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VRP Using ACO MetaHeuristic

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Abstract— *Vehicle routing in present scenario is very complex issue where fleet of vehicles need to be ordered so as to cover the maximum distance in minimum cost. In this paper we propose an algorithm for solving vrp, that is, vehicle routing problem using ACO metaheuristic. The core objective is to minimize the number of vans to do the task and find out the best optimal route using Ant Colony Optimization (ACO). Finally, an example is also presented based on our research work.*

Keywords— *VRP, ACO, metaheuristic, CVRP, Phermone*

I. INTRODUCTION

In the Vehicle Routing Problem (VRP), a fleet of vehicles with limited capacity has to be routed in order to visit a set of customers at a minimum cost [1]. The basic VRP [2] consists of a number of customers, each requiring a specified weight of goods to be delivered. Each vehicle can carry limited weight and can cover limited distance. Vehicles dispatched from a single depot must deliver the goods required, and then return to the depot.

There are different variations of VRP such as vehicle routing problem with time windows (VRPTW), the capacitated vehicle routing problem (CVRP), the multi-depot vehicle routing problem (MDVRP), the site dependent vehicle routing problem (SDVRP) and the open vehicle routing problem (OVRP)[3].

In the CVRP one has to deliver goods to a set of customers with known demands at minimum cost. The vehicle must originate from and terminate at the same depot s .

The VRPTW extends the CVRP by associating time windows with the customers. Its objective is to serve the customers within the predefined time.

The OVRP is closely related to the CVRP, but contrary to the CVRP a route ends as soon as the last customer has been served as the vehicles do not need to return to the depot. The MDVRP extends the CVRP by allowing multiple depots. The SDVRP is another generalization of the CVRP.

In the SDVRP one can specify that certain customers only can be served by a subset of the vehicles, furthermore, vehicles

can have different capacities in the SDVRP.

In this paper we will consider Ant Colony Optimization for solving CVRP by taking into account the number of vans as the capacity constraints for the vehicles.

II. THE CAPACITATED VEHICLE ROUTING PROBLEM

The Capacitated Vehicle Routing Problem (CVRP)[2] concerns the design of a set of minimum cost routes, starting and ending at a single depot, for a fleet of vehicles to service a number of customers with known demands. It is the basic version of VRP [4]. It derives its name as it has the capacity constraint associated with it. Mathematically, it can be represented by a weighted graph $G = (V, A)$ with $V = \{0, 1, 2, \dots, n\}$ as the vertex set and $A = \{(i, j) \mid i, j \in V\}$ as the edge set. The depot is denoted as vertex 0 and the total of n cities or customers to be served are represented by the other vertices. For each edge (i, j) , d_{ij} is a nonnegative distance each measured using Euclidean computations. Each customer $i, i=1, 2, \dots, n$, is associated with a nonnegative demand d_i and a service time t_i which have to be satisfied. The demand at the depot is set to $d_0 = 0$ and its service time is set to $t_0 = 0$. Each vehicle is given a capacity constraint, Q . Consequently, the objective of the CVRP is to find a set of minimum cost routes to serve all the customers by satisfying the following constraints which are listed in Voss (1999): (i) each customer is visited exactly once by exactly one vehicle, (ii) all vehicle routes start and end at the depot, (iii) for each vehicle route, the total demand does not exceed the vehicle capacity Q and (iv) for each vehicle route, the total route length (including service times) does not exceed a given bound L . Since the CVRP is a NP-hard problem, only instances of small sizes can be solved to optimality using exact solution methods (Toth and Vigo, 2002; Baldacci *et al.*,

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2010). As a result, heuristic methods are used to find good, but not necessarily guaranteed optimal solutions using reasonable amount of computing time..

III. METAHEURISTIC ALGORITHMS

A Metaheuristic is a heuristic method for solving a very general class of computational problems. It attempts to provide an efficient framework which combines user given black-box procedures. Such procedures are usually application specific heuristics themselves. Metaheuristics [5] are generally applied to problems for which there is no satisfactory problem specific algorithm or heuristic; or when it is not practical to implement such a method. Most commonly used metaheuristic are targeted to combinatorial optimization problems.

A. Simulated Annealing

Simulated annealing is a generic probabilistic meta-algorithm for finding global optima in large search space [6]. It was inspired by the annealing process in metallurgy, a technique involving heating and controlled cooling of a material to increase the size of its crystals and reduce their defects. The heat causes the atoms to move from their initial positions (a local minimum of the internal energy) and wander randomly through states of higher energy; the slow cooling gives them a chance of finding configurations with lower internal energy than the initial one.

B. Genetic Algorithm

Genetic algorithms use techniques inspired by evolutionary biology such as inheritance, mutation, selection, and crossover (also called recombination) [6]. They essentially solve the problems under consideration by simulating the evolutionary process, in which a population of abstract representations (called chromosomes or the genotype or the genome) of candidate solutions (called individuals, creatures, or phenotypes) evolves toward better solutions.

C. Artificial neural network

Artificial neural networks borrow the concept from how the human brain processes information by using an interconnected group of artificial neurons [7]. In solving an optimization problem, artificial neural networks use a

mathematical model or computational model for information processing based on a connectionist approach, in which each processing unit is to simulate an individual neuron.

D. Ant colony metaheuristic

The Ant Colony Metaheuristic [8] is a relatively new addition to the family of nature inspired algorithms for solving N P-hard combinatorial problems. Also known as Ant Colony Optimization (ACO) or Ant System [10](AS) algorithm. The ACO algorithm is inspired by such observation. It is a population based approach where a collection of agents cooperate together to explore the search space. They communicate via a mechanism imitating the pheromone trails.

IV. ANT COLONY OPTIMIZATION

Ant Colony Optimization (ACO) is a paradigm for designing metaheuristic algorithms for combinatorial optimization problems. In all Ant Colony Optimization algorithms, each ant gets a start city. Beginning from this city, the ant chooses the next city according to algorithm rules. After visiting all customer cities exactly once, the ant returns to the start city. The ants might travel concurrently or in sequence. Each ant deposits some amount of pheromone on its path. The amount of pheromone depends on the quality of the ant's path: a shorter path usually results in a greater amount of pheromone. The deposited pheromone suffers from evaporation. The idea of the ant colony algorithm is to mimic this behaviour with "simulated ants" walking around the graph representing the problem to solve. The biology analogy of ant colony optimization is shown in fig1. During its path from nest to the food source, if the ant finds an obstacle, it tries to find the minimum path it could use so as to cover the minimum distance.

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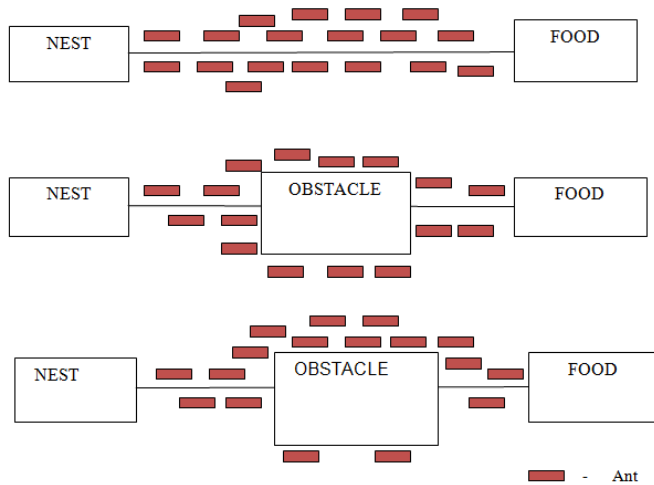


Fig1. Biological analogy of Ant colony optimization

V. FORMAL PROBLEM DEFINITION

We now present a mathematical formulation of the Capacitated Vehicle Routing Problem (CVRP). Each vehicle is given a capacity constraint, Q . Consequently, the objective of the CVRP is to find a set of minimum cost routes to serve all the customers by satisfying the following constraints which are listed in Voss (1999): (i) each customer is visited exactly once by exactly one vehicle, (ii) all vehicle routes start and end at the depot, (iii) for each vehicle route, the total demand does not exceed the vehicle capacity Q and (iv) for each vehicle route, the total route length (including service times) does not exceed a given bound L .

VI. PROPOSED SYSTEM

For solving this problem we have used a dynamic scenario. Our algorithm consists of the following steps:

Step 1: Generating a virtual environment

In this step an environment is created by deploying a number of customers, a depot and the vehicles used for serving the customers.

Step 2: Distance Probing

This step accounts for gathering the data about the deploying units. Also, at this step, the distance between the various units is calculated. This is divided into two phases:

Phase 1:- Initial Level-1 Distance probing,- Scouting units

will probe distances of each customer from the depot.

Phase 2:- N-Level Distance probing,- Scouting units will probe distances of each customer from every other customers.

Step3: Initial Route Building- This is carried out by using the following algorithm.

Algorithm:-

- While all nodes are not covered and agents are available for route building.
- Choose a free agent and start a new route. Select depot as start point.
- While agent capacity is not full
- Choose node at minimum distance from current position and add to route. Set node as current position.
- When agent capacity is full add depot as destination node and close route.

In this effort we strive to choose the nearest unoccupied node for adding in a route. This way we might be choosing the best node a particular instance of time, but considering the overall scenario this might not result in best route.

Step 4: - Level 1 Route optimization – Reordering nodes within a route to minimize total length of route.

A route consists of various nodes to be travelled in a specific order and hence total length of route can be determined. Greedy approach used for building route ensures the best node is chosen as next but the overall order is not controlled and may not be best.

Algorithm for internal route optimization

- Load current order of nodes and total route distance.
- Shuffle order of nodes.
- Re-probe total route distance.
- If new distance is lesser, update memory with new order of nodes
- Else discard the shuffled route.

Step 5: Level 2 Route optimization – Transferring nodes from a route to another route to minimize total length of both routes.

Even though after internal optimization of individual routes, the overall system may not be optimal. There can be scope of

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further reduction in total distance travelled for all routes in system.

Algorithm for Level 2 route optimization.

- For each route in system, find if exists a far-sighted node.
- Find a capable route to which far-sighted node can be transferred.
- Remove node from original route and add node to chosen route.
- Internally optimize both routes and re-probe the distances of these two routes
- If the combined distance of both routes reduces then the change is made permanent and updated in memory.
- Else the change is discarded.
- Repeat while no more transferrable-far-sighted nodes are present.

VII. RESULT AND ANALYSIS

Step1: Creating a virtual environment

In fig2, we have shown an example in which there is a centrally located depot and around 15 customers

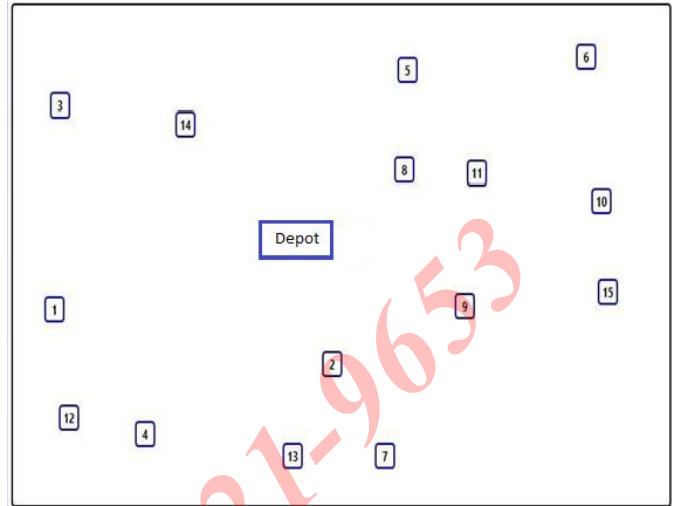


Fig2. Example step 1 node deployment

Step 2: Distance probing

Fig.3 shows the route calculation step.

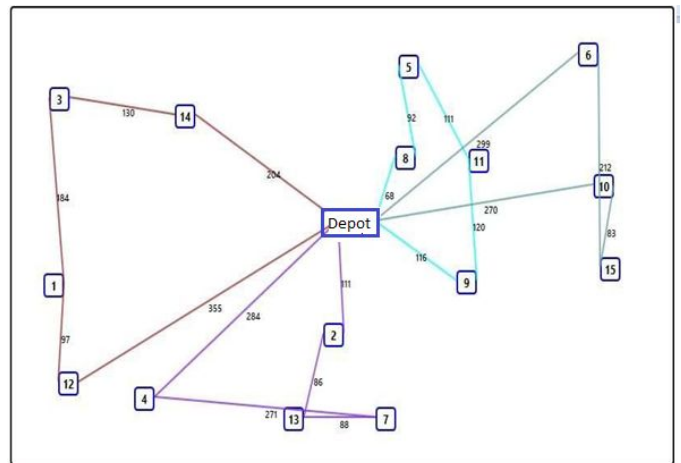


Fig.3.Route calculation step

This step is carried out by using a route calculation table which is shown in table1.

TABLE1-Route calculation table

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Agent	Current Position	Closest unoccupied node	Route
1	Depot	8	D
	8	5	D-8
	5	11	D-8-5
	11	9	D-8-5-11
	9		D-8-5-11-9
	Depot		D-8-5-11-9-D
2	Depot	2	D
	2	13	D-2
	13	7	D-2-13
	7	4	D-2-13-7
	4		D-2-13-7-1
	Depot		D-2-13-7-4-D
3	Depot	14	D
	14	3	D-14
	3	1	D-14-3
	1	12	D-14-3-1
	12		D-14-3-1-12
	Depot		D-14-3-1-12-D
4	Depot	10	D
	10	15	D-10
	15	6	D-10-15
	6		D-10-15-6
	Depot		D-10-15-6-D

After optimization (optimized order)

Paths 2-13 (86) & 7-4 (271) are removed, while Paths 2-7 (91) & 13-4(159) are added.

Route1(Purple)=>D-2-7-13-4-D=>
(111+91+88+159+284=733)

Route 4: Before optimization (actual order)

Route 4(Cadet Blue) => D-10-15-6-D=> (270+83+212+299=864)

After optimization (optimized order)

Paths D-10(270) & 15-6(212) are removed, while Paths D-15(279) & 10-6(130) are added.

Initial Routes are calculated and marked with different colours.

Each path in route is also marked with its length.

Following Routes are calculated:

Route1 (Aqua) =>D-8-5-11-9-D=> (68+92+111+120+116=507)

Route2(Purple)=>D-2-13-7-4-D =>
(111+86+88+271+284=840)

Route3(Brown)=>D-14-3-1-12-D=>
(204+130+184+97+355=970)

Route4(CadetBlue) => D-10-15-6-D=>
(270+83+212+299=864) Step3: Level 1 Optimization (Route Order Shuffling)

Level 1 Optimization is applied on all routes and improvement are noticed in routes 2, 4

Route 2:Before optimization (actual order)

Route2(Purple)=>D-2-13-7-4-D=>
(111+86+88+271+284=840)

Route4(Cadet Blue) => D-15-10-6-D=>
(279+83+130+299=791).

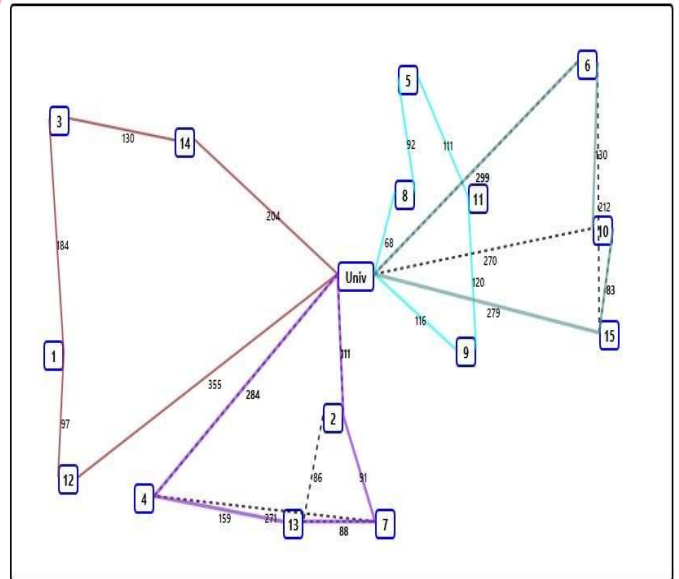


Fig.4.Route optimization

Analysis: From the above results, we found that it produced satisfactory results. Initially, the route calculated was not the optimal one. It could produce the better results but after

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optimization, the route improved and was optimal. There was reduction in the distance travelled as shown in the fig.5.

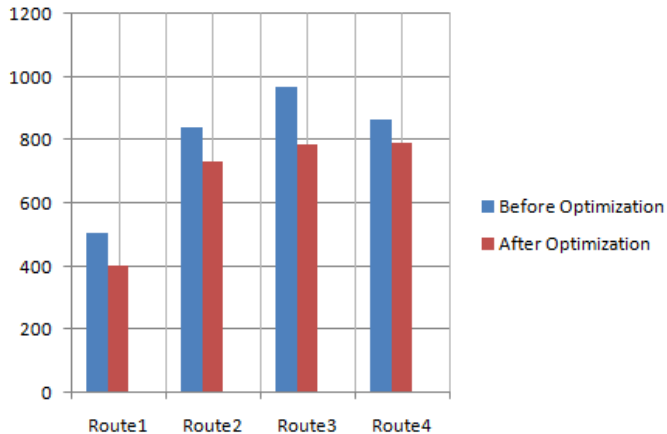


Fig. Reduction in average route length through optimization

VIII. CONCLUSION

A dynamic approach for solving vrp is studied in this paper. Comparatively small amount of memory can be used for marking, allocation and calculations. In this paper, the distance from each node was calculated and then optimal route was found through route optimization. This was done using ACO approach.

Future work will be conducted to improve the proposed algorithm. It is possible to achieve further optimization of routes by transferring/ exchanging nodes between two routes and increasing the number of nodes.

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