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Efficient Memory-based Multiplier Technique for SWL DSP Systems

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Abstract: *The DSP systems usually deal with a lot of multiplications as it is dealt with many discrete signals. The combinational circuits consume a lot of power as there are many intermediate blocks (i.e., usually full adders & and gates). The combinational circuits take more area and the delay is also more. Usually there is a tradeoff between area and delay. To make the multiplier more efficient we usually prefer memory-based multiplier. Different types of techniques are there in memory-based multipliers like the APC (anti-symmetric product coding), OMS (odd multiple storage) etc. In these techniques LUT based storage is used. The multiplied products are stored efficiently based on the technique used to store the data. To optimize the memory required we combine the APC and OMS technique for better storage and retrieval of data. In this project we show how combined technique increases the performance of multiplier. The suggested combined technique reduces the size of the LUT to one-fourth that of a standard LUT. It is demonstrated that the proposed LUT architecture for tiny input sizes can be used to execute high-precision multiplication with input operand decomposition in an efficient manner.*

Keywords: Antisymmetric product coding (APC); Odd multiple storage (OMS); Digital Signal Processing (DSP); lookup- table (LUT); memory-based computing.

I. INTRODUCTION

Memory-based computing is crucial in digital signal processing (DSP) techniques that use a fixed set of coefficients for multiplication. Memory-based computing is a subset of specialized systems in which look-up tables (LUT) perform the computational activities. In comparison to multiply accumulate structures, they are closer to human computing and more regular. Antisymmetric product coding (APC), odd-multiple-storage (OMS), and the combined approach of APC and OMS known as APC-OMS are three memory-based computation techniques that can be used to optimize LUTs for memory-based multiplication. Only the odd multiples of the fixed coefficients must be stored in LUT, resulting in odd-multiple-storage (OMS). The product words are encoded as antisymmetric pairs in the antisymmetric product coding (APC) technique. The LUT size is only reduced by a factor of two with each of these strategies. In the APC-OMS technique, the LUT size is reduced to one-fourth of the conventional LUT size. The complement operations might be greatly reduced in the combined technique of APC-OMS based LUT multiplier since the input address and LUT output are always mapped into odd integers. However, it displays a significant overhead in area in APC-OMS, so a modified APC-OMS technique based LUT multiplier is proposed.

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II. MEMORY BASED COMPUTATION TECHNIQUES

A. Antisymmetric Product Coding for LUT Optimization

Table 1 shows the result words for various input X values for word length L = 5. The input word X in the third column of each row is the two's complement of that in the first column of the same row, as seen in this table. Also, the total of product values in the same row corresponding to these two input values is 32A. We'll use positive integers for X (input) and A (fixed coefficient), and u and v for the product values in the second and fourth columns of the row. The sum of u and v is 32A, as shown in the table, and u and v may be calculated using the following equation.

$$u=[u+v]/2 +[v-u]/2 \text{ and } v=[u+v]/2 \text{ and } v=[u+v]/2-[v-u]/2 \dots\dots\dots(1)$$

Substituting $(u + v) = 32A$ we get

$$u=16A+[v-u]/2 \text{ and } v=16A-[v-u]/2 \dots\dots\dots(2)$$

A negative symmetry can be shown on u and v in Equation 2. As a result of this behavior, we can cut the size of the lookup table in half by just storing $[v-u]/2$ for a pair of inputs on the same row. The APC word for $X = (00000)$ is already stored as 16A. The product word is obtained by the following equation. The technique is called an antisymmetric product code because the representation of the product is derived from the antisymmetric behavior of the products. The four-bit address $X'=(x_3', x_2', x_1', x_0')$ is accessible using the relation $X'=XL$ for $x_4=1$ and $X=X'L$ for $x_4=0$, where XL is the four-bit LSB of X and $X'L$ is the two's complement of XL .

$$\text{Product} = 16A + (\text{sign value})(\text{APC-word})$$

The most significant bit determines the sign value. When the most significant bit is 1, the sign value is 1, and when the most significant bit is 0, the sign value is -1. We use an adder circuit to do addition and subtraction operations, and the operations are performed between the 16A and look up table outputs.

B. APC-OMS for LUT Optimization

Only the odd multiples of the fixed coefficient (A) are stored in the LUT using the OMS technique, and all the even multiples of A are produced from the left-shift operations of one of those odd multiples. The product words for various input X values for an APC-OMS based LUT multiplier with $L = 5$ are displayed. For the input X, just nine memory spaces are required to hold the product values (00000). In Table II, you'll see that the eight odd multiples are stored in only eight memory places. Even multiples 2A, 4A are obtained by left-shift operations on fixed coefficient A.

Input, X	product values	Input, X	product values	address $x'_3x'_2x'_1x'_0$	APC words
0 0 0 0 1	A	1 1 1 1 1	31A	1 1 1 1	15A
0 0 0 1 0	2A	1 1 1 1 0	30A	1 1 1 0	14A
0 0 0 1 1	3A	1 1 1 0 1	29A	1 1 0 1	13A
0 0 1 0 0	4A	1 1 1 0 0	28A	1 1 0 0	12A
0 0 1 0 1	5A	1 1 0 1 1	27A	1 0 1 1	11A
0 0 1 1 0	6A	1 1 0 1 0	26A	1 0 1 0	10A
0 0 1 1 1	7A	1 1 0 0 1	25A	1 0 0 1	9A
0 1 0 0 0	8A	1 1 0 0 0	24A	1 0 0 0	8A
0 1 0 0 1	9A	1 0 1 1 1	23A	0 1 1 1	7A
0 1 0 1 0	10A	1 0 1 1 0	22A	0 1 1 0	6A
0 1 0 1 1	11A	1 0 1 0 1	21A	0 1 0 1	5A
0 1 1 0 0	12A	1 0 1 0 0	20A	0 1 0 0	4A
0 1 1 0 1	13A	1 0 0 1 1	19A	0 0 1 1	3A
0 1 1 1 0	14A	1 0 0 1 0	18A	0 0 1 0	2A
0 1 1 1 1	15A	1 0 0 0 1	17A	0 0 0 1	A
1 0 0 0 0	16A	1 0 0 0 0	16A	0 0 0 0	0

For $X = (0 0 0 0 0)$, the encoded word to be stored is 16A.

Table 1: APC Word Different Input Values for L=5

input X' $x'_3x'_2x'_1x'_0$	product value	# of shifts	shifted input, X''	stored APC word	address $d_3d_2d_1d_0$
0 0 0 1	A	0	0 0 0 1	$P_0 = A$	0 0 0 0
0 0 1 0	$2 \times A$	1			
0 1 0 0	$4 \times A$	2			
1 0 0 0	$8 \times A$	3			
0 0 1 1	3A	0	0 0 1 1	$P_1 = 3A$	0 0 0 1
0 1 1 0	$2 \times 3A$	1			
1 1 0 0	$4 \times 3A$	2			
0 1 0 1	5A	0	0 1 0 1	$P_2 = 5A$	0 0 1 0
1 0 1 0	$2 \times 5A$	1			
0 1 1 1	7A	0	0 1 1 1	$P_3 = 7A$	0 0 1 1
1 1 1 0	$2 \times 7A$	1			
1 0 0 1	9A	0	1 0 0 1	$P_4 = 9A$	0 1 0 0
1 0 1 1	11A	0	1 0 1 1	$P_5 = 11A$	0 1 0 1
1 1 0 1	13A	0	1 1 0 1	$P_6 = 13A$	0 1 1 0
1 1 1 1	15A	0	1 1 1 1	$P_7 = 15A$	0 1 1 1
input X $x_4x_3x_2x_1x_0$	product values	encoded word	stored values	# of shifts	address $d_3d_2d_1d_0$
1 0 0 0 0	16A	0	---	---	---
0 0 0 0 0	0	16A	2A	3	1 0 0 0

Table 2: OMS Words For Different Input Values for L=5

III. IMPLEMENTATION OF TECHNIQUES

A. APC Based LUT Multiplier

The block diagram of an APC-based LUT multiplier for L=5 is shown in Figure. It comprises of a four-input LUT with 16 words for storing the APC values of product words, as shown in Table I's sixth column. It also includes an address mapping circuit as well as an add/subtract block. Accordingly, the address circuit will provide the desired address (x3'x2'x1'x0'). The LUT output is then calculated based on the address, and the LUT output is subsequently added to or removed from 16A based on the most significant bit. The LUT output is added to 16A when the most significant bit is 1, and it is removed from 16A when x4=0.

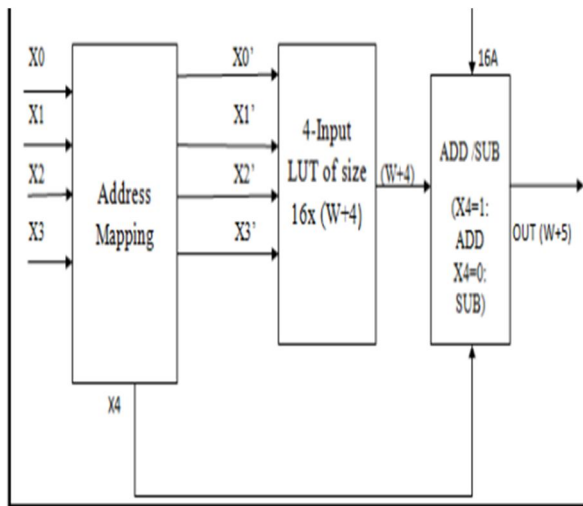


Figure 1: APC based LUT multiplier for L=5

B. APC-OMS based LUT multiplier

The block diagram of an APC-OMS based LUT multiplier for L=5 is shown in Figure. It comprises of a shifter, an address generating circuit, and a control circuit, as well as a LUT of nine words with a 4-bit width. The 5-bit input will be converted to a 4-bit address word by the address generating circuit (d3d2d1d0). The control circuit is utilized to generate the control bits s0, s1 that are used to produce the shifter's number of shifts. If the most significant bit is 0, the output is the same product word from the shifter; if the most significant bit is 1, the product is formed by adding addition 16A and the shifted value. The following expression generates the control signals.

$$S0 = \sim(x0 + (\sim(x1 + (\sim(x2)))))) \quad S1 = \sim(x0 + x1)$$

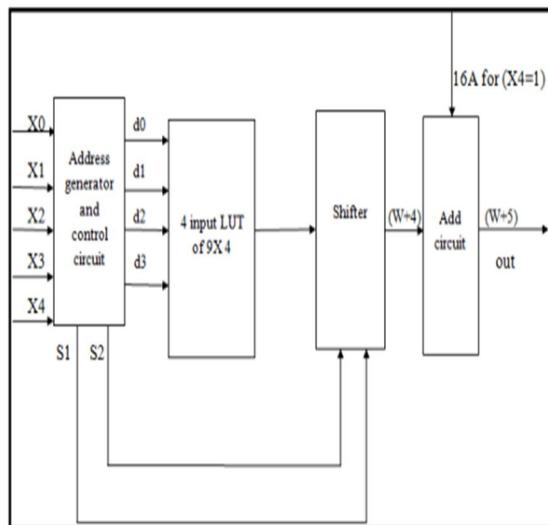


Figure 2 : APC-OMS based LUT multiplier for L=5

IV. SIMULATION RESULTS

The LUT-based multipliers based on APC, and APC-OMS are coded in Verilog HDL and generated in the Xilinx ISE design suite. The simulator used is I-sim tool. The family used is Automotive Artix 7, device is XA7A100T, Package is CSG324, and speed is -2. The delay may vary based on the family, device and package used.

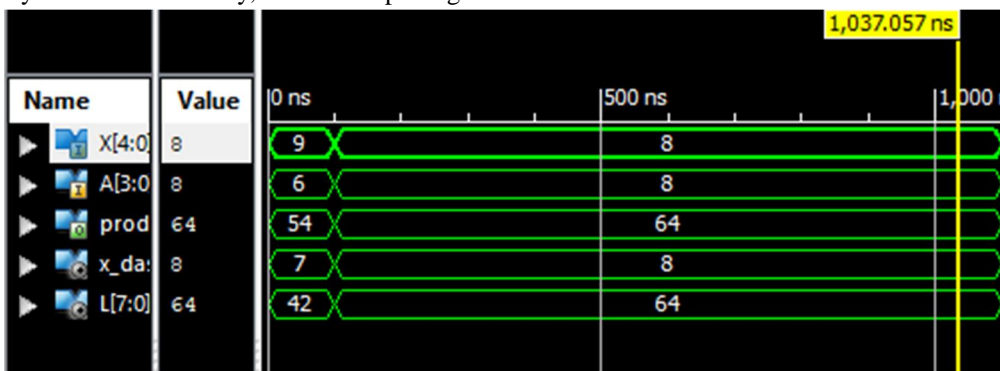


Figure 3: Simulation result of APC based LUT multiplier for L=5

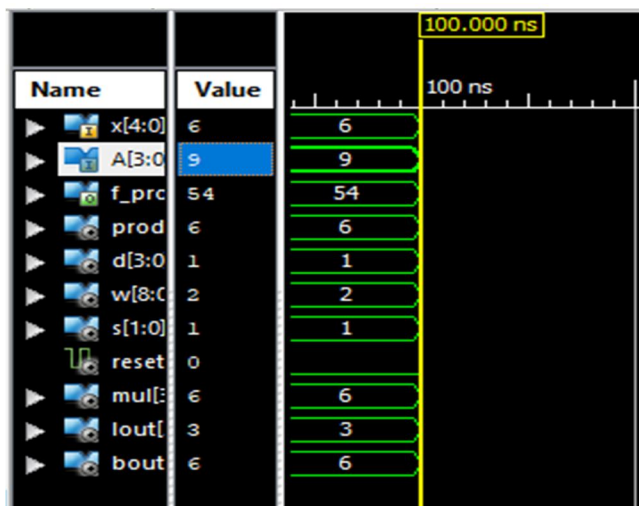


Figure 4: Simulation result of APC- OMS based LUT multiplier for L=5

```
Timing constraint: Default path analysis
Total number of paths / destination ports: 2587 / 9
-----
Delay: 6.148ns (Levels of Logic = 11)
Source: X<1> (PAD)
Destination: product<8> (PAD)

Data Path: X<1> to product<8>

Cell:in->out      fanout  Gate  Net  Logical Name (Net Name)
-----
IBUF:I->O          8  0.001  0.610  X_1_IBUF (X_1_IBUF)
LUT3:I0->O         3  0.097  0.628  m1/Mxor_x_dash<1>_xo<0>1 (x_da
LUT6:I2->O         5  0.097  0.594  ADDERTREE_INTERNAL_Madd1_lut<3
LUT6:I3->O         2  0.097  0.758  ADDERTREE_INTERNAL_Madd1_xor<4
LUT6:I0->O         2  0.097  0.748  ADDERTREE_INTERNAL_Madd2_lut<0
LUT6:I1->O         3  0.097  0.628  ADDERTREE_INTERNAL_Madd2_cy<0>
LUT6:I2->O         1  0.097  0.439  ADDERTREE_INTERNAL_Madd2_xor<0
LUT3:I1->O         1  0.097  0.000  m3/Maddsub_out_lut<7> (m3/Madd
MUXCY:S->O         0  0.353  0.000  m3/Maddsub_out_cy<7> (m3/Madd
XORCY:CI->O        1  0.370  0.339  m3/Maddsub_out_xor<8> (product
OBUF:I->O          0  0.000  0.000  product_8_OBUF (product<8>)
-----
Total 6.148ns (1.403ns logic, 4.745ns route)
(22.8% logic, 77.2% route)
```

Figure 5: The timing report of APC based circuit

```

Timing constraint: Default path analysis
Total number of paths / destination ports: 1855 / 9
-----
Delay:          5.380ns (Levels of Logic = 10)
Source:         x<1> (PAD)
Destination:    f_prod<8> (PAD)

Data Path: x<1> to f_prod<8>

Cell:in->out    fanout    Gate    Net    Logical Name (Net Name)
-----
IBUF:I->O       14    0.001  0.815  x_l_IBUF (x_l_IBUF)
LUT5:I0->O      1    0.097  0.439  bl/ml/Mmux_y_d[0]_MUX_8_o131 (b
LUT3:I1->O      1    0.097  0.753  bl/ml/Mmux_y_d[0]_MUX_8_o132 (b
LUT6:I0->O     15    0.097  0.517  sl/Mmux_s4l (prod<3>)
LUT6:I4->O      5    0.097  0.594  Mmult_f_prod_Madd1_cy<4>1 (Mmul
LUT5:I2->O      1    0.097  0.616  Mmult_f_prod_Madd1_cy<5>11 (Mmu
LUT6:I2->O      1    0.097  0.000  Mmult_f_prod_Madd2_lut<7> (Mmul
MUXCY:S->O      0    0.353  0.000  Mmult_f_prod_Madd2_cy<7> (Mmult
XORCY:CI->O     1    0.370  0.339  Mmult_f_prod_Madd2_xor<8> (f_pr
OBUF:I->O       0    0.000  0.000  f_prod_8_OBUF (f_prod<8>)
-----
Total          5.380ns (1.306ns logic, 4.074ns route)
              (24.3% logic, 75.7% route)

```

Figure 6: The timing report of APC-OMS based circuit

V. CONCLUSION

In this article, we demonstrated how LUT-based multipliers can be used to provide constant multiplication in DSP applications. However, if the LUTs are implemented as NAND or NOR read-only memories and the arithmetic shifts are done by an array barrel shifter using metal-oxide-semiconductor transistors, the full benefits of the proposed LUT-based system can be realized. Point to the future work is to observe this multiplier by incorporating it in FIR Filter and Adaptive Filter design. For reasonable area-delay tradeoffs, more work might be done to generate OMS-APC-based LUTs for larger input sizes using alternative types of decompositions and parallel and pipelined addition algorithms. As a result, the LUT multiplier based on APC-OMS can be employed in DSP applications such as interpolator designs. Furthermore, replacing the multipliers in the interpolator with the modified APC-OMS LUT based multiplier can improve operating speed while also reducing hardware complexity.

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