



# IJRASET

International Journal For Research in  
Applied Science and Engineering Technology



# INTERNATIONAL JOURNAL FOR RESEARCH

IN APPLIED SCIENCE & ENGINEERING TECHNOLOGY

**Volume:** 11    **Issue:** III    **Month of publication:** March 2023

**DOI:** <https://doi.org/10.22214/ijraset.2023.49699>

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# A Study on Root Cube Even Mean Labeling for Some Special Graphs

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**Abstract:** A graph  $G = (V,E)$  with  $p$  vertices and  $q$  edges is said to be a Root Cube Even Mean Graph if it is possible to label the vertices  $x \in V$  with distinct elements  $f(x)$  from  $1, 2, \dots, q+1$  in such a way that when each edge  $e = uv$  is labeled with  $f(e = uv)$

$$= \left\lfloor \sqrt{\frac{f(u)^2 + f(v)^2}{2}} \right\rfloor \text{ or } \left\lceil \sqrt{\frac{f(u)^2 + f(v)^2}{2}} \right\rceil, \text{ then the resulting edge labels are distinct. Here } f \text{ is called a Root Cube Even}$$

Mean Labeling of  $G$ . In this paper we prove that Quadrilateral snake, Triangular Snake,  $P_n \odot K_{1,3}$ , Star is a root cube even mean labeling.

**Key Words:** Labeling, Root Mean Square Graph, Graceful graph

## I. INTRODUCTION

All Graphs in this paper are finite and undirected. The symbols  $V(G)$  and  $E(G)$  denote the vertex set and edge set of a graph  $G$ . The cardinality of the vertex set is called the order of  $G$  denoted by  $p$ . The cardinality of the edge set is called the size of  $G$  denoted by  $q$  edges is called a  $(p,q)$  graph. A graph labeling is an assignment of integers to the vertices or edges. Bloom and Hsu [2] extended the notion of graceful labeling to directed graphs. Further this work can be extended in the field of automata theory [6,7,8,9,10,11] which has a wide range of application in automata theory. There are many applications in graph labeling under undirected [16,17,18,19,20,21] and directed graph[12,13,14,15]

## II. BASIC DEFINITIONS

A. Definition 2.1

The graph  $P_n \odot K_{1,3}$  is obtained by attaching complete bipartite graph  $K_{1,3}$  to each vertex of path  $P_n$ .

B. Definition 2.2

The graph is called a Quadrilateral Snake graph which is defined as series connection of non-adjacent vertices of  $N$  number of cycle.

C. Definition 2.3

A triangular  $T_n$  is obtained from a path  $u_1, u_2, u_3, \dots, u_n$  and  $v_1, v_2, v_3, \dots, v_n$ . That is every edge of a path.

## III. MAIN RESULTS

A. Theorem 3.1

$P_n \odot K_{1,3}$  is a Root Cube Even Mean Labeling Graph.

Proof

Let  $P_n \odot K_{1,3}$  with vertices as  $v_1, v_2, \dots, v_n$ ;  $w_1, w_2, \dots, w_n$ ;  $u_1, u_2, \dots, u_n$  and  $x_1, x_2, \dots, x_n$

Define a function  $f: V(G) \rightarrow \{2, 4, 6, 8, \dots, 8n\}$

$$f(v_i) = 8i - 6, 1 \leq i \leq n$$

$$f(w_i) = 8i - 4, 1 \leq i \leq n$$

$$f(v_i) = 8i - 2, 1 \leq i \leq n$$

$$f(u_i) = 8i, 1 \leq i \leq n$$

The edge of the graph  $P_n \odot K_{1,3}$  receive distinct numbers .  
Hence  $P_n \odot K_{1,3}$  is root cube even mean labeling graph.

Example 3.1

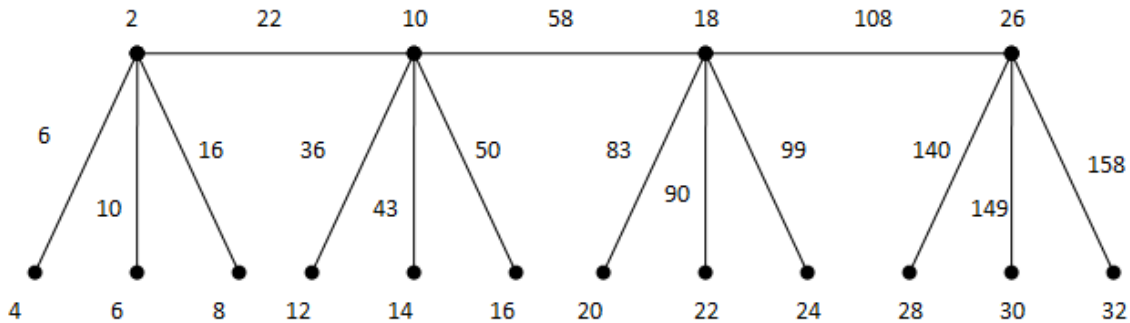


Figure: 3.1  $P_n \odot K_{1,3}$

**B. Theorem:3.2**

The Star  $K_{1,n}$  is a Root Cube Even Mean Labeling Graph

Proof

Let  $G$  be a graph  $k_{1,n}$

Let  $k_{1,n}$  be a star with vertices as  $v_1, v_2, \dots, v_n$

Define  $f: V(G) \rightarrow \{2, 4, 6, 8, \dots, 2n+1\}$

$$f(v) = 2i + 2; 1 \leq i \leq n$$

Then the edge labels as  $2i + 1; 1 \leq i \leq n$

Therefore, the edge of the star graph receive distinct numbers

Hence, the star  $K_{1,n}$  is a root cube even mean labeling

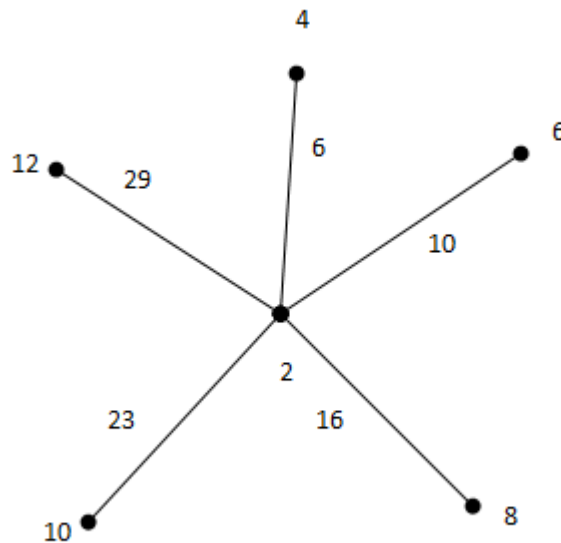


Figure:3.2 Star  $k_{1,n}$

**C. Theorem: 3.3**

$Q_3$  is a root cube even mean labeling graph

**Proof**

Let  $Q_3$  is a graph

Let  $Q_3$  with vertices  $v_1, v_2, \dots, v_n ; w_1, w_2, \dots, w_n ; u_1, u_2, \dots, u_n$  and  $x_1, x_2, \dots, x_n$

Define a function  $f:V(G) \rightarrow \{2,4,6,\dots,n\}$

$$f(u_i) = 6i - 2$$

$$f(v_i) = 6i - 4$$

$$f(w_i) = 6i$$

Then the edge labels are distinct.

Therefore,  $Q_3$  is said to be a root cube even mean labeling of graph.

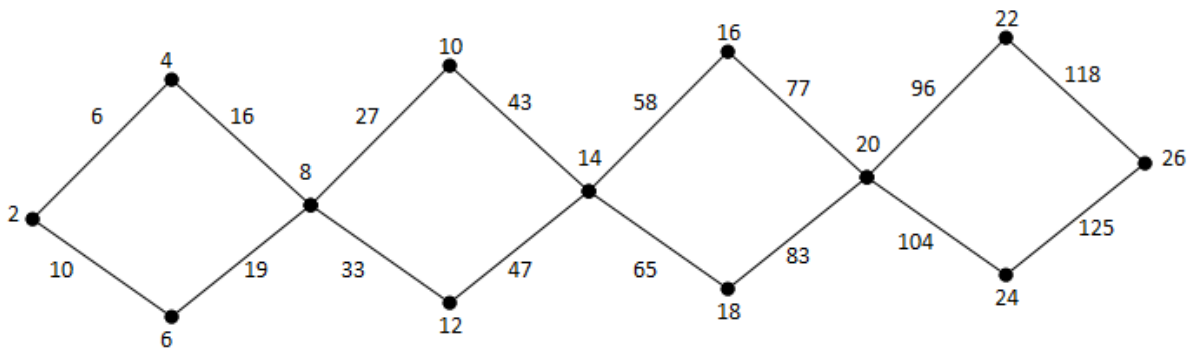


Figure:3.3 Quadrilateral snake

**D. Theorem :3.4**

$T_4$  is a root cube even mean labeling of graph

**Proof**

Let  $T_4$  be a triangular snake

Let  $T_4$  with vertices  $v_1, v_2, \dots, v_n ; w_1, w_2, \dots, w_n ; u_1, u_2, \dots, u_n$  and  $x_1, x_2, \dots, x_n$

Define a function  $f:V(G) \rightarrow \{2,4,6,\dots,n\}$

$$f(u_i) = 2i - 2$$

$$f(v_i) = 2i$$

Then the edge labels are distinct.

Therefore,  $T_n$  is said to be a root cube even mean labeling of graph.

**Example: 3.4**

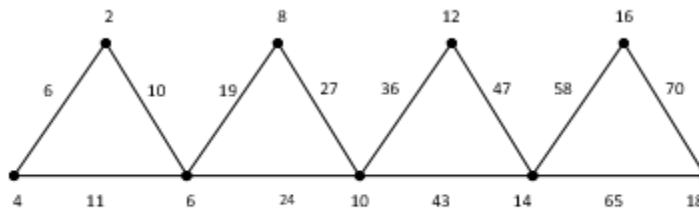


Figure 3.4 Triangular Snake

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