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Performance Optimization of Combined Gas and Steam Power Plant using Matrix Laboratory (MATLAB)

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Abstract: *The ever increasing demands for higher thermal efficiency from power plants have resulted to wide range of research in this regard. This work is one of such researches that deal with the performance optimization of a COGAS plant using MATLAB. A mathematical model of the COGAS plant was developed based on thermodynamic analyses and energy balance equations. This was used to develop a program and run in MATLAB environment for analysis and Optimization of the COGAS thermal efficiency.*

Results show that the program simulation yielded an overall maximum operational thermal efficiency of 69.7% at about 1750K, considering metallurgical limits of the topping cycle turbine components. The resulting model could predict the optimized performance output of the system with high degree of accuracy and reliability. The novelty of this research is essentially in its methodology and will remain invaluable in future works that will focus towards improving the thermal efficiency of power plants.

Keywords: *Gas turbine, Steam turbine, Optimization, Efficiency, MATLAB*

I. INTRODUCTION

A gas turbine (GT) is an internal combustion engine that uses the gaseous energy of air to convert chemical energy of fuel into mechanical energy. The steam turbine is a device that extracts thermal energy from pressurized steam and uses it to produce mechanical work. Bringing together these two systems thermodynamically to function as a single system is termed "cogeneration" which means generation of both work (shaft power) and heat (steam) simultaneously.

Cogeneration systems can work with high capacity and high efficiency nearly all year. Cogeneration systems save 30 % more energy than conventional energy systems [1].

Thermodynamically, when two thermal cycles are combined in a single power plant the efficiency that can be achieved is higher than that of one cycle alone and energy is conserved [2]. The exhaust temperature of GT can be within the range of about 500-600°C [3]. Combination of cycles with different working media is quite interesting because their advantages can complement one another. Normally, when two cycles are combined, the cycle operating at the higher temperature level is called the "topping cycle". The waste heat it produces is then used in a second process that operates at a lower temperature level and is therefore called the "bottoming cycle" [4]. It thus makes engineering sense to take advantage of the very desirable characteristics of the gas-turbine cycle at high temperatures and to use the high-temperature exhaust gases as the energy source for the steam power cycle [5]. The combination most widely accepted for commercial power generation and marine propulsion application is that of a gas topping cycle with a steam bottoming cycle [6].

Along with its wide and successful application in land-based power plants, the combined gas and steam turbines (COGAS) concept is being extended to provide an alternative form of power plant for ships [7]. COGAS should not be confused with combined steam and gas power plants, which employ oil-fired boilers for steam turbine propulsion during normal cruising and the gas turbines are supplemented for high speed and faster response/reaction times. COGAS plant uses heat from the exhaust gas of the gas turbine to heat water through a series of tubes in a heat exchanger under high pressure to become superheated steam. In this plant, the network done is a combination of the work done in the gas and steam turbines all from only one source of heat supply [5]. Flexibility provided by these systems satisfies utility power- generations, industrial-cogeneration and ship propulsion applications where the efficiency of these systems can exceed 60% [8]. Modeling and simulation of combined cycles has always been a powerful tool for their performance optimization. However, the need to develop accurate and reliable models of COGAS for different objectives and

applications has been a strong motivation for researchers to continue to work in this fascinating area [9]. MATLAB has shown a high and strong potential to be considered as a reliable alternative to the conventional modeling approaches, simulation and optimization methodologies due to their independence and adaptability. This work will deal with novel methodology for performance optimization of a COGAS plant using MATLAB.

II. METHODOLOGY

The performance optimization of the units that make up the entire system of this COGAS plant with technical parameters shown below in Fig. 1, are implemented utilizing the approach stated below: modeling the COGAS plant, writing a program to implement the modeling in MATLAB and to use the obtained operational data from a COGAS plant for performance optimization of the COGAS plant. The technical details of the COGAS system used for this research are shown in Appendix A.

A. Analytical Model of the COGAS System

For the purpose of this research, fig. 1 shows the schematic diagram of the COGAS plant used for the modeling. The modeling were carried out in segment for mathematical convenience and simplification starting with the gas turbine modeling, then steam turbine modeling and finally the combined cycle following the nomenclature of the schematic diagrams of each power plant.

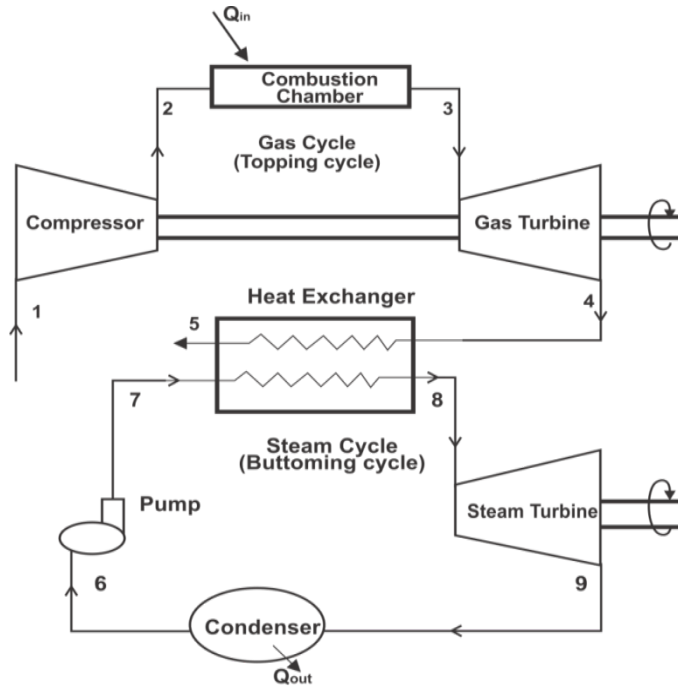


Fig. 1 A schematic diagram of a COGAS plant [10]

B. Modeling the Gas Turbine

In the GT cycle (topping cycle) as shown in fig 1, the air is compressed isentropically in the compressor from state 1 to 2 where its temperature rises from T_1 to T_2 . The compressed air then enters the combustion chamber where the combustion of fuel takes place isobarically. This results in rise of temperature of combustion product from T_2 to T_3 . The high temperature gases enter the turbine where it expands to the final temperature T_4 . According to Ogbonnaya [5], [11] the work done in the compressor is given by:

$$W_{gc} = m_a C_{p_a} (T_2 - T_1) \tag{1}$$

$$= m C_p T_1 \left(\frac{T_2}{T_1} - 1 \right) \tag{2}$$

But the pressure ratio is given by the expression below;

$$\frac{T_2}{T_1} = P_r^{\left(\frac{\gamma-1}{\gamma} \right)} \tag{3}$$

Considering the pressure ratio of the turbine, equation (1) becomes

$$W_{gc} = m_a C_p T_1 \left(P_r^{\left(\frac{\gamma-1}{\gamma}\right)} - 1 \right) \tag{4}$$

The expression for the work done, W_{gt} by the turbine is:

$$W_{gt} = m_a C_p (T_3 - T_4) \tag{5}$$

Similarly;

$$T_3 = T_4 P_r^{\left(\frac{\gamma-1}{\gamma}\right)} \tag{6}$$

From equation (2.6), the turbine outlet temperature is given by;

$$\frac{T_3}{T_4} = \left(P_r^{\left(\frac{\gamma-1}{\gamma}\right)} \right) \tag{7}$$

Substituting equation (7) into equation (5), the expression for the work done in the gas turbine is;

$$W_{gt} = m_a C_p T_4 \left(P_r^{\left(\frac{\gamma-1}{\gamma}\right)} - 1 \right) \tag{8}$$

The heat supplied, Q_{sg} to the system is obtained by the relations below:

$$Q_{sg} = m_a C_p (T_3 - T_2) \tag{9}$$

Substituting equation (3) into equation (9), the heat supply to the system is given by the expression in equation (10);

$$Q_{sg} = m_a C_p \left(T_3 - T_1 P_r^{\left(\frac{\gamma-1}{\gamma}\right)} \right) \tag{10}$$

Where:

$T_3 =$ inlet temperature to the turbine

$Q_{sg} =$ heat supplied

The network done by the topping cycle is derived from the expression below:

$$W_{net, gas} = W_{gt} - W_{gc} \tag{11}$$

According to Cengel and Boles the above, the efficiency of the gas turbine is [12]:

$$\eta_{gas, tur} = \frac{W_{net, gas}}{Q_s} \tag{12}$$

$$\eta_{gas, tur} = \frac{m_a C_p \left(T_3 - \left(\frac{T_3}{P_r^{\left(\frac{\gamma-1}{\gamma}\right)}} \right) \right) - m_a C_p T_1 \left(P_r^{\left(\frac{\gamma-1}{\gamma}\right)} - 1 \right)}{m_a C_p \left(T_3 - T_1 P_r^{\left(\frac{\gamma-1}{\gamma}\right)} \right)} \tag{13}$$

$$\eta_{gas, tur} = \frac{\left[\left(T_3 - \left(\frac{T_3}{P_r^{\left(\frac{\gamma-1}{\gamma}\right)}} \right) \right) - T_1 \left(P_r^{\left(\frac{\gamma-1}{\gamma}\right)} - 1 \right) \right]}{\left(T_3 - T_1 P_r^{\left(\frac{\gamma-1}{\gamma}\right)} \right)} \tag{14}$$

C. Modeling the Steam cycle (Bottoming Cycle)

In the steam cycle, feed water flows through the heat exchanger where it absorbs heat from the exhaust gas of the GT cycle and in this way the temperature of the air rises [13]. The high pressure and high temperature steam leaving the heat exchanger enters the turbine where it expands to the final state as shown in fig. 2. Therefore the expression for energy balance in the heat exchanger is given by:

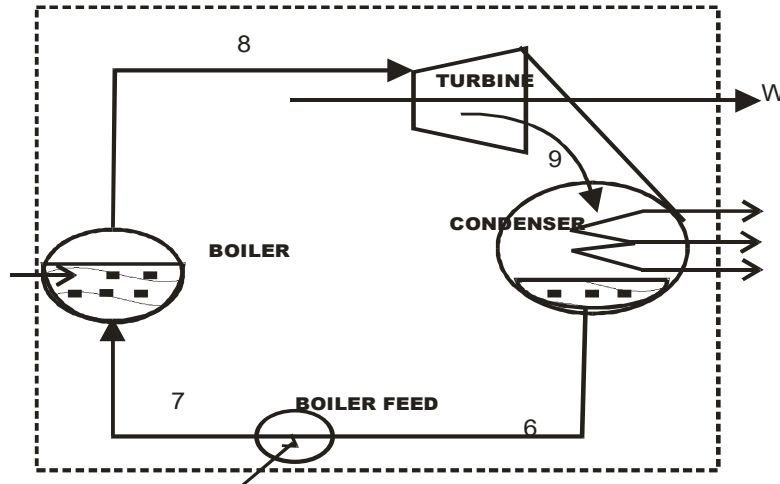


Fig. 2 A schematics diagram of a steam turbine [10]

The energy balance in the heat exchanger is expressed by equation 15

$$m_a C_p (T_4 - T_5) = m_s (h_8 - h_7) \tag{15}$$

According to Ogbonnaya (2004), the work done by the steam turbine is;

$$W_{st} = m_s (h_8 - h_9) \tag{16}$$

The work done by the pump is given by:

$$w_p = v_f (P_7 - P_6) \times 100 \tag{17}$$

Therefore, the net work done by the steam turbine is given by the expression:

$$W_{net,steam} = W_{st} - w_p \tag{18}$$

$$W_{net,steam} = m_s (h_8 - h_9) - v_f (P_7 - P_6) \tag{19}$$

Equation (2.18) can be written as;

$$W_{net,steam} = m_s (h_8 - h_9) - m_s (h_7 - h_6) \tag{20}$$

The heat supplied to the system can be obtained from the expression below:

$$Q_{ss} = m_s (h_8 - h_7) \tag{21}$$

Therefore, the steam cycle efficiency will be given by;

$$\eta_{st} = \frac{m_s [(h_8 - h_9) - (h_7 - h_6)]}{m_s (h_8 - h_7)} \tag{22}$$

From Cengel and Boles [12] and Shalan et al [9], the net efficiency of the combined cycle can be obtained from the expression:

$$\eta_{combined} = \frac{(W_{net,gas} + W_{net,steam})}{Q_{ss}} \tag{23}$$

$$\eta_{combined} = \frac{\left[m_a C_p \left(T_3 - \left(\frac{T_2}{P_r^{(\frac{\gamma-1}{\gamma})}} \right) \right) - T_1 \left(P_r^{(\frac{\gamma-1}{\gamma})} - 1 \right) + m_s [(h_8 - h_9) - (h_7 - h_6)] \right]}{m_a C_p \left(T_3 - T_1 P_r^{(\frac{\gamma-1}{\gamma})} \right)} \tag{24}$$

D. Computer Model and Programming of the COGAS System

MATLAB (R2016a) programming language was used to write script files for analyzing the various parameters and for optimizing the COGAS thermal efficiency using technical data collected from COGAS plant for ship propulsion. To obtain a maximally optimized and to ensure good generalization characteristic of the COGAS model, a comprehensive computer code was generated and run in MATLAB. Table 1 and Fig. 3 show the input parameters for the COGAS optimization and flow chart developed for the program to optimize the thermal efficiency of the COGAS system respectively.

Table 1
Input Parameters for COGAS Optimization

Parameters	Symbol	Unit	Operational Range
GT compressor inlet temperature	T_1	K	[273.15; 328.15]
GT compressor inlet pressure	P_1	bar	[1.01325; 21.0325]
GT pressure ratio	P_r	-	[11.5; 20.8]
GT inlet temperature to the turbine	T_3	K	[1650; 1850]
GT air mass flow Rate	m_a	Kg/sec	[67.9268; 77.9268]
GT fuel mass flow rate	m_g	Kg/sec	[0.00367; 0.2661]
ST steam mass flow rate	m_s	Kg/sec	[0.79; 60.75]
ST enthalpy before entering the pump	h_6	KJ/kg	[174.0; 194.0]
ST enthalpy after the pump	h_7	kJ/kg	[182.06; 202.0]
ST enthalpy after the boiler	h_8	kJ/kg	[3398.0; 3599.0]
ST enthalpy after the turbine	h_9	kJ/kg	[2102.8; 2302.8]
ST inlet temperature	T_5	K	[500.0; 550.0]
ST boiler pressure	P_5	Bar	[80.0; 100.0]
Specific heat capacity of air	C_p	kJ/kgk	[1.005; 1.010]
Ratio of specific heat	γ	-	[1.33; 1.44]
ST Condenser pressure	P_6	Bar	[0.08; 0.10]

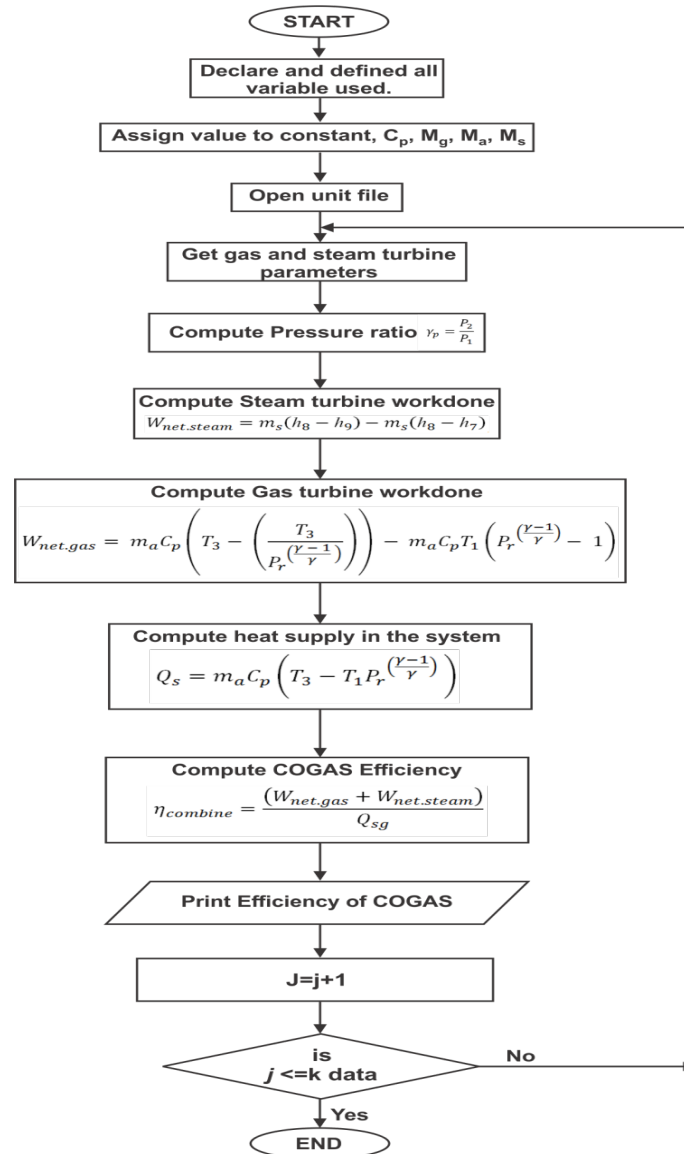


Fig. 3 A Flow Chart to Calculate the Efficiency of COGAS Plant

III. RESULT AND ANALYSIS

To obtain and ensure a good optimization of the COGAS model, a comprehensive code was developed and run in MATLAB. From the analysis obtained from the computer model, the following graphs were plotted to demonstrate the relationship between COGAS thermal efficiency and some selected parameters from the MATLAB program. Fig. 4 shows a graph of COGAS efficiency against the steam turbine mass flow rate. In this case, as the turbine mass flow rate increases, there is a corresponding increase in the thermal efficiency. Steam mass flow rate influence on the COGAS thermal efficiency is observed to be at a value of 0.195kg/sec, after which both parameter increases proportionately.

Fig. 5 shows a graph of compressor pressure ratio against COGAS efficiency. It was observed that, as the pressure ratio increases, the COGAS efficiency increases correspondingly. This indicates a proportional relationship between these two quantities of COGAS system. Fig. 6 shows the variation of COGAS efficiency against the gas turbine inlet temperature. The COGAS efficiency begins to show an increase at value of 0.6912 as the turbine inlet temperature increases. It shows that the rate of rise in efficiency of COGAS increases as the gas turbine inlet temperature increase. The final overall data generated in MATLAB with which ANN was trained is shown in Appendix B.

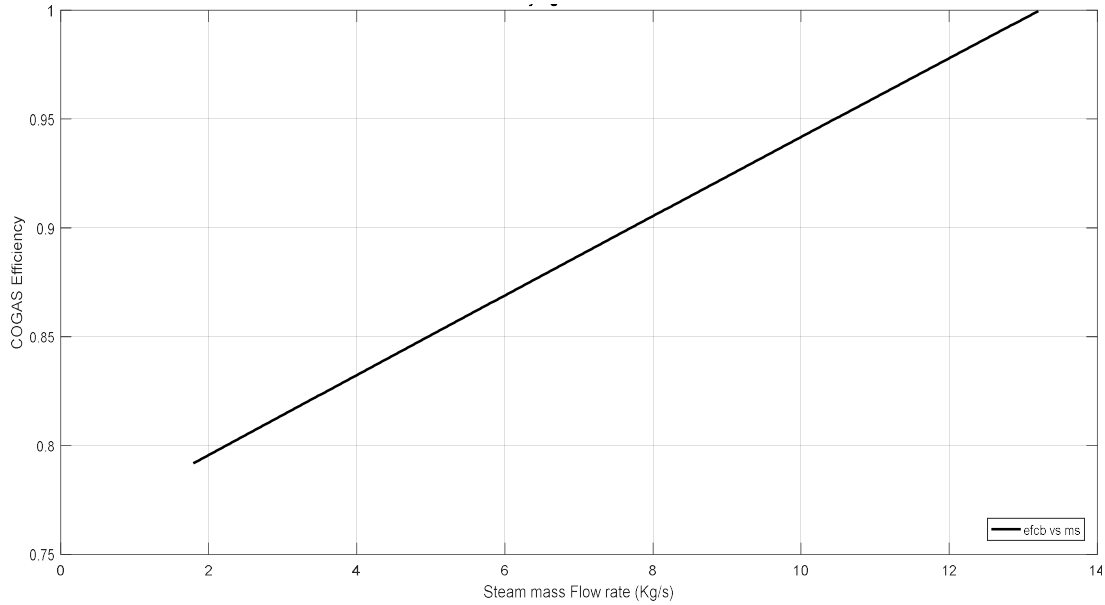


Fig. 4 COGAS efficiency against Steam mass flowrate

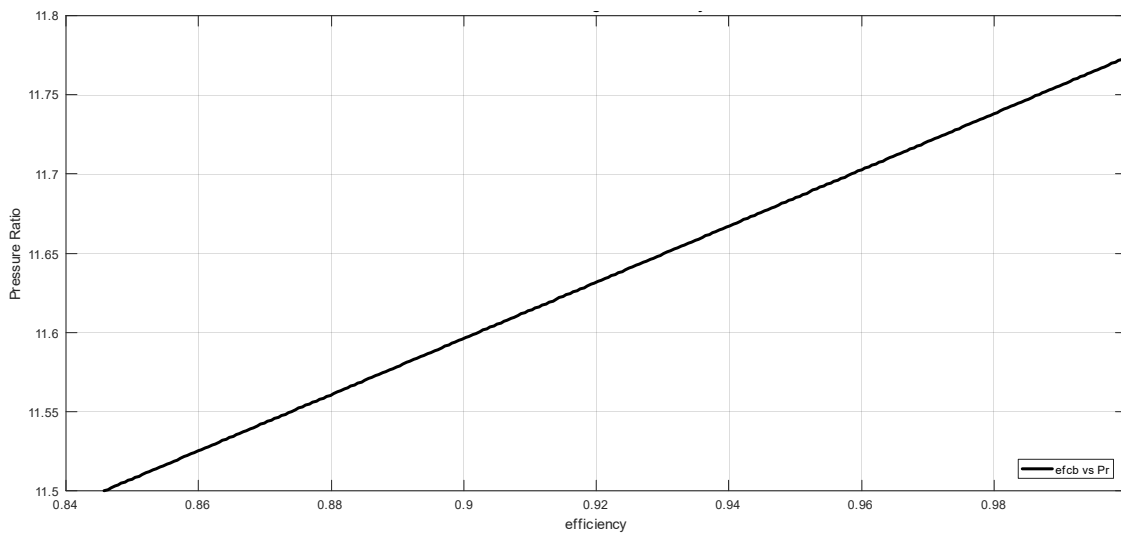


Fig. 5 Graph of Pressure Ratio against Efficiency

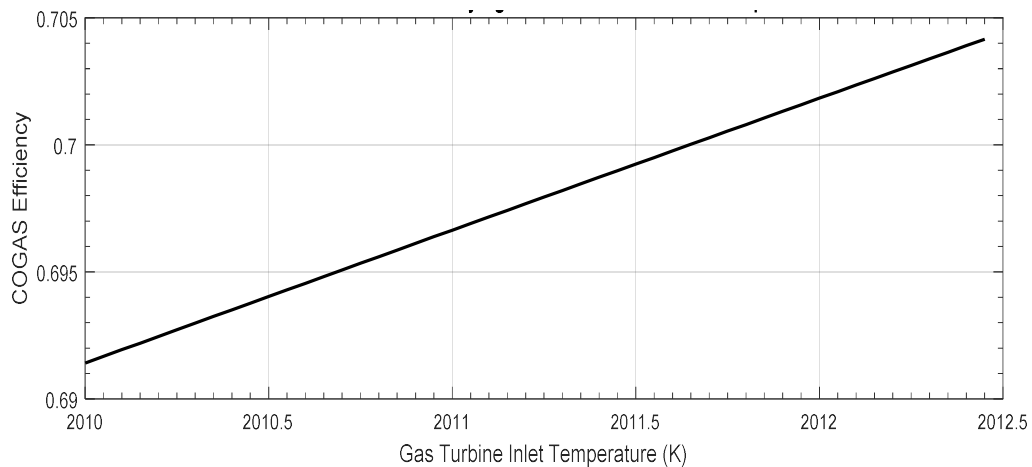


Fig. 6 COGAS efficiency against Gas turbine inlet temperature

IV. CONCLUSION

In this research work, thermodynamics and energy balance equations were employed to model the COGAS plant. A comprehensive computer program code was generated and run in MATLAB environment using the COGAS data obtained for ship propulsion. The main objective of the research was to explore and optimize the thermal efficiency of the COGAS plant using MATLAB. This analysis is vital as COGAS plant satisfactory performance depends extensively on the thermodynamic properties and efficiency of the systems. The program simulation yielded an overall maximum operational thermal efficiency of 69.7% at about 1750K, considering metallurgical limits of the topping cycle turbine components. Similarly, some COGAS parameters have a proportional relationship with the thermal efficiency of the system. The results are evident to conclude that modeling, simulation and analysis can be handled using MATLAB to produce results with a high degree of accuracy and reliability.

A. Recommendations

Based on the findings from the computer model and analysis results, recommendations are as follows:

- 1) MATLAB should be employed to maximize the optimization characteristics of COGAS systems.
- 2) MATLAB methodology should be used to predict the thermal efficiency and performance of similar COGAS systems.
- 3) Reasonable attention and consideration should be given to the thermodynamic properties of COGAS systems

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APPENDIX A

Technical Details of the COGAS Used In This Work

Gas turbine:

Manufacturer	General Electric
Model	GE9351FA
Fuel	Natural Gas
Number of shaft	1
Frequency	50Hz
Pressure ratio	15.8
Compressor inlet temperature	273.15K
Turbine inlet temperature	1950K
Exhaust temperature	872K
Power	259.5MW
Thermal Efficiency	37.3%
Heat rate	9643 KJ/Kwh
Air flow rate	802 kg/s

Steam turbine

Manufacturer	Babcock
Model	D2248B
Steam flow rate	70.74kg/s
Power	120MW
Thermal efficiency	42%
Inlet pressure	80bar
Condenser pressure	0.08bar
Inlet temperature	500°C

Calculated parameters

Steam enthalpy at state 6, h_6	174Kj/kg
Steam enthalpy at state 7, h_7	182.06 Kj/kg
Steam enthalpy at state 8, h_8	3398 Kj/kg
Steam enthalpy at state 9, h_9	2102.8 Kj/kg

APPENDIX B

COGAS generated data in MATLAB for ANN training

GT Compressor inlet Temperature(T1)	GT compressor inlet Pressure(P1)	GT pressure ratio (Pr)	GT inlet Temperature to the turbine(T3)	GT inlet Temperature to the turbine(T4)	GT fuel mass flow rate(mf)	ST steam mass flow rate(ms)	Enthalpy before entering the pump (h6)	Enthalpy after entering the pump(h7)	Enthalpy before the boiler (h8)	Enthalpy after the boiler(h9)	ST inlet temperature (T5)	ST boiler pressure(P5)
253.15	1.01325	10.5	2010	800.9268	0.00367	0.75	174	182.06	3398	2102.8	500	80
253.225	1.05326925	10.5053	2010.05	800.9318	0.00393243	0.90925	174.02	182.07994	3398.201	2103	500.05	80.02
253.3	1.0932885	10.5106	2010.1	800.9368	0.00419486	1.0685	174.04	182.09988	3398.402	2103.2	500.1	80.04
253.375	1.13330775	10.5159	2010.15	800.9418	0.00445729	1.22775	174.06	182.11982	3398.603	2103.4	500.15	80.06
253.45	1.173327	10.5212	2010.2	800.9468	0.00471972	1.387	174.08	182.13976	3398.804	2103.6	500.2	80.08
253.525	1.21334625	10.5265	2010.25	800.9518	0.00498215	1.54625	174.1	182.1597	3399.005	2103.8	500.25	80.1
253.6	1.2533655	10.5318	2010.3	800.9568	0.00524458	1.7055	174.12	182.17964	3399.206	2104	500.3	80.12
253.675	1.29338475	10.5371	2010.35	800.9618	0.00550701	1.86475	174.14	182.19958	3399.407	2104.2	500.35	80.14
253.75	1.333404	10.5424	2010.4	800.9668	0.00576944	2.024	174.16	182.21952	3399.608	2104.4	500.4	80.16
253.825	1.37342325	10.5477	2010.45	800.9718	0.00603187	2.18325	174.18	182.23946	3399.809	2104.6	500.45	80.18
253.9	1.4134425	10.553	2010.5	800.9768	0.0062943	2.3425	174.2	182.2594	3400.01	2104.8	500.5	80.2
253.975	1.45346175	10.5583	2010.55	800.9818	0.00655673	2.50175	174.22	182.27934	3400.211	2105	500.55	80.22
254.05	1.493481	10.5636	2010.6	800.9868	0.00681916	2.661	174.24	182.29928	3400.412	2105.2	500.6	80.24
254.125	1.53350025	10.5689	2010.65	800.9918	0.00708159	2.82025	174.26	182.31922	3400.613	2105.4	500.65	80.26
254.2	1.5735195	10.5742	2010.7	800.9968	0.00734402	2.9795	174.28	182.33916	3400.814	2105.6	500.7	80.28
254.275	1.61353875	10.5795	2010.75	801.0018	0.00760645	3.13875	174.3	182.3591	3401.015	2105.8	500.75	80.3
254.35	1.653558	10.5848	2010.8	801.0068	0.00786888	3.298	174.32	182.37904	3401.216	2106	500.8	80.32
254.425	1.69357725	10.5901	2010.85	801.0118	0.00813131	3.45725	174.34	182.39898	3401.417	2106.2	500.85	80.34
254.5	1.7335965	10.5954	2010.9	801.0168	0.00839374	3.6165	174.36	182.41892	3401.618	2106.4	500.9	80.36
254.575	1.77361575	10.6007	2010.95	801.0218	0.00865617	3.77575	174.38	182.43886	3401.819	2106.6	500.95	80.38
254.65	1.813635	10.606	2011	801.0268	0.0089186	3.935	174.4	182.4588	3402.02	2106.8	501	80.4
254.725	1.85365425	10.6113	2011.05	801.0318	0.00918103	4.09425	174.42	182.47874	3402.221	2107	501.05	80.42
254.8	1.8936735	10.6166	2011.1	801.0368	0.00944346	4.2535	174.44	182.49868	3402.422	2107.2	501.1	80.44
254.875	1.93369275	10.6219	2011.15	801.0418	0.00970589	4.41275	174.46	182.51862	3402.623	2107.4	501.15	80.46
254.95	1.973712	10.6272	2011.2	801.0468	0.00996832	4.572	174.48	182.53856	3402.824	2107.6	501.2	80.48
255.025	2.01373125	10.6325	2011.25	801.0518	0.01023075	4.73125	174.5	182.5585	3403.025	2107.8	501.25	80.5



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