



# IJRASET

International Journal For Research in  
Applied Science and Engineering Technology



---

# INTERNATIONAL JOURNAL FOR RESEARCH

IN APPLIED SCIENCE & ENGINEERING TECHNOLOGY

---

**Volume: 5      Issue: III      Month of publication: March 2017**

**DOI: <http://doi.org/10.22214/ijraset.2017.3037>**

**[www.ijraset.com](http://www.ijraset.com)**

**Call:  08813907089**

**E-mail ID: [ijraset@gmail.com](mailto:ijraset@gmail.com)**

# **A Novel Three-Phase to Nine-Phase Transformation Using a Special Transformer Connection**

Bokam Poorna<sup>1</sup>, Pudi Sekhar<sup>2</sup>

<sup>1,2</sup>*Electrical and Electronics department, Vignan's Institute of Information Technology*

**Abstract:** *Multiphase (more than three-phase) electric drive system is the priority of an important research in the last decade. Three-phase supply is available from the grid, however for many industrial applications multiphase supply is necessary. In the multiphase power transmission and multiphase rectifier systems, the number of phases investigated is a multiple of three. This paper proposes a technique to obtain nine-phase output from three-phase supply system using special transformer connections. The primary windings of the transformer connected in star input and secondary side of the transformer connected in star output. The output phases with requisite phase angle of  $40^\circ$  between each phase is obtained using appropriate turns ratios. The connection scheme is designed and simulated in MATLAB/Simulink environment. From the simulation results, it is observed that, a pure nine-phase sine-wave of fixed voltage/current and frequency is obtained.*

**Keywords:** *converting transformer, multi-phase, nine-phase, Three-phase, turns ratio*

## **I. INTRODUCTION**

Multiphase (more than three-phase) electric drive system is the priority of an important research in the last decade. Three-phase supply is available from the grid, however for many industrial applications multiphase supply is necessary for its operation. There are different methods to transform three-to-nine-phase using 18-pulse converter, carrier based PWM technique, multilevel converter and multiphase transformer. These are more complex to design for higher ratings or a pure sine wave will not be acquired or harmonics will be more. Multiphase power transmission system is also explored in the literature because multiphase transformers are required at the input of rectifiers. In the multiphase power transmission and multiphase rectifier systems, the number of phases investigated is a multiple of three. Therefore, the variable speed multiphase drive system examined in the literature are mostly of five, seven, nine, eleven, twelve, and fifteen phases. Multiphase systems are advantages compared to three-phase systems have brought relevant to researcher interest. The applicability of multiphase systems is enquired into in electric power generation [1]-[7], transmission [8]-[14], utilization [15]-[32]. The research on six phase transmission systems was proposed due to increasing cost of right-of-way for transmission corridors, environmental issues, and different severe licensing laws. Six-phase transmission lines can produce the same power capacity with a lower line voltage and smaller towers as compared to a standard double circuit three-phase line. The calculus of the six-phase smaller towers may also lead to the depletion of magnetic fields and electromagnetic interference [11]. The research on multiphase generators has latterly started and only a small number of referrals are available [1]-[7]. The work on multiphase power generation has investigated asymmetrical six-phase (two sets of stator windings with  $30^\circ$  phase displacement) induction generator configuration as a solution for the use in renewable energy generation. The research on multiphase drive systems has been significantly developed since the beginning of this century due to advancement in semiconductor devices and digital signal processors technologies [17]-[21]. It is to be emphasized here that ac/dc/ac converters generally supply the multiphase motors. Thus, the focus of current research on multiphase electric drives is limited to the modelling and controlling the power converters [22]-[32]. Little effort is being made to develop any static multi winding transformation system to change the phase number from three-phase to n-phase (where  $n > 3$  and odd). An exception is, proposing a novel phase transformation system which is three-phase to five-phase system. In [31] and [32], the authors presented a solution for three-phase to five-phase conversion and three-phase to seven-phase conversion.

Multiphase, especially a 6-phase and 12-phase, systems are found to produce less amplitude ripples with higher frequency in an ac-dc rectifier system. Thus a 6-phase and 12-phase transformers are designed to feed a multi-pulse rectifier system. The reason of choice for a 6-, 12-, or 24-phase system is that these numbers are multiples of three and designing this type of system is simple and straightforward. However, increasing the number of phases certainly enhances the complexity of the system. No such designs are available for an odd number of phases.

## International Journal for Research in Applied Science & Engineering Technology (IJRASET)

In three-phase to five-phase transformation [31], primary winding connected in a star as three-phase input. Phase difference between in each phase is  $120^{\circ}$  apart. secondary winding connected in a star as five-phase output. Phase difference between in each phase is  $72^{\circ}$  apart. Thus, with this technique, a pure five-phase sine-wave of fixed voltage and frequency is obtained. In three-phase to seven-phase transformation [32], primary winding connected in a star as three-phase input. Phase difference between in each phase is  $120^{\circ}$  apart. secondary winding connected in a star as five-phase output. Phase difference between in each phase is  $51.42^{\circ}$  apart. Thus, with this technique, a pure seven-phase sine-wave of fixed voltage and frequency is obtained.

This paper proposes a special transformer connection scheme to obtain a balanced three-phase to nine-phase supply. The remainder of the paper is organized as follows: In section 2, presents the winding arrangement nine-phase star output where as In section 3 presents simulations results of three-phase to nine-phase transformation. Finally to conclude that three-phase to nine-phase transformation in section 4.

### II. WINDING ARRANGEMENT OF NINE-PHASE STAR OUTPUT

The objective of the work is to design and implement three phase to nine phase transformation using a special transformer connection. The Fig. 1. shows the block diagram of three-phase to nine-phase transformation.

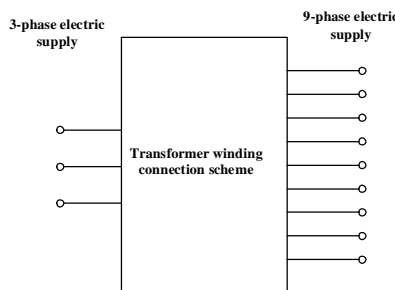


Fig.1. Block representation of the system.

The fixed three-phase voltage and fixed frequency is available in grid supply can be transformed to the fixed voltage and fixed frequency nine-phase output supply. The output magnitude may be made variable by connecting the autotransformer at the input side. The input and output supply can be arranged in the following manners:

- Input star, output star;
- Input star, output nonagon;
- Input delta, output star;
- input delta, output nonagon;

Since input is a three-phase system, the windings are connected in normally were as, the output/secondary side star connection is discussed in the following sections. The nonagon output connection may be derived following a similar approach. Thus, only star output connection is discussed in this paper.

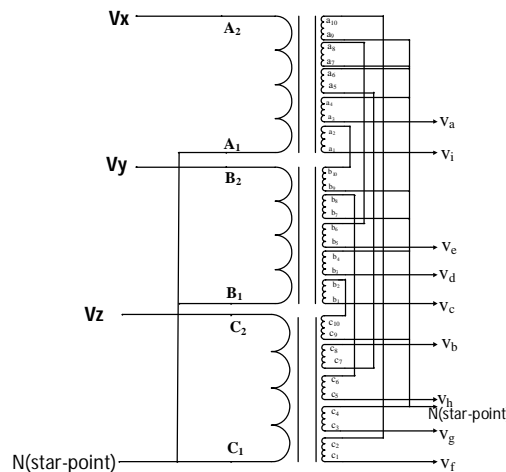


Fig. 2. Transformer winding arrangement of three-phase to nine-phase transformation (star-star)

## International Journal for Research in Applied Science & Engineering Technology (IJRASET)

The Fig. 2. shows the winding arrangement of three-phase to nine-phase transformation. Three separate cores are designed with each of them carrying one primary coil and five secondary coils are wound. Six primary terminals connected in an appropriate manner resulting in star/delta connections, and the 30 secondary terminals are connected in a different fashion resulting in a star/nonagon output. The Fig. 3 shows the winding connection along with turns ratios and the corresponding phasor diagram is shown in Fig. 4. The construction of output phases with requisite phase angles of  $360/9 = 40^\circ$  between each phase is obtained using appropriate turn ratios and the phasor equation as given in (1). The turn ratios are different in each phase. The choice of turn ratio is the key in creating the phase displacement in the output phases. The turn ratios between different phases are given in Table I.

Table I -Turn Ratio Secondary Turns ( $N_2$ ) To Primary Turns ( $N_1$ )

Name of winding	Turn ratio $N_2/N_1$	Name of winding	Turn ratio $N_2/N_1$	Name of winding	Turn ratio $N_2/N_1$
$a_1 a_2$	0.394	$b_1 b_2$	0.394	$c_1 c_2$	0.394
$a_3 a_4$	1.000	$b_3 b_4$	1.000	$c_3 c_4$	1.000
$a_5 a_6$	0.394	$b_5 b_6$	0.394	$c_5 c_6$	0.394
$a_7 a_8$	0.7422	$b_7 b_8$	0.7422	$c_7 c_8$	0.7422
$a_9 a_{10}$	0.7422	$b_9 b_{10}$	0.7422	$c_9 c_{10}$	0.7422

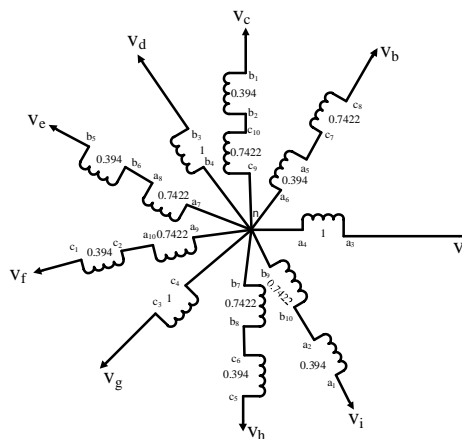


Fig. 3. Transformer winding connection of three-phase to nine-phase transformation (star-star)

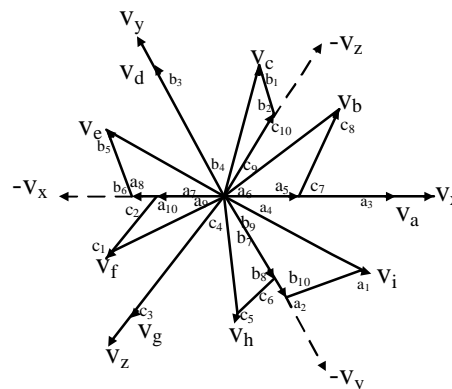


Fig. 4. Phasor diagram of three-phase to nine-phase transformation (star-star)

## International Journal for Research in Applied Science & Engineering Technology (IJRASET)

The input phases are represented with letters “X”, “Y” and “Z” and the outputs are represented with letters “a”, “b”, “c”, “d”, “e”, “f”, “g”, “h” and “i” as illustrated in Fig. 3. The output phase “a” is along the input phase “X”. The output phase “b” results from the phasor sum of winding voltage “a<sub>6</sub>a<sub>5</sub>” and “c<sub>7</sub>c<sub>8</sub>”, the output phase “c” results from the phasor sum of winding voltage “c<sub>9</sub>c<sub>10</sub>” and “b<sub>2</sub>b<sub>1</sub>”, the output phase “d” is along the input phase “Y”, the output phase “e” results from the phasor sum of winding voltage “a<sub>7</sub>a<sub>8</sub>” and “b<sub>6</sub>b<sub>5</sub>”, the output phase “f” results from the phasor sum of winding voltage “a<sub>9</sub>a<sub>10</sub>” and “c<sub>2</sub>c<sub>1</sub>”, the output phase “g” is along the input phase “Z”, the output phase “h” results from the phasor sum of winding voltage “b<sub>7</sub>b<sub>8</sub>” and “c<sub>6</sub>c<sub>5</sub>”, the output phase “i” results from the phasor sum of winding voltage “b<sub>9</sub>b<sub>10</sub>” and “a<sub>2</sub>a<sub>1</sub>”. The mathematical basis for this connection is the basic addition of real and imaginary parts of the vectors. For example, the solution for (1) gives the turn ratio of phase “b” (V<sub>b</sub> taken as unity)

$$v_x \left[ \cos\left(\frac{2\pi}{9}\right) + j \sin\left(\frac{2\pi}{9}\right) \right] - v_z \left[ \cos\left(\frac{\pi}{9}\right) - j \sin\left(\frac{\pi}{9}\right) \right] = 1 \dots\dots(1)$$

Equating real and imaginary parts and solving for V<sub>x</sub> and V<sub>z</sub>.

$$|v_x| = \frac{\left| \sin\left(\frac{\pi}{9}\right) \right|}{\left| \sin\left(\frac{\pi}{3}\right) \right|} = 0.394 \dots\dots\dots(2)$$

$$|v_z| = - \frac{\left| \sin\left(\frac{2\pi}{9}\right) \right|}{\left| \sin\left(\frac{\pi}{3}\right) \right|} = 0.7422 \dots\dots\dots(3)$$

Equation (4) is the result of solutions of (1). Similarly for other equations also

$$\begin{bmatrix} v_a \\ v_b \\ v_c \\ v_d \\ v_e \\ v_f \\ v_g \\ v_h \\ v_i \end{bmatrix} = \frac{1}{\sin\left(\frac{\pi}{3}\right)} \begin{bmatrix} \sin\left(\frac{\pi}{3}\right) & 0 & 0 \\ \sin\left(\frac{\pi}{9}\right) & 0 & -\sin\left(\frac{\pi}{9}\right) \\ 0 & \sin\left(\frac{\pi}{9}\right) & -\sin\left(\frac{\pi}{9}\right) \\ 0 & \sin\left(\frac{\pi}{3}\right) & 0 \\ -\sin\left(\frac{\pi}{9}\right) & \sin\left(\frac{\pi}{9}\right) & 0 \\ -\sin\left(\frac{\pi}{9}\right) & 0 & \sin\left(\frac{\pi}{9}\right) \\ 0 & 0 & \sin\left(\frac{\pi}{3}\right) \\ 0 & -\sin\left(\frac{\pi}{9}\right) & \sin\left(\frac{\pi}{9}\right) \\ \sin\left(\frac{\pi}{9}\right) & -\sin\left(\frac{\pi}{9}\right) & 0 \end{bmatrix} \begin{bmatrix} v_x \\ v_y \\ v_z \end{bmatrix} \dots\dots\dots(4)$$

## International Journal for Research in Applied Science & Engineering Technology (IJRASET)

$$v_a = v_{\max} \sin(\omega t) \dots\dots\dots(5)$$

$$v_b = v_{\max} \sin\left(\omega t + \frac{2\pi}{9}\right) \dots\dots\dots(6)$$

$$v_c = v_{\max} \sin\left(\omega t + \frac{4\pi}{9}\right) \dots\dots\dots(7)$$

$$v_d = v_{\max} \sin\left(\omega t + \frac{6\pi}{9}\right) \dots\dots\dots(8)$$

$$v_e = v_{\max} \sin\left(\omega t + \frac{8\pi}{9}\right) \dots\dots\dots(9)$$

$$v_f = v_{\max} \sin\left(\omega t - \frac{8\pi}{9}\right) \dots\dots\dots(10)$$

$$v_g = v_{\max} \sin\left(\omega t - \frac{6\pi}{9}\right) \dots\dots\dots(11)$$

$$v_h = v_{\max} \sin\left(\omega t - \frac{4\pi}{9}\right) \dots\dots\dots(12)$$

$$v_i = v_{\max} \sin\left(\omega t - \frac{2\pi}{9}\right) \dots\dots\dots(13)$$

$$v_x = v_{\max} \sin(\omega t) \dots\dots\dots(14)$$

$$v_y = v_{\max} \sin\left(\omega t + \frac{2\pi}{3}\right) \dots\dots\dots(15)$$

$$v_z = v_{\max} \sin\left(\omega t - \frac{2\pi}{3}\right) \dots\dots\dots(16)$$

Therefore, by summing the voltages of two different coils, one output phase is created. It is important to note that the phase “a” output is generated from only one coil namely”a<sub>3a4</sub>” in contrast to other phases which utilizes two coils. Thus, the voltage rating of “a<sub>3a4</sub>” coil should be kept to that of rated phase voltage to obtain balanced and equal voltages.

### III. SIMULATION RESULTS

To realize the effectiveness of the proposed connection scheme, it is designed and implemented in MATLAB/Simulink environment. The Fig. 5 shows three-phase input voltage. The corresponding output voltage waveforms for the designed transformer scheme is shown in Fig. 6. It can be observed that the output is a balanced nine-phase supply for a balanced three-phase input.

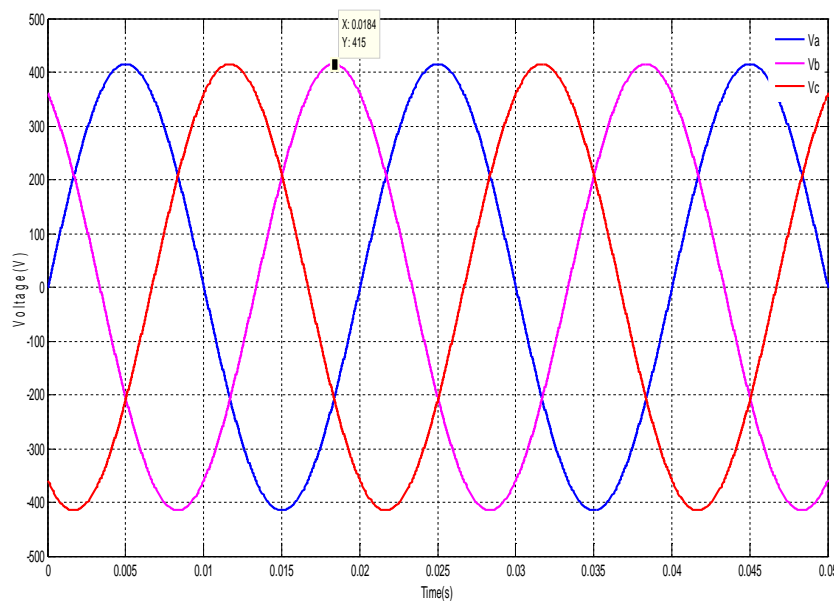


Fig. 5. Input voltage (Three-phase).

# International Journal for Research in Applied Science & Engineering Technology (IJRASET)

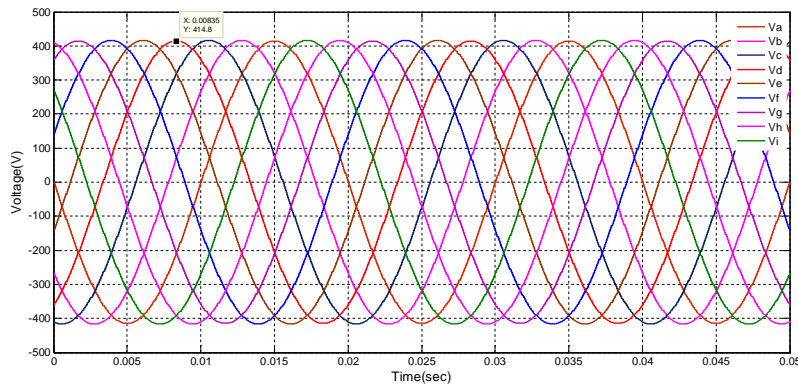


Fig. 6. Output voltage of three-phase to nine-phase transformation.

Further, an RL ( $R= 300 \Omega$ ,  $L= 40 \text{ mH}$ ) load is connected to study the performance of the transformer. The Fig. 7 and 8 shows the voltage and current at the load side. The output voltages can be altered by simply varying the taps of the autotransformer.

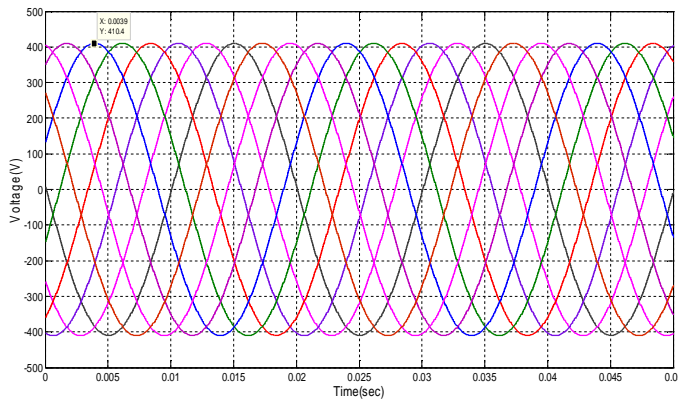


Fig. 7. Load voltage of three-phase to nine-phase transformation.

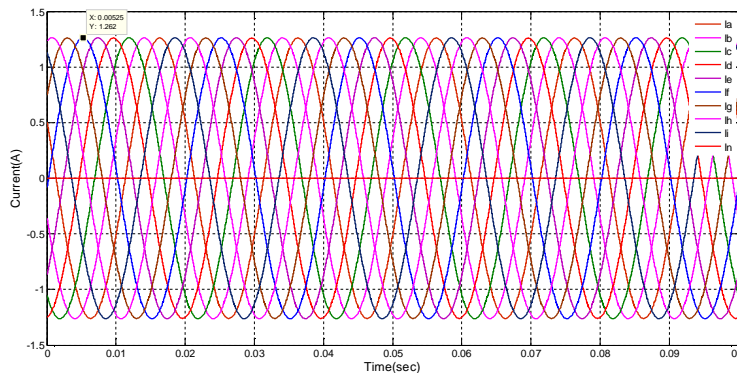


Fig. 8. Load current of three-phase to nine-phase transformation.

## IV. CONCLUSIONS

This paper proposes a novel transformer connection scheme to transform the three-phase grid power to a nine-phase output supply. The connection scheme and the phasor diagram along with turn ratios are presented. To realize the effectiveness of the connection scheme, it is designed and implemented in MATLAB/Simulink under no-load and RL loading condition. The simulation results proved that the proposed connection scheme is efficient in transforming three-phase to nine-phase supply. It is expected that the proposed connection scheme can be used in drives and multiphase applications.

# International Journal for Research in Applied Science & Engineering Technology (IJRASET)

## REFERENCES

- [1] G.K. Singh, "Self excited induction generator research—A survey," *Elect. Power Syst. Res.*, vol. 69, pp. 107–114, 2004.
- [2] O. Ojo and I. E. Davidson, "PWM-VSI inverter-assisted stand-alone dual stator winding induction generator," *IEEE Trans. Energy Convers.*, vol. 36, no. 6, pp. 1604–1611, Nov./Dec. 2000.
- [3] G. K. Singh, K. B. Yadav, and R. P Sani, "Analysis of saturated multiphase (six-phase) self excited induction generator," *Int J. Emerg. Electr. Power Syst.*, vol. 7, no. 2, Sep. 2006.
- [4] G. K. Singh, "Modelling and experimental analysis of a self-excited six-phase induction generator for stand -alone renewable energy generation," *Renewable Energy*, vol. 33, no. 7, pp. 1605–162, Jul. 2008
- [5] J. R. Stewart and D. D.Wilson, "High phase order transmission—A feasibility analysis—Part-I: Steady state considerations," *IEEE Trans. Power App. Syst.*, vol. PAS-97, no. 6, pp. 2300–2307, Nov. 1978.
- [6] J.R. Stewart and D.D.Wilson, "High phase order transmission-A feasibility analysis—Part-II: Over voltages and insulation requirements," *IEEE Trans. Power App. Syst.*, vol. PAS-97, no. 6, pp. 2308–2317, Nov. 1978
- [7] J. R. Stewart, E. Kallaur, and J. S. Grant, "Economics of EHV high phase order transmission," *IEEE Trans. Power App. Syst.*, vol. -PAS 103, no. 11, pp. 3386–3392, Nov. 1984
- [8] S. N. Tewari, G. K. Singh, and A. B. Saroor, "Multiphase Power transmission research—A survey," *Electr. Power Syst. Res.*, vol. 24, pp. 207–215, 1992
- [9] C. M. Portela and M.C. Tavares, "Six-phase transmission line-propagation characteristics and new three-phase representation," *IEEE Trans. Power Delivery*, vol. 18, no. 3, pp. 1470–1483, Jul. 1993.
- [10] T. L. Landers, R. J. Richeda, E. Krizanskas, J. R. Stewart, and R. A. Brown, "High phase order economics: Constructing a new transmission line," *IEEE Trans. Power Delivery*, vol. 13, no. 4, pp. 1521–1526, Oct. 1998.
- [11] J. M. Arroyo and A. J. Conejo, "Optimal response of power generators to energy, AGC, and reserve pool based markets," *IEEE Power Eng. Rev.*, vol. 22, no. 4, pp. 76–77, Apr. 2002
- [12] M. A. Abbas, R. Chirsten, and T
- [13] . M. Jahns, "Six-phase voltage source inverter driven induction motor," *IEEE Trans. Ind. Appl.*, vol. IA-20, no. 5, pp. 1251–1259, Sep./Oct. 1984
- [14] K. N. Pavithran, R. Parimelalagan, and M. R. Krsihnamurthy, "Studies on inverter fed five-phase induction motor drive," *IEEE Trans. Power Elect.*, vol. 3, no. 2, pp. 224–235, Apr. 1988.G. K. Singh, "Multi-phase induction machine drive research—A survey," *Electr. Power Syst. Res.*, vol. 61, pp. 139–147, 2002
- [15] R. Bojoi, F. Farina,
- [16] F. Profumo, and A. Tenconi, "Dual-three phase induction machine drives control—A survey," *IEE J. Trans. Ind. Appl.*, vol. 126, no. 4, pp. 420–429, 2006. E. Levi, R. Bojoi, F. Profumo, H. A. Toliyat, and S. Williamson, "Multiphase induction motor drives—A technology status review," *IET Electr. Power Appl.*, vol. 1, no. 4, pp. 489–516, Jul. 2007.
- [17] E. Levi, "Multiphase electric machines for variable-speed applications," *IEEE Trans Ind. Elect.* vol. 55, no. 5, pp. 1893–1909, May 2008.
- [18] A. Iqbal and E. Levi, "Space vector PWM techniques for sinusoidal output voltage generation with a five-phase voltage source inverter," *Electr. Power Compon. Syst.*, vol. 34, no. 2, pp. 119–140, 2006.
- [19] D. Dujic, M. Jones, and E. Levi, "Generalized space vector PWM for sinusoidal output voltage generation with multiphase voltage source inverter," *Int. J. Ind. Elect. Drives*, vol. 1, no. 1, pp. 1–13, 2009.
- [20] M. J. Duran, F. Salas, and M. R. Arahah, "Bifurcation analysis of five-phase induction motor drives with third harmonic injection," *IEEE Trans. Ind. Elect.*, vol. 55, no. 5, pp. 2006–2014, May 2008
- [21] M. R. Arahah and M. J. Duran, "PI tuning of five-phase drives with third harmonic injection," *Control Engg. Pract.*, vol. 17, no. 7, pp. 787–797, Jul. 2009.
- [22] D. Dujic, M. Jones, and E. Levi, "Analysis of output current ripple rms in multiphase drives using space vector approach," *IEEE Trans. Power Elect.*, vol. 24, no. 8, pp. 1926–1938, Aug. 2009.
- [23] M. Correa, C. R. da Silva, H. Razik, C. B. Jacobina, and E. da Silva, "Independent voltage control for series-connected six-and three-phase Induction machines," *IEEE Trans. Ind. Appl.*, vol. 45, no. 4, pp. 1286–1293, Jul./Aug. 2009.
- [24] M. Jones, "A novel concept of a multi-phase multi-motor vector controlled drive system," Ph.D. dissertation, School Eng., Liverpool John Moores Univ., School Eng., Liverpool, U.K., 2005.
- [25] S. Choi, B. S. Lee, and P. N. Enjeti, "New 24-pulse diode rectifier systems for utility interface of high power AC motor drives," *IEEE Trans. Ind. Appl.*, vol. 33, no. 2, pp. 531–541, Mar./Apr. 1997.
- [26] V. Garg, B. Singh, and G. Bhuvaneswari, "A tapped star connected autotransformer based 24-Pulse AC-DC converter for power quality improvement in induction motor drives," *Int. J. Emerg. Electr. Power Syst.*, vol. 7, no. 4, 2006.
- [27] B. Singh and S. Gairola, "An autotransformer based 36 pulse controlled ac–dc converter," *IETE J. Res.*, vol. 54, no. 4, pp. 255–262, 2008.B. Sing
- [28] Gairola, "A 24 pulse AC-DC converter employing a pulse doubling technique for vector controlled induction motor drives," *IETE J. Res.*, vol. 54, no. 4, pp. 314–322, 2008.
- [29] P. C. Krause, *Analysis of Electric Machinery*. New York: McGraw-Hill, 1986.
- [30] M. H. Rashid, *Power Electronics Handbook: Devices, Circuits, and Applications*, 3rd ed. Amsterdam, The Netherlands: Elsevier, 2011.
- [31] A. Iqbal, S. Moinuddin, M. R. Khan, SK. M. Ahmed, and H. Abu-Rub, "A novel three-phase to five-phase transformation using special transformer connection," *IEEE Trans. Power Delivery*, vol. 25, no. 3, pp. 1637–1644, Jun. 2010.
- [32] A. Iqbal, S. Moinuddin, M. R. Khan, SK. M. Ahmed, and H. Abu-Rub, "Three-phase to Seven-phase transformation using power converter," *IEEE Trans. Power Delivery*, vol. 27, no. 3, July. 2012.
- [33] A. Iqbal, "Modelling and control of series-connected five-phase and six-phase two-motor drive," Ph.D. dissertation, School Eng., Liverpool John Moores Univ., School Eng., Liverpool, U.K., 2006.
- [34] G. K. Singh, K. B. Yadav, and R. P. Saini, "Modelling and analysis of multiphase (six-phase) self-excited induction generator," in *Proc. 8th Int. Conf. Electr. Mach. Syst.*, 2005, pp. 1922–1927.





10.22214/IJRASET



45.98



IMPACT FACTOR:  
7.129



IMPACT FACTOR:  
7.429



# INTERNATIONAL JOURNAL FOR RESEARCH

IN APPLIED SCIENCE & ENGINEERING TECHNOLOGY

Call : 08813907089  (24\*7 Support on Whatsapp)