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# **On Semi-T**<sub>1/2</sub> Spaces

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Abstract: In this paper we introduce new types of Semi-T<sub>1/2</sub> spaces using sg-closed type sets. We define new topological ordered spaces namely semi- $_{sgi}T_{1/2}$  space, semi- $_{sgd}T_{1/2}$  space, semi- $_{sgb}T_{1/2}$  space, semi- $_{sgb}T_{1/2}$  space, semi- $_{sgi}T_{is,1/2}$  space, semi- $_{sgd}T_{ds,1/2}$  space and semi- $_{sgb}T_{bs,1/2}$  space. We lso establish relationships between these spaces. Mathematics subject classification: 54A05

Keywords: Topological ordered space, i-closed set, d-closed set, b-closed set, sg-closed set, Semi- $T_{1/2}$ , space.

#### I. INTRODUCTION

L.Nachbin [1] initiated the study of Topological ordered spaces (TOS). A topological ordered space is a topological space in which a partial order is available. Using order relation one can think of increasing, decreasing and balanced sets. N. Levine [5] defined generalized closed (briefly g-closed) set in 1970 by slightly weakening the notion of closedness. They are not only the natural generalizations of closed sets but they can suggest more properties of topological spaces. In recent years, some authors have introduced notions which uses both topological and order structure, for example generalized increasing sets.

Let X be a non-empty set. A TOS is a triple  $(X, \tau, \leq)$  where " $\tau$ " is a topology and " $\leq$ " is a partial order on X. For any  $x \in X$ , the sets  $[x, \rightarrow]$  and  $[\leftarrow, x]$  are defined as  $[x, \rightarrow] = \{y \in X / x \leq y\}$  and  $[\leftarrow, x] = \{y \in X / y \leq x\}$ . A subset A of a TOS  $(X, \tau, \leq)$  is said to be increasing if A = i[A] and decreasing if A = d[A] where  $i[A] = \bigcup_{a \in A} [a, \rightarrow]$  and  $d[A] = \bigcup_{a \in A} [\leftarrow, a]$ . The complement of an increasing set is a decreasing set and vice versa. A subset of a TOS  $(X, \tau, \leq)$  is said to be balanced if it is both increasing and decreasing. M.K.R.S.Veera Kumar [2] introduced the study of increasing closed set (briefly i-closed), decreasing closed set (briefly d-closed) and balanced closed set (briefly b-closed) in

2001. N. Levine [4] introduced semi-open sets. The complement of a semi-open set is a semi-closed set. Bhattacharya & Lahiri [6] introduced and studied semi-generalized sets (briefly sg-closed).

#### **II. PRELIMINARIES**

Throughout this paper  $(X, \tau)$  represent a non-empty topological space on which no separation axioms are assumed unless otherwise mentioned. For a subset A of a topological space  $(X, \tau)$ , the intersection of all closed sets containing A is called closure of A denoted by cl(A) and the intersection of semi-closed sets containing A is called the semi-closure of A denoted by scl(A). We recall the following definitions.

A. Definition 2.1.

A subset A of a topological space  $(X,\tau)$  is called a semi-open set [4] if  $A \subseteq cl(int(A))$  and a semi-closed set if  $int(cl(A)) \subseteq A$ .

B. Definition 2.2.

- A subset A of a topological space  $(X, \tau)$  is called
- 1) a generalized closed set (briefly g-closed)[5] if  $cl(A) \subseteq U$  whenever  $A \subseteq U$  and U is open in  $(X, \tau)$ . The complement of a g-closed set is a g-open set.
- 2) a semi-generalized closed set (briefly sg-closed)[6] if  $scl(A) \subseteq U$  whenever



 $A \subseteq U$  and U is semi-open in  $(X, \tau)$ . The complement of a sg-closed set is

a sg-open set.

## C. Definition 2.3 [7]

A subset A of a topological ordered space  $(X, \tau, \leq)$  is called

1) a semi generalized increasing closed (briefly sgi-closed) set if A is a sg-closed set and an increasing set.

2) a semi generalized decreasing closed (briefly sgd-closed) set if A is a sg-closed set and a decreasing set.

3) a semi generalized balanced closed (briefly sgb-closed) set if A is a sg-closed set and a balanced set.

In view of the above definitions, we have every sgb-closed set is sgi-closed and sgd-closed also. [9]

## D. Definition 2.4 [7]

A topological ordered space  $(X, \tau, \leq)$  is called a  $semi - T_{1/2}$  space if every sg-closed set is semi-closed.

## III. SEMI-T<sub>1/2</sub> SPACES DEFINED USING SG-CLOSED TYPE SETS

In this section, we introduce new types of Semi- $T_{1/2}$  spaces using sgi-closed, sgd-closed and sgb-closed sets.

A. Definition 3.1: [8]

A topological ordered space  $(X, \tau, \leq)$  is called

- 1) a semi- $_{sgi}T_{1/2}$  space if every sgi-closed set is semi-closed.
- 2) a semi- $_{sgd} T_{1/2}$  space if every sgd-closed set is semi-closed.
- 3) a semi-sep  $T_{1/2}$  space if every sgb-closed set is semi-closed.

## B. Example 3.2.

Consider the set  $X = \{a, b, c\}$  with the topology  $\tau_8 = \{\phi, X, \{a, b\}\}$  and partial order  $\leq_4 = \{(a, a), (b, b), (c, c), (a, b), (c, a), (c, b)\}$ . Then,  $(X, \tau_8, \leq_4)$  is a topological ordered space. Semi-closed sets in this space are  $\phi$ , X,  $\{c\}$ . Increasing sets in this space are  $\phi$ , X,  $\{b\}$ ,  $\{a, b\}$ . Also, sg-closed sets are  $\phi$ , X,  $\{c\}$ ,  $\{b, c\}$ ,  $\{a, c\}$ . Then, sgi-closed sets are  $\phi$ , X. Clearly, every sgi-closed set is a semi-closed set. So, the space  $(X, \tau_8, \leq_4)$  is a semi-sgi  $T_{1/2}$  space.

## C. Example 3.3

Consider the set  $X = \{a, b, c\}$  with the topology  $\tau_8 = \{\phi, X, \{a, b\}\}$  and partial order  $\leq_1 = \{(a, a), (b, b), (c, c), (a, b), (a, c), (b, c)\}$ . Then,  $(X, \tau_8, \leq_1)$  is a topological ordered space. Semi-closed sets in this space are  $\phi$ , X,  $\{c\}$ . Sg-closed sets are  $\phi$ , X,  $\{c\}$ ,  $\{b, c\}$ ,  $\{a, c\}$  and decreasing sets are  $\phi$ , X,  $\{a\}$ ,  $\{a, b\}$ . Then, sgd-closed sets are  $\phi$ , X. Clearly, every sgd-closed set in X is a semi-closed set. So, the space  $(X, \tau_8, \leq_1)$  is a *semi* –  $sed T_{1/2}$  space.

## D. Example 3.4

Consider the set  $X = \{a, b, c\}$  with the topology  $\tau_8 = \{\phi, X, \{a, b\}\}$  and partial order  $\leq_1 = \{(a, a), (b, b), (c, c), (a, b), (a, c), (b, c)\}$ . Then,  $(X, \tau_8, \leq_1)$  is a topological ordered space. Semi-closed sets in this space are  $\phi$ , X, {c}. Balanced sets in this space are  $\phi$ , X and sg-closed sets are  $\phi$ , X, {c}, {b, c}, {a, c}. Then, sgb-closed sets are  $\phi$ , X. Clearly, every sgb-closed set in X is a semi-closed set. So, the space  $(X, \tau_8, \leq_1)$  is a semi- $seh \frac{T_1}{2}$  space.

#### IV. RELATIONSHIPS BETWEEN SEMI-T<sub>1/2</sub> SPACES

In this section we establish relationships between  $semi - T_{1/2}$  and  $semi - sgi T_{1/2}$ ,  $semi - sgd T_{1/2}$  and  $semi - sgb T_{1/2}$  spaces. We also establish independency of some of the spaces.



A. Theorem 4.1

Every  $semi - T_{1/2}$  space is a  $semi - sgi T_{1/2}$  space but not conversely.

- 1) Proof: Let  $(X, \tau, \le)$  be a  $semi T_{1/2}$  space and A be a sgi-closed set in X. Then, A is a sg-closed set. Since X is a  $semi T_{1/2}$  space, A is a semi-closed set. Therefore, every sgi-closed set in X is a semi-closed set. Hence, the space  $(X, \tau, \le)$  is a  $semi \frac{1}{sgi}T_{1/2}$  space.
- 2) The following example shows that the converse is not true.: Consider the set  $X = \{a, b, c\}$  with the topology  $\tau_8 = \{\phi, X, \{a, b\}\}$ and partial order  $\leq_4 = \{(a, a), (b, b), (c, c), (a, b), (c, a), (c, b)\}$ . Then,  $(X, \tau_8, \leq_4)$  is a topological ordered space. Semi-closed sets in this space are  $\phi$ , X, {c}. Increasing sets in this space are  $\phi$ , X, {b}, {a, b}. Also, sg-closed sets are  $\phi$ , X, {c}, {b, c}, {a, c}. Then, sgi-closed sets are  $\phi$ , X. Clearly, every sgi-closed set is a semi-closed set. So, the space  $(X, \tau_8, \leq_4)$  is a  $semi - sgi T_{1/2}$  space. The subset {b, c} is a sg-closed set but not a semi-closed set. Hence, the space  $(X, \tau_8, \leq_4)$  is not a  $semi - T_{1/2}$  space.

## B. Theorem 4.2

Every  $semi - T_{1/2}$  space is a  $semi - sgd T_{1/2}$  space but not conversely.

- Proof: Let (X, τ, ≤) be a semi-T<sub>1/2</sub> space and A be a sgd-closed set. Then, A is a sg-closed set. Since X is a semi-T<sub>1/2</sub> space, A is a semi-closed set. Therefore, every sgd-closed set in X is a semi-closed set. Hence, the space (X, τ, ≤) is a semi-sgd T<sub>1/2</sub> space.
- 2) The following example shows that the converse is not true.: Consider the set  $X = \{a, b, c\}$  with the topology  $\tau_8 = \{\phi, X, \{a, b\}\}$ and partial order  $\leq_1 = \{(a, a), (b, b), (c, c), (a, b), (a, c), (b, c)\}$ . Then,  $(X, \tau_8, \leq_1)$  is a topological ordered space. Semiclosed sets in this space are  $\phi$ , X, {c}.Sg-closed sets are  $\phi$ , X, {c}, {b, c}, {a, c} and decreasing sets are  $\phi$ , X, {a}, {a, b}. Then, sgd-closed sets are  $\phi$ , X. Clearly, every sgd-closed set in X is a semi-closed set. So, the space  $(X, \tau_8, \leq_1)$  is a semisgd  $T_{1/2}$

space. The subset {b, c} is a sg-closed set but not a semi-closed set. Hence, the space  $(X, \tau_{8} \leq 1)$  is not a semi- $T_{1/2}$  space.

# C. Theorem 4.3

Every  $semi - T_{1/2}$  space is a  $semi - sgb T_{1/2}$  space but not conversely.

- 1) Proof: Let  $(X, \tau, \leq)$  be a  $semi T_{1/2}$  space and A be a sgb-closed set in X. Then, A is a sg-closed set. Since, X is a  $semi T_{1/2}$  space, A is a semi-closed set. Therefore, every sgb-closed set in X is a semi-closed set. Hence, the space  $(X, \tau, \leq)$  is a  $semi \frac{1}{sgb} T_{1/2}$  space.
- 2) The converse is not true as shown in the following example.: Consider the set X = {a, b, c} with the topology τ<sub>8</sub> = {φ, X, {a, b}} and partial order ≤<sub>1 =</sub> {(a, a), (b, b), (c, c), (a, b), (a, c), (b, c)}. Then, (X, τ<sub>8</sub>, ≤<sub>1</sub>) is a topological ordered space. Semi-closed sets in this space are φ, X, {c}. Balanced sets are φ, X and sg-closed sets are φ, X, {c}, {b, c}, {a, c}. Then, sgb-closed sets are φ, X. Clearly, every sgb-closed set in X is a semi-closed set.So, the space (X, τ<sub>8</sub>, ≤<sub>1</sub>) is a semi-sgb T<sub>1/2</sub> space. On

the other hand, the subset {b, c} is a sg-closed set but not a semi-closed set. Hence, the space  $(X, \tau_8, \leq_1)$  is not a semi- $T_{1/2}$ .



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space. The following Figure 1 indicates the relationships between the spaces discussed above. Here, A  $\longrightarrow$  B indicates A implies B but not conversely.





## V. RELATIONSHIPS BETWEEN SEMI-T<sub>1/2</sub> TYPE SPACES

In this section we establish relationships between  $semi - T_{1/2}$  spaces defined by sgi-closed, sgd-closed and sgbclosed sets. We also establish independency of some of these spaces.

## A. Theorem 5.1

Every  $semi - sgi T_{1/2}$  space is a  $semi - sgb T_{1/2}$  space but not conversely.

- 1) Proof: Let  $(X, \tau, \le)$  be a  $semi \frac{T_{1/2}}{sgi}$  space and A be a sgb-closed set in X. So, A is a sgi-closed set. Since X is a  $semi \frac{T_{1/2}}{sgi}$  space, A is a semi-closed set. Hence, the space  $(X, \tau, \le)$  is a  $semi \frac{T_{1/2}}{sgb}$  space.
- 2) The following example shows that the converse is not true.: Consider the set  $X = \{a, b, c\}$  together with the topology  $\tau_8 = \{\phi, X, \{a, b\}\}$  and partial order  $\leq_1 = \{(a, a), (b, b), (c, c), (a, b), (a, c), (b, c)\}$ . Then,  $(X, \tau_8, \leq_1)$  is a topological ordered space. Semi-closed sets in this space are  $\phi$ , X,  $\{c\}$ . Increasing sets in this space are  $\phi$ , X,  $\{c\}$ ,  $\{b, c\}$ , and sg-closed sets are  $\phi$ , X,  $\{c\}$ ,  $\{b, c\}$ ,  $\{a, c\}$ . Then, sgi-closed sets are  $\phi$ , X,  $\{c\}$ ,  $\{b, c\}$ . Balanced sets in this space are  $\phi$ , X. So, sgb-closed sets are  $\phi$ , X. Thus, every sgb-closed set in X is a semi-closed set. Hence, the space  $(X, \tau_8, \leq_1)$  is a *semi*  $-\frac{sgb}{1/2}T_{1/2}$  space. Clearly, the

subset {b, c} is a sgi-closed set but not a semi-closed set. So, the space  $(X, \tau_8 \leq 1)$  is not a  $semi - sgi T_{1/2}$  space.

## B. Theorem 5.2

Every  $semi - sgd T_{1/2}$  space is a  $semi - sgb T_{1/2}$  space but not conversely.

1) Proof: Let  $(X, \tau, \le)$  be a  $semi - \frac{T_{1/2}}{sgd} T_{1/2}$  space and A be a sgb-closed set. So, A is a sgd-closed set. Since X is a  $semi - \frac{T_{1/2}}{sgd} T_{1/2}$  space, A is a semi-closed set. Hence, the space  $(X, \tau, \le)$  is a  $semi - \frac{T_{1/2}}{sgb} T_{1/2}$  space.

2) The following example shows that the converse is not true.: Consider the set X = {a, b, c} together with the topology τ<sub>8</sub> = {φ, X, {a, b}} and partial order ≤<sub>2</sub> = {(a, a), (b, b), (c, c), (a, b), (c, b)}. Then, (X, τ<sub>8</sub>, ≤<sub>2</sub>) is a topological ordered space. Semi-closed sets in this space are φ, X, {c}. Decreasing sets in this space are φ, X, {a}, {c}, {a, c} and balanced sets are φ, X. Also, sg-closed sets with respect to the topology τ<sub>8</sub> are φ, X, {c}, {b, c}, {a, c}. Then, sgd-closed sets are φ, X, {c}, {a, c}. The sgb-closed sets are φ, X. Clearly, every sgb-closed set in X is a semi-closed set. So, the space (X, τ<sub>8</sub>, ≤<sub>2</sub>) is a *semi-sgb* T<sub>1/2</sub>



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space. The subset {a, c} is a sgd-closed set but not a semi-closed set. So, the space (X,  $\tau_8$ ,  $\leq_2$ ) is not a semi-sgd  $T_{1/2}$ 

space.

C. Theorem 5.3 The notions  $semi - \frac{T_{1/2}}{sgi} = \frac{T_{1/2}}{1/2}$  and  $semi - \frac{T_{1/2}}{sgd} = \frac{T_{1/2}}{1/2}$  are independent.

<u>1)</u> Proof: To prove the independency it is enough to exhibit an example of a  $semi - sgiT_{1/2}$  space which is not a

 $semi - sgd T_{1/2}$  space and a space which is a  $semi - sgd T_{1/2}$  space but not a  $semi - sgi T_{1/2}$  space.

For the first part, consider the set  $X = \{a, b, c\}$  with the topology  $\tau_8 = \{\phi, X, \{a, b\}\}$  and partial order  $\leq_4 = \{(a, a), (b, b), (c, c), (a, b), (c, a), (c, b)\}$ . Then,  $(X, \tau_8, \leq_4)$  is a topological ordered space. Semi-closed sets in this space are  $\phi$ , X,  $\{c\}$ . Increasing sets are  $\phi$ , X,  $\{b\}$ ,  $\{a, b\}$  and decreasing sets are  $\phi$ , X,  $\{c\}$ ,  $\{a, c\}$ . The sg-closed sets are  $\phi$ , X,  $\{c\}$ ,  $\{a, c\}$ . Then, sgd-closed sets are  $\phi$ , X,  $\{c\}$ ,  $\{a, c\}$  and sgi-closed sets are  $\phi$ , X. (c),  $\{a, c\}$ . Then, sgd-closed sets are  $\phi$ , X.  $\{c\}$ ,  $\{a, c\}$  and sgi-closed sets are  $\phi$ , X. Clearly, every sgi-closed set in X is a semi-closed set. So, the space  $(X, \tau_8, \leq_4)$  is a semi  $-sgi T_{1/2}$  space. The subset  $\{a, c\}$  is a sgd-closed set but not a semi-closed set. So, the space  $(X, \tau_8, \leq_4)$  is not a semi  $-sgi T_{1/2}$  space.

For the other part, consider the set  $X = \{a, b, c\}$  with the topology  $\tau_8 = \{\phi, X, \{a, b\}\}$  and partial order  $\leq_1 = \{(a, a), (b, b), (c, c), (a, b), (a, c), (b, c)\}$ . Then,  $(X, \tau_8, \leq_1)$  is a topological ordered space. Semi-closed sets in this space are  $\phi$ , X,  $\{c\}$ . Increasing sets are  $\phi$ , X,  $\{c\}$ ,  $\{b, c\}$  and sg-closed sets are  $\phi$ , X,  $\{c\}$ ,  $\{b, c\}$ , and sg-closed sets are  $\phi$ , X,  $\{c\}$ ,  $\{b, c\}$ , and sg-closed sets are  $\phi$ , X,  $\{c\}$ ,  $\{b, c\}$ ,  $\{c\}$ ,

 $\tau_{8}, \leq_{1}$ ) is not a semi-sgi  $T_{1/2}$  space.

he following figure 2 indicates the relationships between the spaces discussed above. Here,  $A \longrightarrow B$  (A B) indicates



Fig. 2



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#### VI. SOME MORE NEW SPACES

In this section we introduce some more new topological ordered spaces using semi-closed sets, increasing, decreasing and balanced closed sets.

We introduce the following definitions.

## A. Definition 6.1: [8

- A topological ordered space  $(X, \tau, \leq)$  is called
- 1) a semi- $_{sgi}T_{is,1/2}$  space if every sgi-closed set is i-semi-closed.
- 2) a semi- $_{sgd} T_{ds,1/2}$  space if every sgd-closed set is d-semi-closed.
- 3) a semi- $_{sgb}T_{bs,1/2}$  space if every sgb-closed set is b-semi-closed.

#### B. Example 6.2

Let  $X = \{a, b, c\}$  with the topology  $\tau_1 = \{\phi, X, \{a\}, \{b\}, \{a, b\}\}$  and partial order  $\leq_1 = \{(a, a), (b, b), (c, c), (a, b), (a, c), (b, c)\}$ . Then,  $(X, \tau_1, \leq_1)$  is a topological ordered space. Increasing sets in this space are  $\phi$ , X,  $\{b, c\}, \{c\}$  and semi-closed sets are  $\phi$ , X,  $\{a\}, \{b\}, \{c\}, \{b, c\}, \{a, c\}$ . Then, i-semi-closed sets are  $\phi$ , X,  $\{b, c\}, \{c\}$ . Also, sg-closed sets are  $\phi$ , X,  $\{a\}, \{b\}, \{c\}, \{b, c\}, \{c\}, \{b, c\}, \{c\}, \{b, c\}, \{a, c\}$ . Then, sgi-closed sets are  $\phi$ , X,  $\{b, c\}, \{c\}$ . Clearly, every sgi-closed set is an i-semi-closed set. So, the space  $(X, \tau_1, \leq_1)$  is a semi-sgi  $T_{is,1/2}$  space.

#### C. Example 6.3

Consider the set  $X = \{a, b, c\}$  with the topology  $\tau_1 = \{\phi, X, \{a\}, \{b\}, \{a, b\}\}$  and partial order  $\leq_2 = \{(a, a), (b, b), (c, c), (a, b), (c, b)\}$ . Then,  $(X, \tau_1, \leq_2)$  is a topological ordered space. Decreasing sets in this space are  $\phi$ ,  $X, \{a, c\}, \{c\}, \{a\}$  and semi-closed sets are  $\phi, X, \{a\}, \{b\}, \{c\}, \{b, c\}, \{a, c\}$ . Also, d-semi-closed sets in this space are  $\phi, X, \{a, c\}, \{c\}, \{a\}$  and sg-closed sets are  $\phi, X, \{a\}, \{b\}, \{c\}, \{b, c\}, \{a, c\}$ . Then, sgd-closed sets are  $\phi, X, \{a, c\}, \{c\}, \{a, c\}, \{c\}, \{a\}$  and sg-closed sets are  $\phi, X, \{a\}, \{b\}, \{c\}, \{b, c\}, \{a, c\}$ . Then, sgd-closed sets are  $\phi, X, \{a, c\}, \{c\}, \{a\}$ . Clearly, every sgd-closed set in this space is a d-semi-closed set. So, the space  $(X, \tau_1, \leq_2)$  is a semi  $- \frac{T}{sgd} \frac{T}{ds, 1/2}$  space.

## D. Example 6.4

Let X = {a, b, c} with the topology  $\tau_1 = \{\phi, X, \{a\}, \{b\}, \{a, b\}\}$  and partial order  $\leq_3 = \{(a, a), (b, b), (c, c), (a, b), (a, c)\}$ . Then, (X,  $\tau_1, \leq_3$ ) is a topological ordered space. Balanced sets in this space are  $\phi$ , X and semi-closed sets are  $\phi$ , X, {a}, {b}, {c}, {b, c}, {a, c}. Also, b-semi-closed sets in this space are  $\phi$ , X. Sg-closed sets are  $\phi$ , X, {a}, {b}, {c}, {a, c}. Then, sgb-closed sets are  $\phi$ , X. Clearly, every sgb-closed set in X is a b-semi-closed set. So, the space (X,  $\tau_1, \leq_3$ ) is a semi-spheric space.

#### E. Theorem 6.5

Every  $semi - sgi T_{is,1/2}$  space is a  $semi - sgi T_{1/2}$  space.

1) Proof: Let  $(X, \tau, \leq)$  be a semi- $sgi T_{is,1/2}$  space and A be a sgi-closed set. Since X is a semi- $sgi T_{is,1/2}$  space, the set

A is an i-semi-closed set. So, A is a semi-closed set. Therefore, every sgi-closed set in X is a semi-closed set. Hence, the space  $(X, \tau, \leq)$  is a  $semi-sgi T_{1/2}$  space.

## F. Theorem 6.6

Every semi- $_{sgd} T_{ds,1/2}$  space is a semi- $_{sgd} T_{1/2}$  space.



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1) Proof: Let  $(X, \tau, \leq)$  be a semi-sgd T ds, 1/2 space and A be a sgd-closed set in X. Since X is a

 $semi - sgd T_{ds,1/2}$  space, A is a d-semi-closed set. So, A is a semi-closed set. Therefore, every sgd-closed set in X is a semi-closed set. Hence, the space (X,  $\tau$ ,  $\leq$ ) is a  $semi - sgd T_{1/2}$  space.

G. Theorem 6.7

Every  $semi - sgb T_{bs,1/2}$  space is a  $semi - sgb T_{1/2}$  space.

1) Proof: Let  $(X, \tau, \leq)$  be a semi- $_{sgb}T_{bs,1/2}$  space and A be a sgb-closed set in X. Since X is a semi- $_{sgb}T_{bs,1/2}$ 

space, A is a b-semi-closed set. So, A is a semi-closed set. Therefore, every sgb-closed set in X is a semi-closed set. Hence, the space  $(X, \tau, \leq)$  is a semi- $_{seb} T_{1/2}$  space.

#### VII. CONCLUSION

In this paper we introduced new types of Semi- $T_{1/2}$  spaces using sg-closed type sets. We studied relationships between these spaces. We also established the independency of some of these topological ordered spaces.

#### REFERENCES

- [1] L. Nachbin, Topology and order, D. Van Nostrand Inc., Princeton, New Jerse (1965
- [2] M.K.R.S. Veera Kumar, Homeomorphisms in topological ordered spaces, Acta Ciencia Indica, XXVIII (M) (1)(2002), 67-76.
- [3] M.K.R.S. Veera Kumar, Between closed sets and g-closed sets, Mem. Fac. Sci. Koch Univ. Ser. A, Math., 21(2000), 1-19
- [4] N. Levine, Semi-open sets and semi-continuity in topological spaces, Amer. Mat Monthly, 70(1963), 36-41
- [5] N. Levine, Generalized closed sets in topology, Rend. Circ. Math. Palermo 19(2) (1970), 89-96
- [6] P. Bhattacharya and B.K. Lahiri, Semi-generalized closed sets in topology, Indian J. Math., 29(3) (1987), 375-38
- [7] V.V.S. Ramachnadram, B. Sankara Rao and M.K.R.S. Veera Kumar g-closed type, g\*-closed type and sg-closed type sets in topological order spaces, Diophantus J. Math., 4(1) (2015), 1-
- [8] V.V.S. Ramachandram, B. Sankara Rao and M.K.R.S. Veera Kumar, On som Applications of g\*-closed, g-closed and sg-closed type sets in topologica ordered spaces, Galois J., Math., 2(1) (2015),1-8
- [9] V.V.S. Ramachandram, B. Sankara Rao and M.K.R.S. Veera Kumar, some relationshipsof g-closed, g\*-closed and sg-closed type sets with *other closed type sets in topologic ordered spaces*, International J., Math. and Nature., 1(1) (2015),1-9.











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