



# **iJRASET**

International Journal For Research in  
Applied Science and Engineering Technology



---

# **INTERNATIONAL JOURNAL FOR RESEARCH**

IN APPLIED SCIENCE & ENGINEERING TECHNOLOGY

---

**Volume: 3**

**Issue: III**

**Month of publication: March 2015**

**DOI:**

**[www.ijraset.com](http://www.ijraset.com)**

**Call: ☎ 08813907089**

**E-mail ID: [ijraset@gmail.com](mailto:ijraset@gmail.com)**

# A Predictive Solution to Unbalanced-Voltage Problem in Wind Turbine Using Four-leg Indirect Matrix Converter

Max Savio<sup>#1</sup>

<sup>#</sup>Department of Electrical and Electronics Engineering, Jeppiaar Institute of Technology, Chennai, India

**Abstract**— In this paper, a four leg indirect matrix converter (IMC) is presented for the solution to unbalanced voltage in wind turbines. The wind driven PMSG is used as a generator for the power supply. The four leg indirect matrix converter is eliminates the unbalanced power supply problems that are common in the wind power generation due to variable input parameters. The zero sequence is developed between the output voltage supply of the wind generator thereby the unbalanced voltage levels are balanced and the output power factor is maintained. The zero sequence is generated efficiently as there is no DC link between the two converter stages of the IMC. This produces the zero vector in the inverter voltage thereby the power factor is improved. Simulation using MATLAB is presented and the results are compared.

**Keywords**— AC-AC Converter, Permanent Magnet Synchronous Generator, Space Vector Modulation, DC Link, Wind Energy

## I. INTRODUCTION

Wind energies are most desired power generation units for more years. Various researches over years have introduced various techniques to improve the power output from the wind turbines. Many industrial applications that are in demand of power consumption have created power crisis in many countries. The power demands are being solved by introducing renewable energy. However the generated power using the renewable energy, wind turbines particularly have a variable output power due to variable inputs which is unavoidable. Solution to this was the power electronics device that converts the variable power to fixed power. Moreover, still problems exists under some constrains of unbalanced power generation. This is very critical issue and challenge to many industries generating power supplies. The solution to unbalanced supply is explained using the four-leg indirect matrix converter [1]. The IMC [3] is an AC-AC converter that is simpler compared to matrix converter. The complexity is reduced in IMC. The four-leg IMC used extra pair of inverter switches that is connected to the neutral of the power supply. The synchronisation is developed such that the neutral link balances the output voltage and current. In the proposed method a PMSG is used as the Wind turbine model. The mathematical modeling of PMSG is done using MATLAB [2], [7].

In the proposed system, the PMSG wind turbine gets the mechanical input. The PMSG is designed to give an unbalanced output voltage. The unbalanced output from PMSG is given to the four-leg indirect matrix converter. The converter output is measured across a RL load. The output obtained is a balanced voltage and current with improved power factor.

## II. MATLAB MODELING OF PROPOSED WIND DRIVEN PMSG

The voltage equation of the Permanent Magnet Synchronous Generator (PMSG) is used in the MATLAB for the mathematical modeling. The voltage equations can be represented as,

$$\begin{aligned}V_a &= i_a R_s + p\varphi_a \\V_b &= i_b R_s + p\varphi_b \\V_c &= i_c R_s + p\varphi_c\end{aligned}$$

Where,  $p = \frac{d}{dt}$ ,  $i_a$ ,  $i_b$  and  $i_c$  are the phase currents,  $\varphi_a$ ,  $\varphi_b$  and  $\varphi_c$  are the flux developed by the phase currents and  $R_s$  is the stator resistance.

$$\begin{bmatrix} \varphi_a \\ \varphi_b \\ \varphi_c \end{bmatrix} = \begin{bmatrix} L_{sl} + L_{aa}(\theta_{er}) & L_{ab}(\theta_{er}) & L_{ca}(\theta_{er}) \\ L_{ab}(\theta_{er}) & L_{sl} + L_{aa}(\theta_{er}) & L_{bc}(\theta_{er}) \\ L_{ca}(\theta_{er}) & L_{bc}(\theta_{er}) & L_{sl} + L_{cc}(\theta_{er}) \end{bmatrix} \begin{bmatrix} i_a \\ i_b \\ i_c \end{bmatrix} + \begin{bmatrix} \varphi_{PMa}(\theta_{er}) \\ \varphi_{PMb}(\theta_{er}) \\ \varphi_{PMc}(\theta_{er}) \end{bmatrix}$$

Where,  $\theta_{er}$  is the rotor PM axis angle to a axis / electrical angle

For the distributed windings of IPM rotor machines,  $\theta_{er}$  is more efficiently considered as the self-inductance and mutual inductance mainly depend on it. But the stator inductance is invariant for the surface PM Pole rotors. The additional factor depending on the stator inductance on  $N_s \theta_{er}$  is due to the existence of slot openings. In consideration with the rotor pole configurations, the stator self and mutual inductance are similar catheterized for the concentrated windings. Contradictorily, the

## International Journal for Research in Applied Science & Engineering Technology (IJRASET)

distributed windings are larger in values. However, the concentrated windings have smaller end-turn leakage inductance. The space harmonics are also one of the factors to be considered in the fluxes of the permanent magnet machines.

Therefore, with this fact the modeling of the machine takes the assumption that, self and the mutual inductance are either constant or vary sinusoidally with the rotor position ( $2\theta_{er}$ ). In general, the flux linkages  $\varphi_{PMa,b,c}(\theta_{er})$  variation in the stator phases are sinusoidal but with  $\theta_{er}$ . Eventual the time pulsation in the torque and current are observed due to harmonics in the d-q model for the  $\omega_1=\omega_2$ :

$$|L_{abc}\theta_{er}| = \begin{vmatrix} L_{ls} + L_0 + L_2 \cos 2\theta_{er} & M_0 + L_2 \cos(2\theta_{er} + \frac{2\pi}{3}) & M_0 + L_2 \cos(2\theta_{er} - \frac{2\pi}{3}) \\ M_0 + L_2 \cos(2\theta_{er} + \frac{2\pi}{3}) & L_{sl} + L_0 + L_2 \cos(2\theta_{er} - \frac{2\pi}{3}) & M_0 + L_2 \cos 2\theta_{er} \\ M_0 + L_2 \cos(2\theta_{er} - \frac{2\pi}{3}) & M_0 + L_2 \cos 2\theta_{er} & L_{sl} + L_0 + L_2 \cos(2\theta_{er} + \frac{2\pi}{3}) \end{vmatrix}$$

$$M = -\frac{L_0}{2} \text{ for distributed windings}$$

Thus the matrix form of the phasor coordinates are given as,

$$|i_{a,b,c}| |R_s| - |V_{a,b,c}| = -\frac{d|\varphi_{a,b,c}|}{dt}$$

$$\varphi_{a,b,c} = |L_{a,b,c}\theta_{er}| |i_{a,b,c}| + \varphi_{PMa,b,c}(\theta_{er})$$

The Park's transformation from stator to rotor coordinates are given as in the Figure 2 are expressed as,

$$\begin{vmatrix} i_d \\ i_q \\ i_0 \end{vmatrix} = |P(\theta_{er})| \begin{vmatrix} i_a \\ i_b \\ i_c \end{vmatrix}$$

$$P(\theta_{er}) = \frac{2}{3} \begin{vmatrix} \cos(-\theta_{er}) & \cos(-\theta_{er} + \frac{2\pi}{3}) & \cos(-\theta_{er} - \frac{2\pi}{3}) \\ \sin(-\theta_{er}) & \sin(-\theta_{er} + \frac{2\pi}{3}) & \sin(-\theta_{er} - \frac{2\pi}{3}) \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{vmatrix}$$

The same transformations are valid for  $\varphi_{dq0}, V_{dq0}$ .

Finally, for sinusoidal  $\varphi_{PMa,b,c}(\theta_{er})$  distributions,

$$i_d R_s - V_d = L_d \frac{di_d}{dt} + \omega_r L_q i_q$$

$$i_q R_s - V_q = -L_q \frac{di_q}{dt} - \omega_r (L_d i_d + \varphi_{PM1})$$

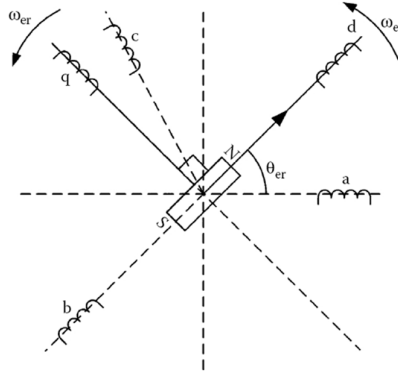


Fig. 2. Three Phase d-q transformation

With

$$\overline{\varphi_s} = \varphi_d + j\varphi_q; \varphi_d = \varphi_{PM1} + L_q i_d; \varphi_q = L_q i_q$$

$$\overline{V_s} = V_d + jV_q; \overline{i_s} = i_d + ji_q$$

From the above equations the space-vector model of the PMSG is obtained as,

$$\overline{i_s} - \overline{V_s} = -\frac{d\overline{\varphi_s}}{dt} - j\omega_r \overline{\varphi_s}$$

The torque is obtained as,

$$T_e = p_1 \frac{P_e}{\omega_r} = \frac{3}{2} p_1 (\varphi_{PM1} + (L_d - L_q) i_d) i_q$$

## International Journal for Research in Applied Science & Engineering Technology (IJRASET)

$$L_d = L_{sl} + \frac{3}{2}(L_0 - |L_2|); L_q = L_{sl} + \frac{3}{2}(L_0 + |L_2|)$$

From the derived expressions the d-q equivalent circuit of the PMSG is given as in the Fig 3.

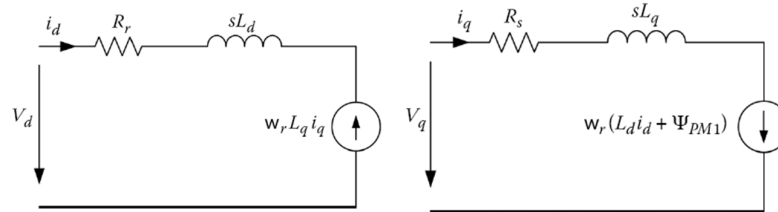


Fig. 3. d-q equivalent circuit of PMSG

The Fig 4 shows the vector representation of the PMSG. The torque value is in negative because of the current  $i_q$  which is negative. Under steady state condition, the phase voltages are given as,

$$V_{abc} = V_1 \sqrt{2} \cos \left( \omega_r t - (i - 1) \frac{2\pi}{3} \right)$$

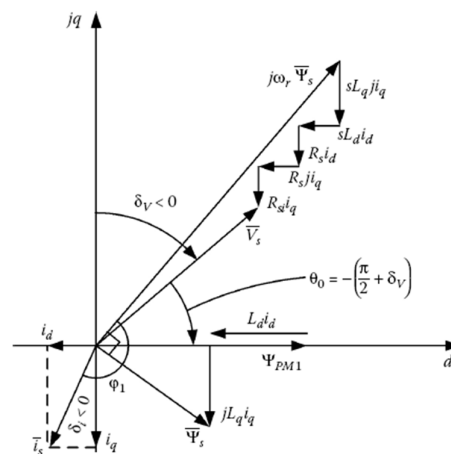


Fig. 4: Vector Representation of PMSG

### III. PROPOSED FOUR-LEG INDIRECT MATRIX CONVERTER

The proposed Four-leg Indirect Matrix Converter [1] is shown in the figure 5. The PMSG wind generator is connected to the load through the IMC. The IMC has two stages, one bidirectional rectification and inversion. The inversion stage consists of four-leg unidirectional switches. The weight of the power converter is reduced as the DC link components for the power storage is not present in the IMC.

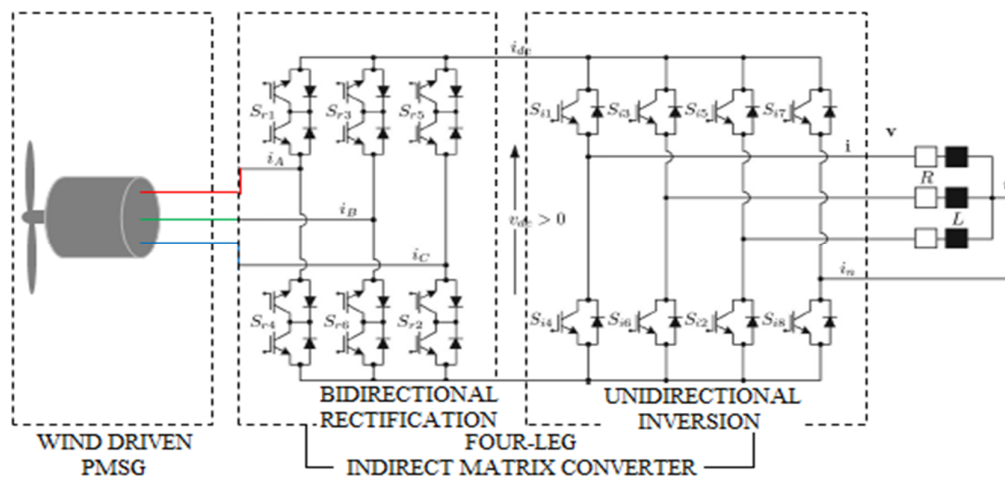


Fig. 5: Proposed Four-Leg Indirect Matrix Converter

## International Journal for Research in Applied Science & Engineering Technology (IJRASET)

By determining the relationship between the input and the output variables the mathematical modeling in MATLAB can be performed. The DC link voltage is  $v_{dc}$  is represented as,

$$V_{dc} = T_r v_i,$$

Where,

$$T_r = [S_{r1} - S_{r4} \ S_{r3} - S_{r6} \ S_{r5} - S_{r2}] \text{ and}$$

$$v_i = [v_A \ v_B \ v_C]$$

The DC link current  $i_i = [i_A \ i_B \ i_C]^T$  is represented as a function of the output current vector  $i = [i_u \ i_v \ i_w]^T$  and as a matrix function of the inversion stage,

$$i_{dc} = T_i i, \text{ where } T_i = [S_{i1} - S_{i7} \ S_{i3} - S_{i7} \ S_{i5} - S_{i7}]$$

The three phase output voltage,  $v = [u_u \ u_v \ u_w]^T$  can be represented as a function of DC-link voltage  $v_{dc}$  and the transpose of the matrix  $T_i$

$$v = T_i^T v_{dc}$$

Using the above equations the controller is used to produce the pulses in a sequence to produce a balanced output at the load side. The firing sequence of the rectifier and the inversion stage is shown in the table I and II respectively.

TABLE I  
RECTIFIER STAGE SWITCHING STATE

State	$S_r$ 1	$S_r$ 2	$S_r$ 3	$S_r$ 4	$S_r$ 5	$S_r$ 6
1	1	1	0	0	0	0
2	0	1	1	0	0	0
3	0	0	1	1	0	0
4	0	0	0	1	1	0
5	0	0	0	0	1	1
6	1	0	0	0	0	1
7	1	0	0	1	0	0
8	0	0	1	0	0	1
9	0	1	0	0	1	0

TABLE II  
INVERSION STAGE SWITCHING STATE

State	$S_i$ 1	$S_i$ 2	$S_i$ 3	$S_i$ 4	$S_i$ 5	$S_i$ 6	$S_i$ 7	$S_i$ 8
1	1	1	0	0	0	1	0	1
2	0	1	1	1	0	0	0	1
3	0	0	0	1	1	1	0	1
4	1	1	1	0		0	0	1
5	1	0	0	0	1	1	0	1
6	0	0	1	1	1	0	0	1
7	1	0	1	0	1	0	0	1
8	0	1	0	1	0	1	0	1
9	1	1	0		0	1	1	0
10	0	1	1	1	0	0	1	0
11	0	0	0	1	1	1	1	0
12	1	1	1	0	0	0	1	0
13	1	0	0	1	1	1	1	0
14	0	0	1	1	1	0	1	0
15	1	0	1	1	1	0	1	0
16	0	1	0	0	0	1	0	1



## International Journal for Research in Applied Science & Engineering Technology (IJRASET)

### IV. PROPOSED SIMULATION MODEL

The proposed system is mathematically modeled of a 4.5kW PMSG system. The wind driven PMSG is modeled to give an unbalanced reference output. The figure 6 shows the unbalanced voltage and current obtained from PMSG.

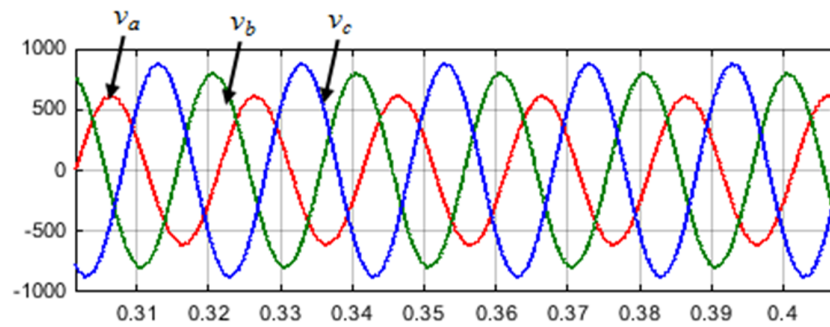


Fig 6. Unbalanced output of PMSG

The unbalanced voltage is corrected by the four-leg topology of IMC. The reference values of the current and the voltages are compared with the PMSG output, thereby the error is minimized to produce a balanced output voltage and current. The figure 7 shows the bidirectional DC voltage and current obtained in rectification stage.

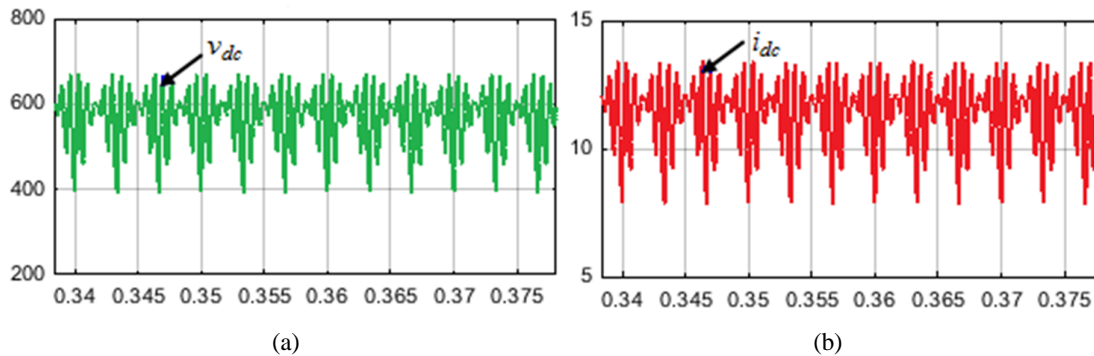


Fig 7. Bidirectional Rectification [M=0.8] (a) Voltage (b) Current

The rectified bidirectional outputs obtained are high level with no losses due to the absence of the dc link elements. The DC supply is then inverted in the inversion stage. The figure 8 shows the inverter balanced output voltage and current at the load side.

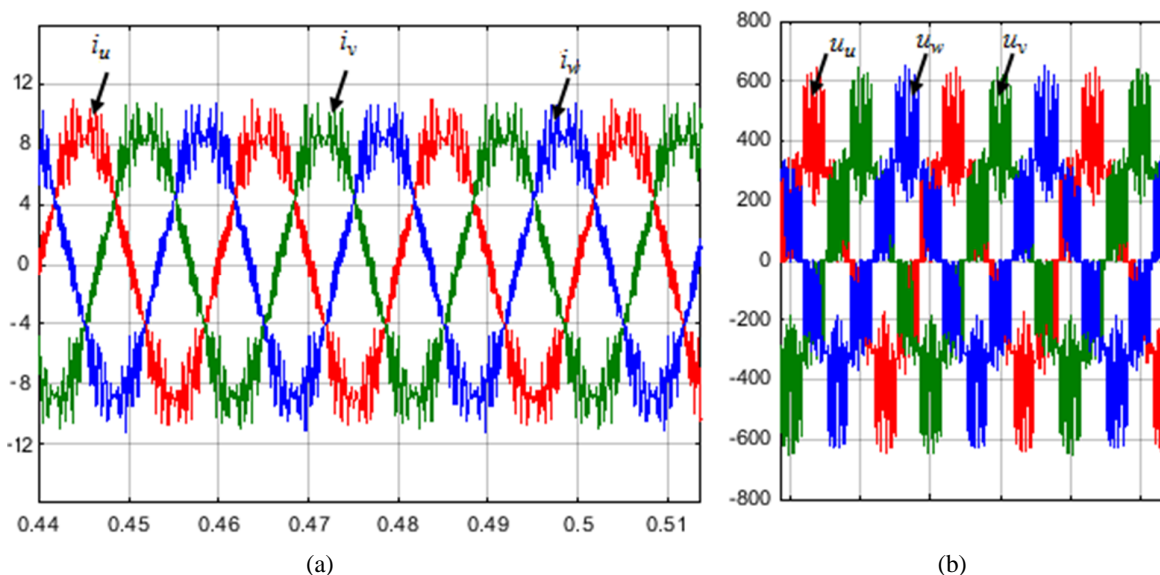


Fig 8: Balanced output [f=50Hz; M=0.7] (a) output load current (b) voltage output across the load

## International Journal for Research in Applied Science & Engineering Technology (IJRASET)

### V. CONCLUSION

Most wind turbine connected to weak power systems face the problem of unbalanced voltage conditions. This creates unequal heating in the generators causing damages to the windings. It is necessary to prevent such damages that particularly found in high power wind turbines. The proposed method uses a four leg indirect matrix converter where the three-phase unbalanced power supply is synchronized in two stages of power conversion. The mathematical modeling of PMSG is designed for an unbalanced system. The output of the PMSG wind model is connected to four-leg IMC so as to synchronize the unbalanced input to the balanced output. The output of the IMC is measured across the RL load of 1.5kW. The implementation of the four-leg IMC reduces the stress of unbalanced network thereby increasing the system performance. The system performance can be further improved through the filter circuits, however the cost will be proportionally increased with the filter circuits.

### VI. ACKNOWLEDGMENT

The author thanks the Director, Dr. N Marie Wilson, Jeppiaar Institute of Technology, Chennai, India for providing technical and financial support for the research work. The author also thanks the Dept. of Electrical and Electronics Engineering Jeppiaar Institute of Technology for providing a technical support.

### REFERENCES

- [1] Crisiti'an Garc'ia, Marco Rivera, Miguel L'opez, Jos'e Rodriguez, Rub'en Pe'na, Patrick W. Wheeler, Jos'e R. Espinoza, "A Simple current Control Strategy for a Four-Leg indirect Matrix Converter", IEEE Transactions on Power Electronics, vol. 30, no. 04, 2275-2287, April 2015.
- [2] Max Savio, M. Sasikumar, "A Supervisory Predictive Control using Indirect Matrix Converter for Variable Speed Wind Energy Conversion System", International referred Journal of Engineering Science, vol. 02, No. 10, pp. 39-47, Oct 2013.
- [3] P. Correa, J. Rodriguez, M. Rivera, J. R. Espinoza, and J. W. Kolar, "Predictive control of an indirect matrix converter," IEEE Trans. Ind. Electron., vol. 56, no. 6, pp. 1847-1853, Jun. 2009.
- [4] E. Reyes, R. Pena, R. Cardenas, J. Clare, and P. Wheeler, "A topology for multiple generation system with doubly fed induction machines and indirect matrix converter," in Proc. IEEE-ISIE, Cambridge, U.K., 2008, pp. 2463-2468.
- [5] Yang Mei, Gang Li and Kai Sun, "High Performance Control of IPMSM Drive Fed by Indirect Matrix Converter", Proceedings of IEEE 2011. pp. 1642 to 1647.
- [6] J. F. Conroy and R. Watson, "Low-voltage ride-through of a full converter wind turbine with permanent magnet generator," IET Renew. Power Gener., vol. 1, no. 3, pp. 182-189, Sep. 2007.
- [7] J. Y. Dai, D. D. Xu, and B. Wu, "A novel control scheme for current source-converter-based PMSG wind energy conversion systems," IEEE Trans. Power Electron., vol. 24, no. 4, pp. 963-972, Apr. 2009.
- [8] K. Amei, Y. Takayasu, T. Ohji, and M. Sakui, "A maximum power control of wind generator system using a permanent magnet synchronous generator and a boost chopper circuit," in Proc. PCC, Osaka, Japan, 2002, vol. 3, pp. 1447-1452.
- [9] S. Grabic, N. Celanovic, and V. A. Katic, "Permanent magnet synchronous generator cascade for wind turbine application," IEEE Trans. Power Electron., vol. 23, no. 3, pp. 1136-1142, May 2008.
- [10] M. Chinchilla, S. Arnaltes, and J. C. Burgos, "Control of permanent magnet generators applied to variable-speed wind-energy systems connected to the grid," IEEE Trans. Energy Convers., vol. 21, no. 1, pp. 130-135, Mar. 2006.
- [11] Z. Chen, J. M. Guerrero, and F. Blaabjerg, "A review of the state of the art of power electronics for wind turbines," IEEE Trans. Power Electron., vol. 24, no. 8, pp. 1859-1875, Aug. 2009.
- [12] Klumpner, and F. Blaabjerg, "Modulation method for a multiple drive system based on a two-stage direct power conversion topology with reduced input current ripple," IEEE Trans. on Power Electronics, vol.20, No.3, 2005, pp: 922-929.
- [13] Sasikumar M. and Chenthur Pandian S. (2010), 'Implementation of an impedance source inverter based variable speed wind driven self - excited induction generator,' Journal of Electrical Engineering (JEE), Vol.10, No.3, pp. 43 - 47.
- [14] Sasikumar M. and Chenthur Pandian S.(2010), 'Performance characteristics of self - excited induction generator fed current source inverter for wind energy conversion system,' International Journal of Computer and Electrical Engineering (IJCEE), Vol. 2, No. 6, pp. 1077-1080.
- [15] Sasikumar M. and Chenthur Pandian S. (2011), 'Modeling and Analysis of Cascaded H-Bridge Inverter for Wind Driven Isolated Self - Excited Induction Generators,' International Journal on Electrical Engineering and Informatics (IJEEI), Vol.3, No. 2, 2011, pp. 132-145.
- [16] J. W. Kolar, M. Baumann, F. Schafmeister, and H. Ertl, "Novel three phase AC-DC-AC sparse matrix converter," Proceedings of IEEE APEC2002, 2002, pp.777-791.
- [17] Gang Li, Kai Sun, Lipei Huang, "A novel algorithm for space vector modulated two-stage matrix converter," Proceedings of ICEMS2008, 2008, pp.1316-1320.
- [18] Mr. V. Y. Vekhande, Mr. B. B. Pimple and B. G. Fernandes, "Control of Indirect Matrix Converter under Unbalanced Source Voltage and Load Current Conditions," Fourth National Power Electronics Conference, IIT Roorkee, June 2010.



10.22214/IJRASET



45.98



IMPACT FACTOR:  
7.129



IMPACT FACTOR:  
7.429



# INTERNATIONAL JOURNAL FOR RESEARCH

IN APPLIED SCIENCE & ENGINEERING TECHNOLOGY

Call : 08813907089  (24\*7 Support on Whatsapp)