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# **New functions in BiČech sgβ-Biclosure spaces**

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Abstract: The aim of this paper is to introduce the concept of BiČech sgß –continuous functions, BiČech sgß-Irresolute functions, Totally BiČech sgß –continuous functions functions and Slightly BiČech sgß –continuous functions in Biclosure spaces and investigate their characterizations.

Keywords: BiČech sgß-closed sets, BiČech sgß-open sets, BiČech sgß – continuous, BiČech sgß Irresolute, Totally BiČech sgß – continuous functions and Slightly BiČech sgß - continuous functions.

#### I. INTRODUCTION

Čech spaces were introduced by Eduard Čech [3] (i.e., sets endowed with a grounded, Extensive and additive closure operators) and studied by many others[6][12]. BiČech closure spaces were introduced by K.Chandrasekhara Rao, R. Gowri and V. Swaminathan [4]. N. Levine [13] introduced g-closed sets. D. Andrijevic [1] initiated the study of  $\beta$ -open sets and  $\beta$ -closed sets. In this paper, we analyze the concept of BiČech sg $\beta$  –continuous functions and BiČech sg $\beta$  –Irresolute functions, Totally BiČech sg $\beta$  –continuous functions in biclosure spaces and discuss some of their basic properties.

### **II. PRELIMINARIES**

**Definition 2.1:** Two maps  $k_1$  and  $k_2$  from power set X to itself are called BiČech closure operator on X and the pair (X,  $k_1$ , $k_2$ ) is called a BiČech closure spaces if the following axioms are satisfied

 $k_{1} (φ) = φ & k_{2}(φ) = φ$   $A ⊆ k_{1}(A) & A ⊆ k_{2} (A) \text{ for every } A ⊆ X$   $k_{1}(A ∪ B) = k_{1}(A) ∪ k_{1}(B) \text{ and } k_{2}(A ∪ B) = k_{2}(A) ∪ k_{2}(B) \text{ for all } A, B ⊆ X.$  **Definition 2.2** [5] A subset A in a BiČech closure space (X, k<sub>1</sub>, k<sub>2</sub>) is said to be k<sub>i</sub>-regular open if A = int<sub>k<sub>i</sub></sub> (k<sub>i</sub>(A)), i = 1, 2 k<sub>i</sub> -regular closed if A = k<sub>i</sub> (int<sub>k<sub>i</sub></sub> (A)), i = 1, 2 k<sub>i</sub>-semi open if A ⊆ k<sub>i</sub> (int<sub>k<sub>i</sub></sub> (A)) ⊆ A, i = 1, 2 k<sub>i</sub>-semi closed if int<sub>k<sub>i</sub></sub> (k<sub>i</sub>(A)) ⊆ A, i = 1, 2 k<sub>i</sub>-pre open if A ⊆ int<sub>k<sub>i</sub></sub> (k<sub>i</sub>(A)) ⊆ A, i = 1, 2 k<sub>i</sub> -α open if A ⊆ int<sub>k<sub>i</sub></sub> (k<sub>i</sub> (int<sub>k<sub>i</sub></sub> (A))), i = 1, 2 k<sub>i</sub> -α open if A ⊆ int<sub>k<sub>i</sub></sub> (k<sub>i</sub> (int<sub>k<sub>i</sub></sub> (A))) ⊆ A, i = 1, 2 k<sub>i</sub> -β open if A ⊆ k<sub>i</sub> (int<sub>k<sub>i</sub></sub> (k<sub>i</sub> (A))) ⊆ A, i = 1, 2 k<sub>i</sub> -β closed if (int<sub>k<sub>i</sub></sub> (k<sub>i</sub> (int<sub>k<sub>i</sub></sub> (k<sub>i</sub>(A)))) ⊆ A, i = 1, 2 k<sub>i</sub> -β closed if (int<sub>k<sub>i</sub></sub> (k<sub>i</sub> (intA)))) ⊆ A, i = 1, 2. **Definition 2.3:** A subset A of a BiČech closure space (X, k<sub>1</sub>, k<sub>2</sub>) is called bicket

**Definition 2.3:** A subset A of a BiČech closure space (X,  $k_1,k_2$ ) is called biclosed if  $k_1A = A = k_2A$  and called biopen if its complement is biclosed.

**Definition 2.4:** A subset A of a BiČech closure space (X,  $k_1, k_2$ ) is said to be  $(k_1, k_2)$ -g biclosed if  $k_2(A) \subseteq G$  whenever  $A \subseteq G$  and G is  $k_1$  open set in X.

**Definition 2.5:** A subset A of a BiČech closure space (X,  $k_1, k_2$ ) is said to be  $(k_1, k_2)-\pi g\alpha$  biclosed if  $k_{2\alpha}(A) \subseteq G$  whenever  $A \subseteq G$  and G is  $k_1 \pi$  -open set in X.



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**Definition 2.6:** Let  $(X, k_1, k_2)$  be a BiČech closure space. A subset  $A \subseteq X$  is said to be  $(k_1, k_2)$ -w -biclosed set if  $k_2(A) \subseteq G$  whenever  $A \subseteq G$  and G is  $k_1$  semi-open set in X.

**Definition 2.7:** Let  $(X, k_1, k_2)$  be a BiČech closure space. A subset  $A \subseteq X$  is said to be  $(k_1, k_2)$ -J- Cech-biclosed set if  $k_{\alpha}(A) \subseteq G$  whenever  $A \subseteq G$  and G is  $k_1$  semi-open set in X, where  $k_{\alpha}(A)$  is the smallest  $\alpha$ -closed set containing A.

**Definition 2.8:** Let  $(X, k_1, k_2)$  be a BiCech closure space. A subset  $A \subseteq X$  is called  $(k_1, k_2)$ -sg $\beta$  closed set if  $k_{2\beta}(A) \subseteq G$  whenever  $A \subseteq G$  and G is semi-open subset of  $(X, k_1)$  where  $k_{2\beta}(A)$  is the smallest  $\beta$ -closed set containing A.

# III. BICECH $sg\beta$ – CONTINUOUS FUNCTIONS

**Definition 3.1:** Let  $(X, k_1, k_2)$  and  $(Y, v_1, v_2)$  be a BiCech biclosure space. A map  $f: (X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  is called BiCech sg $\beta$ -continuous if every  $f^{-1}(v)$  is BiCech sg $\beta$  - open set in  $(X, k_1, k_2)$  for every biopen set V in  $(Y, v_1, v_2)$ .

**Definition 3.2:** A function  $f:(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  is called

(a) continuous if  $f^{-1}(V)$  is biclosed in X for each biclosed set V of Y.

(b) g-continuous if  $f^{-1}(V)$  is g-biclosed in X for each biclosed set V of Y.

(c) w-continuous if  $f^{1}(V)$  is w-biclosed in X for each biclosed set V of Y.

(d) J-continuous if  $f^{1}(V)$  is J-biclosed in X for each biclosed set V of Y.

(e)  $\pi g\alpha$ -continuous if  $f^1(V)$  is  $\pi g\alpha$ -biclosed in X for each biclosed set V of Y.

## **Proposition 3.3:**

(a) Every BiČech continuous is BiČech  $sg\beta$  – continuous.

(b) Every BiČech g – continuous is BiČech  $sg\beta$  – continuous.

(c) Every BiČech w – continuous is BiČech  $sg\beta$  – continuous.

(d) Every BiČech J -continuous is BiČech  $sg\beta$  – continuous.

(e) Every BiČech  $\pi g \alpha$  -continuous is BiČech  $sg\beta$  – continuous.

**Proof:** (a) Let f be a BiČech continuous. Let V be a BiČech open set in  $(Y, v_1, v_2)$ . Since f is BiČech continuous,  $f^{-1}(V)$  is BiČech open set of  $(X, k_1, k_2)$ . Every BiČech open set is BiČech sg $\beta$  – open set.

This implies that  $f^{-1}(V)$  is BiČech sg $\beta$  – open set of (X,  $k_1, k_2$ ), for every BiČech open set V in (Y,  $v_1, v_2$ ). (i.e.,) f is BiČech

 $sg\beta$  – continuous. Therefore every BiČech continuous is BiČech  $sg\beta$  – continuous.

Note: The proof is obvious for others.

Remark 3.4: Converse of the above theorem need not be true which can be seen from the following example.

**Example 3.5:** (a) Let  $X = \{a, b, c\}, Y = \{1, 2, 3\}.$ 

Define a closure operator  $k_1, k_2$  on X by  $k_1\{\phi\} = \{\phi\}, k_1\{a\} = k_1\{a,b\} = \{a,b\}, k_1\{c\} = k_1\{b,c\} = \{b,c\}, k_1\{c\} = \{b,c\}, k_1\{c\}, k_1\{c\} = \{b,c\}, k_1\{c\}, k_1$ 

 $k_1\{b\} = \{b\}, k_1\{a,c\} = k_1\{X\} = X, k_2\{\phi\} = \{\phi\}, k_2\{a\} = k_2\{a,c\} = \{a,c\}, k_2\{b\} = k_2\{b,c\} = \{b,c\}, k_2\{c\} = \{c\}, k_2\{a,b\} = k_2\{X\} = X.$ BiČech closed set of  $X = \{X, \phi, \{b,c\}\}.$ 

 $(k_1,k_2)$  sg $\beta$  - closed set of X = { X,  $\phi$ , {a}, {b}, {c}, {a,c}, {b,c}}.

 $\begin{array}{l} \text{Define a closure operator } v_1, v_2 \text{ on } Y \text{ by } v_1\{\phi\} = \{\phi\}, v_1\{1\} = \{1\}, v_1\{3\} = \{3\}, v_1\{1,3\} = \{1,3\}, v_1\{2\} = v_1\{1,2\} = v_1\{2,3\} = v_1\{Y\} = Y, v_2\{\phi\} = \{\phi\}, v_2\{3\} = \{3\}, v_2\{1,2\} = \{1,2\}, v_2\{1\} = v_2\{2\} = v_2\{1,3\} = v_2\{2,3\} = v_2\{Y\} = Y. \end{array}$ 

Biclosed set of  $Y = \{ Y, \phi, \{3\} \}.$ 

Let f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  be defined by f(a) = 2, f(b) = 3, f(c) = 1. Then f is  $(k_1, k_2) \operatorname{sg}\beta$  – continuous but not continuous. Since for the biclosed set {3} in Y, the inverse image  $f^{-1}{3} = {b}$  is not BiČech closed set in X.

**Example 3.6:** (b)Let X = {a, b, c}, Y = {p, q, r}. Define a closure operator  $k_1, k_2$  on X by  $k_1\{\varphi\} = \{\varphi\}$ ,

 $k_1\{a\} = k_1\{a,c\} = \{a,c\}, k_1\{b\} = k_1\{b,c\} = \{b,c\}, k_1\{c\} = \{c\}, k_1\{a,b\} = k_1\{X\} = X, k_2\{\phi\} = \{\phi\}, k_1\{a,b\} = k_1\{x\} = X, k_2\{\phi\} = \{\phi\}, k_1\{a,b\} = k_1\{a,c\} = \{a,c\}, k_1\{b,c\} = \{b,c\}, k_1\{c\} = \{c\}, k_1\{a,b\} = k_1\{X\} = X, k_2\{\phi\} = \{\phi\}, k_1\{a,b\} = k_1\{a,c\} = \{b,c\}, k_1\{a,b\} = \{b,c\}, k_1\{a,b\} = k_1\{a,c\} = k_1\{a,c\}, k_1\{b,c\} = \{b,c\}, k_1\{c\} = \{c\}, k_1\{a,b\} = k_1\{X\} = X, k_2\{\phi\} = \{\phi\}, k_1\{a,b\} = k_1\{a,c\}, k_1\{b,c\} = \{b,c\}, k_1\{a,b\} = k_1\{a,b\} = k_1\{a,b\}, k_1\{a$ 

 $k_{2}{b} = k_{2}{c} = k_{2}{b,c} = {b,c}, k_{2}{a} = {a}, k_{2}{a,b} = k_{2}{a,c} = k_{2}{X} = X.$ 

g- biclosed set of  $X = \{ X, \phi, \{a\}, \{c\}, \{a, c\}, \{b, c\} \}.$ 

 $(k_1,k_2)$  sg $\beta$  - closed set of X = { X,  $\phi$ , {a}, {b}, {c}, {a,b}, {a,c}, {b,c}}.

Define a closure operator  $v_1, v_2$  on Y by  $v_1\{\phi\} = \{\phi\}, v_1\{p\} = \{p\}, v_1\{q\} = \{q\}, v_1\{p,q\} = \{p,q\}, v_1\{q\} = \{p,q\}, v_1\{q\}, v_1\{q\} = \{p,q\}, v_1\{q\}, v_1$ 

 $v_1{r}=v_1{p,r}=v_1{q,r}=v_1{Y}=Y, v_2{\phi}={\phi}, v_2{p}=v_2{q}=v_2{p,q}={p,q}, v_2{r}=v_2{p,r}=v_2{q, r}=v_2{q, r}=v_2{Y}=Y$ . Biclosed set of  $Y = \{Y, \phi, \{p,q\}\}$ . Let f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  be defined by f(a) = q, f(b) = p, f(c) = r. Then f is  $(k_1, k_2) \text{ sg}\beta$  – continuous but not g-continuous. Since for the biclosed set  $\{p,q\}$  in Y, the inverse image  $f^{-1}{p,q} = \{a,b\}$  is not g-biclosed set in X.



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**Example 3.7:** (c)Let X = {a, b, c}, Y = {1, 2, 3}.Define a closure operator  $k_1$ ,  $k_2$  on X by  $k_1\{\phi\} = \{\phi\}$ ,  $k_1\{c\} = k_1\{a,c\} = \{a,c\}$ ,  $k_1\{a\} = \{a\}$ ,  $k_1\{b\} = k_1\{b,c\} = k_1\{a,b\} = k_1\{X\} = X$ ,  $k_2\{\phi\} = \{\phi\}$ ,  $k_2\{a\} = \{a\}$ ,  $k_2\{b\} = k_2\{a,b\} = \{a,b\}$ ,  $k_2\{c\} = k_2\{a,c\} = \{a,c\}$ ,  $k_2\{b,c\} = k_2\{X\} = X$ .

w-biclosed set of  $X = \{ X, \phi, \{a\}, \{a, b\}, \{a, c\} \}.$ 

 $(k_1,k_2)$  sg $\beta$  - closed set of X = { X,  $\phi$ , {a}, {b}, {c}, {a,c}, {a,b}}.

Define a closure operator  $v_1, v_2$  on Y by  $v_1\{\phi\} = \{\phi\}, v_1\{1\} = \{1\}, v_1\{2\} = v_1\{1,2\} = \{1,2\}, v_1\{3\} = v_1\{1,3\} = \{1,3\}, v_1\{1\} = \{1,3\}, v_1\{1\}, v_1\{1\} = \{1,3\}, v_1\{1\}, v_1\{1$ 

 $v_1\{2,3\}=v_1\{Y\}=Y, v_2\{\phi\}=\{\phi\}, v_2\{1\}=\{1\}, v_2\{2\}=v_2\{3\}=v_2\{2,3\}=\{2,3\},$ 

 $v_2\{1,3\} = v_2\{1,2\} = v_2\{Y\} = Y.$ 

Biclosed set of  $Y = \{ Y, \varphi, \{1\} \}$ . Let f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  be defined by f(a) = 3, f(b) = 1, f(c) = 2. Then f is  $(k_1, k_2)$  sg $\beta$  – continuous but not w-continuous. Since for the biclosed set  $\{1\}$  in Y, the inverse image  $f^{-1}\{1\} = \{b\}$  is not w-biclosed set in X.

**Example 3.8:** (d) Let  $X = \{1,2,3\}$ ,  $Y = \{a,b,c\}$ . Define a closure operator  $k_1,k_2$  on X by  $k_1\{\phi\} = \{\phi\}, k_1\{2\} = \{2\}, k_1\{3\} = k_1\{1,3\} = \{1,3\}, k_1\{1\} = k_1\{1,2\} = k_1\{2,3\} = k_1\{X\} = X, k_2\{\phi\} = \{\phi\}, k_2\{2\} = k_2\{2,3\} = \{2,3\}, k_2\{3\} = \{3\}, k_1\{1\} = k_1\{1,2\} = k_1$ 

 $k_2\{1\} = k_2\{1,3\} = \{1,3\}, \ k_2\{1,2\} = k_2\{X\} = X.$ 

BiČech J- closed set of  $X = \{ X, \phi, \{1\}, \{1,2\}, \{1,3\}, \{2,3\} \}.$ 

 $(k_1,k_2)$  sg $\beta$  - closed set of X = { X,  $\phi$ , {1}, {2}, {3}, {1,2}, {1,3}, {2,3}}.

Define a closure operator  $v_1, v_2$  on Y by  $v_1\{\phi\} = \{\phi\}, v_1\{b\} = v_1\{c\} = v_1\{b,c\} = \{b,c\},$ 

 $v_1\{a\} = \{a\}, v_1\{a,b\} = v_1\{a,c\} = v_1\{Y\} = Y, \ v_2\{\phi\} = \{\phi\}, v_2\{a\} = \{a\}, v_2\{b\} = v_2\{a,b\} = \{a,b\}, v_2\{a\} = \{a\}, v_2\{b\} = v_2\{a,b\} = \{a,b\}, v_2\{a\} = \{a\}, v_2\{b\} = v_2\{a,b\} = \{a,b\}, v_2\{a\} = \{a\}, v_2\{b\} = v_2\{a,b\} = v_2\{a,b$ 

$$v_2{c} = v_2{a,c} = {a,c}, v_2{b,c} = v_2{Y} = Y$$

Biclosed set of  $Y = \{ Y, \phi, \{a\}\}$ .Let f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  be defined by f(1) = c, f(2) = a, f(3) = b.Then f is  $(k_1, k_2)$  sg $\beta$  – continuous but not J-continuous. Since for the biclosed set  $\{a\}$  in Y, the inverse image  $f^{-1}\{a\} = \{2\}$  is not in J -biclosed set in X.

**Example 3.9:** (e) Let  $X = \{a, b, c\}$ ,  $Y = \{p,q,r\}$ . Define a closure operator  $k_1, k_2$  on X by  $k_1\{\phi\} = \{\phi\}$ ,  $k_1\{a\} = \{a\}$ ,

 $k_1\{b\} = k_1\{a,b\} = \{a,b\}, k_1\{c\} = k_1\{a,c\} = \{a,c\}, k_1\{b,c\} = k_1\{X\} = X, k_2\{\phi\} = \{\phi\},$ 

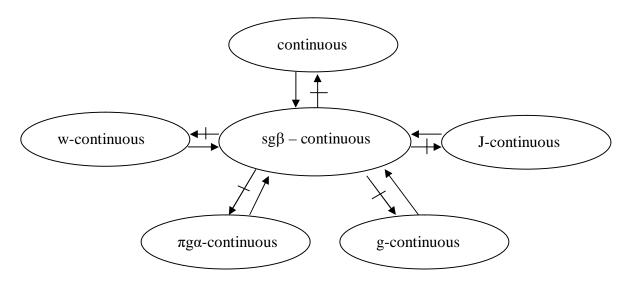
 $k_2\{b\} = k_2\{c\} = k_2\{b,c\} = \{b,c\}, k_2\{a\} = \{a\}, k_2\{a,c\} = k_2\{a,b\} = k_2\{X\} = X.$ 

BiČech  $\pi g\alpha$  – closed set of X = { X,  $\phi$ , {a}, {a, b}, {a, c}, {b, c}}.

 $(k_1,k_2)$  sg $\beta$  - closed set of X = { X,  $\phi$ , {a}, {b}, {c}, {a,c}, {b,c}, {a,b}}.

Define a closure operator  $v_1, v_2$  on Y by  $v_1\{\phi\} = \{\phi\}, v_1\{p\} = \{p\}, v_1\{q\} = v_1\{r\} = v_1\{q,r\} = \{q,r\}, v_1\{p,q\} = v_1\{q,r\} = v_1\{Y\} = Y, v_2\{\phi\} = \{\phi\}, v_2\{p\} = \{p\}, v_2\{q\} = v_2\{p,q\} = \{p,q\}, v_2\{r\} = v_2\{p,r\} = \{p,r\}, v_2\{q,r\} = v_2\{Y\} = Y.$ 

Biclosed set of  $Y = \{ Y, \phi, \{p\} \}$ .Let f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  be defined by f(a) = r, f(b) = p, f(c) = q. Then f is  $(k_1, k_2)$  sg $\beta$  – continuous but not  $\pi g\alpha$ -continuous. Since for the biclosed set  $\{p\}$  in Y, the inverse image  $f^{-1}\{p\} = \{b\}$  is not in  $\pi g\alpha$ -biclosed set in X.





**Proposition 3.10:** Let  $(X, k_1, k_2)$  and  $(Y, v_1, v_2)$  be biclosure spaces and let  $f: (X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  be a map. Then f is BiČech  $sg\beta$  – continuous if and only if the inverse image of every BiČech closed subset of  $(Y, v_1, v_2)$  is BiČech –  $sg\beta$  closed in  $(X, k_1, k_2)$ . **Proof:** Let F be BiČech closed subset in  $(Y, v_1, v_2)$ . Then Y – F is BiČech open in  $(Y, v_1, v_2)$ . Since f is BiČech  $sg\beta$  – continuous,  $f^{-1}(Y - F)$  is BiČech  $sg\beta$  – open. But  $f^{-1}(Y - F) = X - f^{-1}(F)$  thus  $f^{-1}(F)$  is BiČech  $sg\beta$  – closed in  $(X, k_1, k_2)$ . Conversely let G be an BiČech open subset in  $(Y, v_1, v_2)$ . Then Y – G is BiČech closed in  $(Y, v_1, v_2)$ . Since the inverse image of each BiČech closed subset in  $(Y, v_1, v_2)$  is BiČech  $sg\beta$  – closed in  $(X, k_1, k_2)$ . But  $f^{-1}(Y - G)$  is BiČech  $sg\beta$  – closed in  $(X, k_1, k_2)$ . But  $f^{-1}(Y - G) = X - f^{-1}(G)$ . Thus  $f^{-1}(G)$  is BiČech  $sg\beta$  – open. Therefore f is BiČech  $sg\beta$  – continuous.

**Remark 3.11:** The composition of two BiČech  $sg\beta$ - continuous need not be BiČech  $sg\beta$ - continuous.

**Definition 3.12:** A Biclosure space  $(X, k_1, k_2)$  is said to be a  $T_d$  – space if every BiČech sg $\beta$ – open set in  $(X, k_1, k_2)$  is BiČech open. **Proposition 3.13:** Let  $(X, k_1, k_2)$  and  $(Z, w_1, w_2)$  be biclosure spaces and  $(Y, v_1, v_2)$  be a  $T_d$  – space. If f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  and g:  $(Y, v_1, v_2) \rightarrow (Z, w_1, w_2)$  are BiČech sg $\beta$ – continuous, then g o f is BiČech sg $\beta$ – continuous.

**Proof:** Let H be BiČech open in (Z,  $w_1, w_2$ ). Since g is BiČech sg $\beta$ - continuous,  $g^{-1}(H)$  is BiČech sg $\beta$ - open in (Y,  $v_1, v_2$ ). But (Y,  $v_1, v_2$ ) is a  $T_d$  – space, hence  $g^{-1}(H)$  is BiČech open in (Y,  $v_1, v_2$ ). Thus  $f^{-1}(g^{-1}(H)) = (g \circ f)^{-1}(H)$  is BiČech sg $\beta$ - open in (X,  $k_1, k_2$ ). Therefore, g o f is BiČech sg $\beta$ - continuous.

**Proposition 3.14:** Let  $(X, k_1, k_2)$ ,  $(Y, v_1, v_2)$  and  $(Z, w_1, w_2)$  be biclosure spaces. If f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  is BiČech

 $sg\beta$  – continuous and g:  $(Y, v_1, v_2) \rightarrow (Z, w_1, w_2)$  is continuous then g o f is BiČech  $sg\beta$  – continuous.

**Proof:** Let H be an BiČech open subset of (Z,  $w_1, w_2$ ). Since g is continuous,  $g^{-1}(H)$  is BiČech open in (Y,  $v_1, v_2$ ). Since f is BiČech  $sg\beta$  – continuous,  $f^{-1}(g^{-1}(H))$  is BiČech  $sg\beta$  – open in (X,  $k_1, k_2$ ). But  $f^{-1}(g^{-1}(H)) = (g \circ f)^{-1}(H)$ . Therefore, g o f is BiČech  $sg\beta$  – continuous.

# IV. BIČECH sgβ – IRRESOLUTE FUNCTION

**Definition 4.1:**Let  $(X, k_1, k_2)$  and  $(Y, v_1, v_2)$  be biclosure space and a map f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  is called BiČech sg $\beta$  – irresolute, if f<sup>-1</sup>(G) is BiČech sg $\beta$  – open set (closed set) in  $(X, k_1, k_2)$  for every BiČech sg $\beta$  – open set (closed set) G in  $(Y, v_1, v_2)$ .

**Proposition 4.2:** Every BiČech  $sg\beta$  – irresolute map is BiČech  $sg\beta$  – continuous.

**Proof:** Assume that f is BiČech  $sg\beta$  – irresolute. Let V be a BiČech closed set in Y. Every BiČech closed set is BiČech  $sg\beta$  – closed. That implies V be a BiČech  $sg\beta$  – closed set in Y. Since f is BiČech  $sg\beta$  – irresolute,  $f^{-1}(V)$  is BiČech  $sg\beta$  – closed set in X. Thus  $f^{-1}(V)$  is BiČech  $sg\beta$  – closed set in X,  $\forall$  BiČech closed set V in Y. That implies f is BiČech  $sg\beta$  – continuous. **Remark 4.3:** The converse is not true as can be seen from the following example:

**Example 4.4:** Let  $X = \{a,b,c\}$  and  $Y = \{1,2,3\}$ . Define a closure operator  $k_1$ ,  $k_2$  on X by  $k_1\{\phi\} = \{\phi\}$ ,  $k_1\{a\} = k_1\{a,c\} = \{a,c\}$ ,  $k_1\{b\} = k_1\{b,c\} = \{b,c\}$ ,  $k_1\{c\} = \{c\}$ ,  $k_1\{a,b\} = k_1\{X\} = X$ ,  $k_2\{\phi\} = \{\phi\}$ ,  $k_2\{b\} = \{b\}$ ,  $k_2\{a\} = k_2\{a,b\} = \{a,b\}$ ,

 $k_2\{c\} = k_2\{b,c\} = \{b,c\}, \ k_2\{a,c\} = k_2\{X\} = X.$ 

Biclosed set of  $X = \{ X, \phi, \{b,c\} \}$ .

BiČech  $sg\beta$  – closed set of X = { X,  $\phi$ , {a}, {b}, {c}, {a, b}, {b, c}}.

 $\begin{array}{l} \text{Define a closure operator } v_1, v_2 \text{ on } Y \text{ by } v_1\{\phi\} = \{\phi\}, \ v_1\{2\} = v_1\{1,2\} = \{1,2\}, \ v_1\{3\} = v_1\{1,3\} = \{1,3\}, \ v_1\{1\} = \{1\}, \ v_1\{2,3\} = v_1\{Y\} = Y, \ v_2\{\phi\} = \{\phi\}, \ v_2\{1\} = \{1\}, \ v_2\{2\} = v_2\{3\} = v_2\{2,3\} = \{2,3\}, \end{array}$ 

 $v_2\{1,2\} = v_2\{1,3\} = v_2\{Y\} = Y.$ 

Biclosed set of  $Y = \{ Y, \phi, \{1\} \}.$ 

BiČech sg $\beta$  – closed set of Y = { Y,  $\phi$ , {1}, {2}, {3}, {1, 2}, {1,3}, {2,3}}.

Define a function f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  such that f(a) = 3, f(b) = 2, f(c) = 1. Here f is BiČech sg $\beta$  – continuous.

 $f^{-1}{1,3} = {a,c}$  is not BiČech  $sg\beta$  – closed in (X,  $k_1,k_2$ ). Therefore f is not BiČech  $sg\beta$  – irresolute.

**Proposition 4.5:** Let  $(X, k_1, k_2)$  and  $(Y, v_1, v_2)$  be biclosure spaces and f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  be a map. Then f is BiČech

 $sg\beta$  – irresolute if and only if  $f^{-1}(B)$  is BiČech  $sg\beta$  – closed in  $(X, k_1, k_2)$  whenever B is BiČech  $sg\beta$  – closed in  $(Y, v_1, v_2)$ .

**Proof:** Suppose B be a BiČech  $sg\beta$  – closed subset of  $(Y, v_1, v_2)$ . Then Y - B is BiČech  $sg\beta$  – open in  $(Y, v_1, v_2)$ .

Since f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  is BiČech sg $\beta$  – irresolute, f<sup>-1</sup>(Y – B) is BiČech sg $\beta$  – open in  $(X, k_1, k_2)$ .



But,  $f^{-1}(Y - B) = X - f^{-1}(B)$ , so that  $f^{-1}(B)$  is BiČech  $sg\beta$  – closed in (X,  $k_1, k_2$ ). Conversely, Let A be a BiČech  $sg\beta$  – open subset in (Y,  $v_1, v_2$ ). Then Y – A is BiČech  $sg\beta$  – closed in (Y,  $v_1, v_2$ ). By the assumption,  $f^{-1}(Y - A)$  is BiČech  $sg\beta$  – closed in (X,  $k_1, k_2$ ). But  $f^{-1}(Y - A) = X - f^{-1}(A)$ . Thus  $f^{-1}(A)$  is BiČech  $sg\beta$  – open in (X,  $k_1, k_2$ ). Therefore, f is BiČech  $sg\beta$  – irresolute. **Proposition 4.6:** Let (X,  $k_1, k_2$ ), (Y,  $v_1, v_2$ ) and (Z,  $w_1, w_2$ ) be biclosure spaces. If f: (X,  $k_1, k_2$ )  $\rightarrow$  (Y,  $v_1, v_2$ ) is a BiČech  $sg\beta$  – irresolute map and g: (Y,  $v_1, v_2$ )  $\rightarrow$  (Z,  $w_1, w_2$ ) is a BiČech  $sg\beta$  – continuous map, then the composition g o f: (X,  $k_1, k_2$ )  $\rightarrow$  (Z,  $w_1, w_2$ ) is BiČech  $sg\beta$  – continuous.

**Proof:** Let G be an open subset of (Z,  $w_1, w_2$ ). Then  $g^{-1}(G)$  is a BiČech sg $\beta$ -open in (Y, $v_1, v_2$ ) as g is BiČech sg $\beta$  – continuous. Hence,  $f^{-1}(g^{-1}(G))$  is BiČech sg $\beta$  – open in (X,  $k_1, k_2$ ) because f is BiČech sg $\beta$  – irresolute. Thus gof is BiČech sg $\beta$  – continuous.

**Proposition 4.7:** Let  $(X, k_1, k_2)$ ,  $(Y, v_1, v_2)$  and  $(Z, w_1, w_2)$  be biclosure spaces. If  $f: (X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  and

g:  $(Y, v_1, v_2) \rightarrow (Z, w_1, w_2)$  are BiČech sg $\beta$  – irresolute, then g o f:  $(X, k_1, k_2) \rightarrow (Z, w_1, w_2)$  is BiČech sg $\beta$  – irresolute.

**Proof:** Let F be BiČech sg $\beta$  – open set in (Z, w<sub>1</sub>,w<sub>2</sub>). As g is BiČech sg $\beta$  – irresolute,  $g^{-1}(F)$  is BiČech sg $\beta$  – open in (Y, v<sub>1</sub>,v<sub>2</sub>). Since, f is BiČech sg $\beta$  – irresolute.  $f^{-1}(g^{-1}(F))$  is BiČech sg $\beta$  – open in (X, k<sub>1</sub>,k<sub>2</sub>) implies (g o f)  $^{-1}F = (f^{-1}g^{-1}(F))$  is BiČech sg $\beta$  – open in (X, k<sub>1</sub>,k<sub>2</sub>). Hence g o f is BiČech sg $\beta$  – irresolute.

**Proposition 4.8:** Let  $(X, k_1, k_2)$  and  $(Z, w_1, w_2)$  be biclosure spaces and  $(Y, v_1, v_2)$  be a  $T_d$  – space. If f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  be a BiČech sg $\beta$  –continuous map and g:  $(Y, v_1, v_2) \rightarrow (Z, w_1, w_2)$  is a BiČech sg $\beta$  – irresolute, then the composition

g o f:  $(X, k_1, k_2) \rightarrow (Z, w_1, w_2)$  is BiČech sg $\beta$ -irresolute.

**Proof:** Let V be BiČech sg $\beta$  – open in Z. Since g is BiČech sg $\beta$  – irresolute,  $g^{-1}(V)$  is BiČech sg $\beta$  – open in Y. As Y is a  $T_d$  – space,  $g^{-1}(V)$  is BiČech open in Y. Since f is BiČech sg $\beta$ -continuous ,  $f^{-1}(g^{-1}(V))$  is BiČech sg $\beta$  – open in X. Thus (g o f)  $^{-1}(V)$  is BiČech sg $\beta$  – open in X. Hence g o f is BiČech sg $\beta$  – irresolute.

# V. TOTALLY BIČECH sg $\beta$ – CONTINUOUS FUNCTION

**Definition 5.1:** Let  $(X, k_1, k_2)$  and  $(Y, v_1, v_2)$  be a BiCech closure space. A function  $f: (X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  is called Totally BiCech continuous if the inverse image of every biopen subset of  $(Y, v_1, v_2)$  is a BiCech clopen subset in  $(X, k_1, k_2)$ .

**Definition 5.2:** Let  $(X, k_1, k_2)$  and  $(Y, v_1, v_2)$  be a BiCech closure space. A function f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  is called Totally BiCech sg $\beta$ -continuous if the inverse image of every biopen subset of  $(Y, v_1, v_2)$  is a BiCech sg $\beta$ - clopen subset in  $(X, k_1, k_2)$ .

**Theorem 5.3:** A function f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  is totally BiCech sg $\beta$ -continuous if and only if the inverse image of every biclosed subset of  $(Y, v_1, v_2)$  is a BiCech sg $\beta$ - clopen subset in  $(X, k_1, k_2)$ .

**Proof**: Assume that f is totally BiCech sg $\beta$ -continuous. Let A be any biclosed subset in Y. Then A<sup>c</sup> is a biopen subset in Y. Since f is totally BiCech sg $\beta$ -continuous. Thus f<sup>1</sup>(A<sup>c</sup>) is BiCech sg $\beta$ - clopen subset in (X, k<sub>1</sub>,k<sub>2</sub>). But f<sup>1</sup>(A<sup>c</sup>) = X - f<sup>1</sup>(A) and so f<sup>1</sup>(A) is both BiCech sg $\beta$ - closed subset and BiCech sg $\beta$ -open subset in X. Conversely, let G be a biopen subset in Y.Then G<sup>c</sup> is biclosed subset in X. By assumption f<sup>1</sup>(G<sup>c</sup>) is BiCech sg $\beta$ - clopen subset in (X, k<sub>1</sub>,k<sub>2</sub>). But f<sup>1</sup>(G<sup>c</sup>) = X - f<sup>1</sup>(G) and so f<sup>1</sup>(G) is both BiCech sg $\beta$ - clopen subset in (X, k<sub>1</sub>,k<sub>2</sub>). But f<sup>1</sup>(G<sup>c</sup>) = X - f<sup>1</sup>(G) and so f<sup>1</sup>(G) is both BiCech sg $\beta$ - clopen subset in (X, k<sub>1</sub>,k<sub>2</sub>). But f<sup>1</sup>(G<sup>c</sup>) = X - f<sup>1</sup>(G) and so f<sup>1</sup>(G) is both BiCech sg $\beta$ - clopen subset in (X, k<sub>1</sub>,k<sub>2</sub>). Therefore f is totally BiCech sg $\beta$ -continuous.

**Theorem 5.4:** Every totally BiCech sg $\beta$ -continuous f: (X,  $k_1, k_2$ )  $\rightarrow$  (Y, $v_1, v_2$ ) is BiČech sg $\beta$  – continuous function. **Proof:** Let A be any biopen subset in Y. Since f is totally BiCech sg $\beta$ -continuous. Thus f<sup>1</sup>(A) is BiCech sg $\beta$  - clopen subset in (X,  $k_1, k_2$ ).(i.e) f<sup>1</sup>(A) is both BiCech sg $\beta$  - closed subset and BiCech sg $\beta$ -open subset in X. Thus f<sup>1</sup>(A) is BiCech sg $\beta$ -open subset in (X,  $k_1, k_2$ ). Therefore f is a sg $\beta$ -continuous.

**Remark 5.5:** The converse is not true as can be seen from the following example: **Example 5.6:** Let  $X = \{a,b,c\}$ ,  $Y = \{1,2,3\}$ . Define a closure operator  $k_1,k_2$  on X by  $k_1\{\phi\} = \{\phi\}$ ,  $k_1\{a\} = k_1\{a,c\} = \{a,c\}, k_1\{b\} = k_1\{b,c\} = \{b,c\}, k_1\{c\} = \{c\}, k_1\{a,c\} = k_1\{X\} = X, k_2\{\phi\} = \{\phi\}, k_2\{b\} = \{b\}, k_2\{c\} = \{b,c\}, k_2\{a\} = k_2\{a,b\} = \{a,b\}, k_2\{a,c\} = k_2\{X\} = X.$ Biclosed set of  $X = \{X, \phi, \{b, c\}\}$ .  $(k_1,k_2) \text{ sg}\beta$  - closed set of  $X = \{X, \phi, \{a\}, \{b\}, \{c\}, \{a,b\}, \{b,c\}\}$ . Define a closure operator  $v_1,v_2$  on Y by  $v_1\{\phi\} = \{\phi\}, v_1\{1\} = \{1\}, v_1\{2\} = v_1\{1,2\} = \{1,2\}, v_1\{3\} = v_1\{1,3\} = \{1,3\}, v_1\{2,3\} = v_1\{Y\} = Y, v_2\{\phi\} = \{\phi\}, v_2\{1\} = \{1\}, v_2\{2\} = v_2\{3\} = v_2\{2,3\} = \{2,3\}, v_2\{1,3\} = v_2\{Y\} = Y.$ 



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Biclosed set of Y = {  $Y, \, \phi, \, \{1\}\}$ . Biopen set of Y = {  $Y, \, \phi, \, \{2,3\}\}.$ 

Let f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  be defined by f(a) = 2, f(b) = 1, f(c) = 3. Then f is  $(k_1, k_2) \operatorname{sg\beta}$  – continuous but not totally BiCech sg\beta-continuous. Since for the biopen set {2,3} in Y, the inverse image  $f^{-1}{2,3} = \{a,c\}$  is not totally BiCech sg\beta-clopen set in X. **Theorem 5.7:** Let f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  and g:  $(Y, v_1, v_2) \rightarrow (Z, w_1, w_2)$  be function. Then g o f:  $(X, k_1, k_2) \rightarrow (Z, w_1, w_2)$ 

(i) If f is BiCech sg $\beta$ -irresolute and g is totally BiCech sg $\beta$ -continuous then gof is totally BiCech sg $\beta$ -continuous.

(ii) If f is totally BiCech sg $\beta$ -continuous and g is BiCech continuous then gof is totally BiCech sg $\beta$ -continuous.

**Proof:** (i) Let U be a BiCech open set in Z. Since g is totally BiCech sg $\beta$ -continuous, g<sup>-1</sup>(U) is BiCech sg $\beta$ -clopen in Y. Since f is BiCech sg $\beta$ -irresolute, f<sup>1</sup>(g<sup>-1</sup>(U)) is BiCech sg $\beta$ -open and BiCech sg $\beta$ -closed in X. Since gof<sup>-1</sup>(U) = f<sup>-1</sup>(g<sup>-1</sup>(U)), gof is totally BiCech sg $\beta$ -continuous.

(ii) Let U be a BiCech open set in Z. Since g is BiCech continuous,  $g^{-1}(U)$  is BiCech open in Y. Also since f is totally BiCech sg $\beta$ -continuous,  $f^{-1}(g^{-1}(U))$  is BiCech sg $\beta$ -clopen in X. Hence gof is totally BiCech sg $\beta$ -continuous.

### VI. SLIGHTLY BIČECH sgβ – CONTINUOUS FUNCTION

**Definition 6.1:** Let  $(X, k_1, k_2)$  and  $(Y, v_1, v_2)$  be a BiCech closure space. A function  $f: (X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  is called Slightly BiCech -continuous if the inverse image of every clopen subset of  $(Y, v_1, v_2)$  is a BiCech-open subset in  $(X, k_1, k_2)$ .

**Definition 6.2:** Let  $(X, k_1, k_2)$  and  $(Y, v_1, v_2)$  be a BiCech closure space. A function  $f: (X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  is called Slightly BiCech sg $\beta$ -continuous if the inverse image of every clopen subset of  $(Y, v_1, v_2)$  is a BiCech sg $\beta$ -open subset in  $(X, k_1, k_2)$ .

**Theorem 6.3:** Every BiCech sg $\beta$ -continuous f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  is Slightly BiČech sg $\beta$ -continuous.

**Proof:** Let f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  be a BiCech sg $\beta$ -continuous function. Let U be a clopen set in Y.Then f<sup>-1</sup>(U) is BiCech sg $\beta$ -open in X and BiCech sg $\beta$ -closed in X. Hence f is Slightly BiČech sg $\beta$ - continuous.

**Theorem 6.4:** Every Slightly BiCech continuous is Slightly BiČech sgβ – continuous.

**Proof**: Let  $f: (X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  be Slightly BiCech continuous function. Let U be a clopen set in Y.Then  $f^1(U)$  BiCech open in X.Since every open set is sg $\beta$ -open,  $f^1(U)$  BiCech sg $\beta$ -open. Hence f is Slightly BiČech sg $\beta$ - continuous.

Remark 6.5: The converse is not true as can be seen from the following example:

**Example 6.6:** Let  $X = \{a,b,c\}$ ,  $Y = \{1,2,3\}$ . Define a closure operator  $k_1,k_2$  on X by  $k_1\{\phi\} = \{\phi\}$ ,

 $k_1\{a\} = k_1\{a,c\} = \{a,c\}, k_1\{b\} = k_1\{b,c\} = \{b,c\}, k_1\{c\} = \{c\}, k_1\{a,c\} = k_1\{X\} = X, k_2\{\phi\} = \{\phi\},$ 

 $k_2\{\phi\} = \{\phi\}, k_2\{b\} = \{b\}, k_2\{c\} = k_2\{b,c\} = \{b,c\}, k_2\{a\} = k_2\{a,b\} = \{a,b\}, k_2\{a,c\} = k_2\{X\} = X.$ 

Biclosed set of X={X,  $\phi$ , {b,c}}. Biopen set of X={X,  $\phi$ , {a}}.

 $(k_1,k_2)$  sg $\beta$  - closed set of X = { X,  $\phi$ , {a}, {b}, {c}, {a,b}, {b,c} }.

Define a closure operator  $v_1, v_2$  on Y by  $v_1\{\phi\} = \{\phi\}, v_1\{1\} = v_1\{1,3\} = \{1,3\}, v_1\{2\} = \{2\},$ 

 $v_1{3} = v_1{2,3} = v_1{1,2} = v_1{Y} = Y, v_2{\phi} = {\phi}, v_2{2} = {2}, v_2{3} = {3}, v_2{1} = v_2{1,3} = {1,3},$ 

 $v_2{2,3} = {2,3}, v_2{1,2} = v_2{Y} = Y.$ 

Biclopen set of  $Y = \{ Y, \phi, \{2\}, \{1,3\} \}.$ 

Let f:  $(X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  be defined by f(a) = 3, f(b) = 1, f(c) = 2. Then f is slightly BiCech sg $\beta$  – continuous but not slightly BiCech continuous. Since for the clopen set {1,3} in Y, the inverse image  $f^{-1}{1,3} = \{a,b\}$  is not slightly BiCech open set in X.

**Theorem 6.7:** Let  $f: (X, k_1, k_2) \rightarrow (Y, v_1, v_2)$  and  $g: (Y, v_1, v_2) \rightarrow (Z, w_1, w_2)$  be function.

(i) If f is BiCech sg $\beta$ -irresolute and g is slightly BiCech sg $\beta$ -continuous then gof is slightly BiCech sg $\beta$ -continuous.

(ii) If f is BiCech sg $\beta$ -irresolute and g is BiCech sg $\beta$ -continuous then gof is slightly BiCech sg $\beta$ -continuous.

(iii) If f is BiCech sg $\beta$ -continuous and g is slightly BiCech continuous then gof is slightly BiCech sg $\beta$ -continuous.

**Proof:** (i) Let U be a BiCech clopen set in Z. Since g is slightly BiCech sg $\beta$  -continuous,  $g^{-1}(U)$  is BiCech sg $\beta$  -open in Y. Since f is BiCech sg $\beta$  -irresolute,  $f^{-1}(g^{-1}(U))$  is BiCech sg $\beta$  -open in X. Since  $gof^{-1}(U) = f^{-1}(g^{-1}(U))$ , gof is slightly BiCech sg $\beta$  -continuous.

(ii) Let U be a BiCech clopen set in Z. Since g is BiCech sg $\beta$  - continuous, g<sup>-1</sup>(U) is BiCech sg $\beta$ -open in Y. Also since f is BiCech sg $\beta$ -irresolute, f<sup>-1</sup>(g<sup>-1</sup>(U)) is BiCech sg $\beta$ -open in X. Hence gof is slightly BiCech sg $\beta$ -continuous.

(iii) Let U be a BiCech clopen set in Z. Since g is BiCech continuous,  $g^{-1}(U)$  is BiCech open in Y. Also since f is BiCech sg $\beta$ -continuous,  $f^{-1}(g^{-1}(U))$  is BiCech sg $\beta$ -copen in X. Hence gof is slightly BiCech sg $\beta$ -continuous.

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