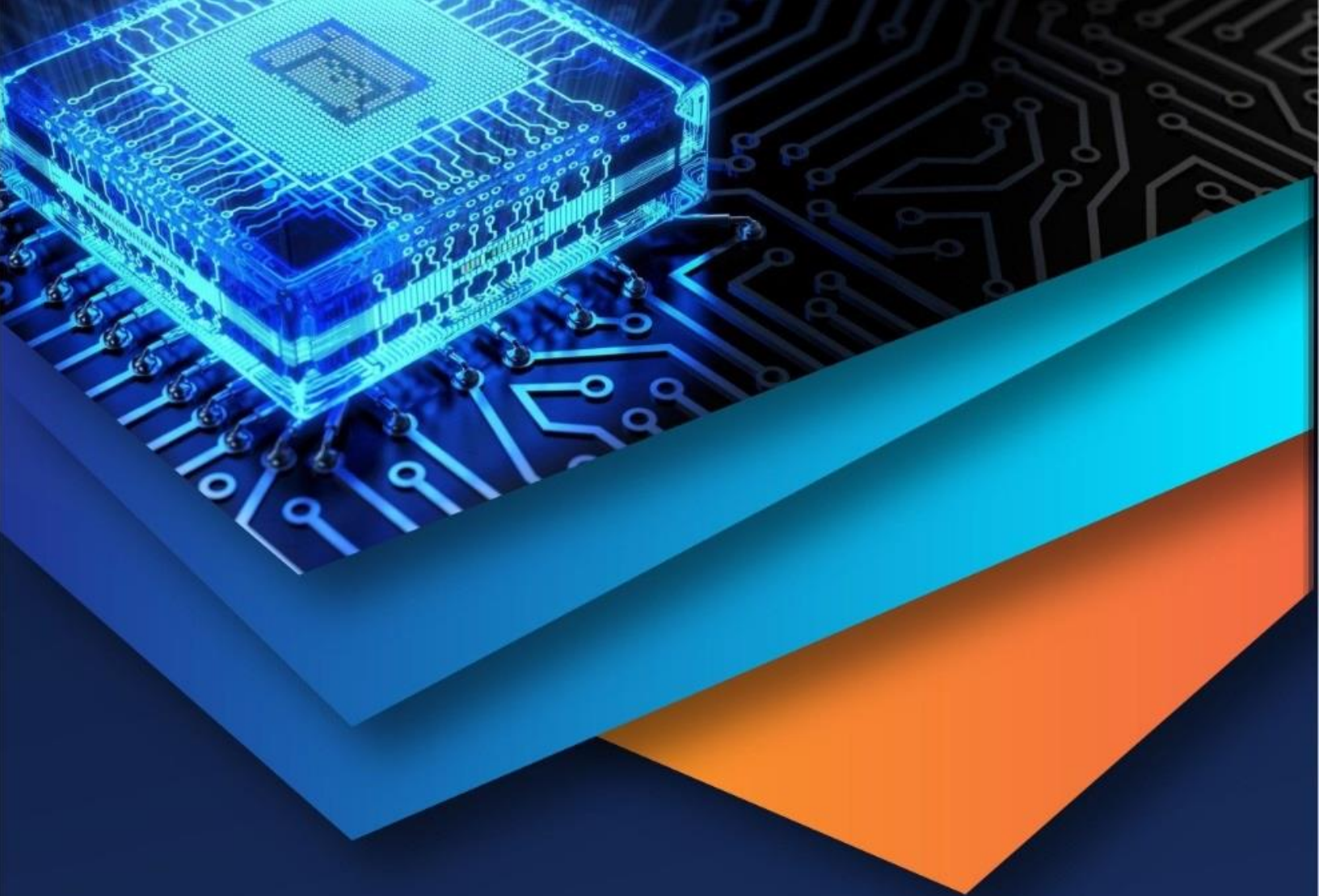
An attempt has been made to perform reliability analyses in the frameworks of possibility- and fuzzy set- theory. The reliability analyses based on the two methods are illustrated with a numerical example of axially loaded single pile. From the results obtained, it is noted that the reliability values obtained from both the methods are more or less the same, for all the three limit states considered. However, the computations involved in fuzzy set theory method are comparatively simpler. Also, by using this method, the bounds of reliability can be obtained. Hence, the fuzzy set theory method is recommended for carrying out fuzzy reliability analysis of structural components.

IX. ACKNOWLEDGEMENT

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REFERENCES

- [1] Barbara Ferracuti and Isaac Elishakoff, "Fuzzy sets based interpretation of the safety factor", Fuzzy sets and Systems, Elsevier, Vol. 157, 2006, pp 2495-2512.
- [2] Coyle, H. M. and Reese, L. C., "Load Transfer of Axially Loaded Piles in Clay", Journal of Soil Mechanics and Foundation Division, ASCE, Vol. 92, SM 2, March 1966, pp 1-26.
- [3] Cremona, C. and Gao, Y., "The possibilistic reliability theory: theoretical aspects and applications", Structural Safety, Elsevier, Vol. 19 (2), 1997, pp 173-201.
- [4] Datta, D., "Measures of sensitivity and uncertainty with the fuzzy model of solute transport through groundwater", Computational Radiation Physics Section, Health Physics Division, Bhabha Atomic Research Centre, Mumbai.
- [5] Fred H. Kulhawy, Kok-Kwang Phoon and Widjojo A. Prakoso, "Uncertainty in basic properties of geomaterials", 2000.
- [6] Haldar, A., et.al., "Probabilistic reliability estimation of an axially loaded pile", The Twelfth International Conference of "International association for Computer Methods and Advances in Geomechanics", Goa, October 2008, pp 1811-1817.
- [7] Joseph E. Bowles, "Foundation analysis and design", Mc-Graw Hill Book Co., New York, 5th Edition, 1996.
- [8] Marco Savoia, "Structural reliability analysis through fuzzy number approach, with application to stability", Computers and structures, Elsevier, Vol. 80, 2002, pp 1087-1102.
- [9] Ranganathan, R., "Reliability analysis and design of structures", Tata Mc-Graw Hill publications, New Delhi.
- [10] Swami Saran, "Analysis and design of substructures: Limit state design", Oxford and IBH Publishing Co. Pvt. Ltd., New Delhi, 2nd Edition, 2006.
- [11] Vijayavergiya, V. N., "Load distribution for a drilled shaft in clay shale", Ph.D. Dissertation, The University of Texas at Austin, Texas, 1969.
- [12] William M. Bulleit, "Uncertainty in structural engineering, Practice Periodical on Structural Design and Construction, ASCE, Vol. 13 (1), February 2008, pp 24-30.



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