



iJRASET

International Journal For Research in
Applied Science and Engineering Technology



INTERNATIONAL JOURNAL FOR RESEARCH

IN APPLIED SCIENCE & ENGINEERING TECHNOLOGY

Volume: 5 Issue: VIII Month of publication: August 2017

DOI: <http://doi.org/10.22214/ijraset.2017.8334>

www.ijraset.com

Call:  08813907089

E-mail ID: ijraset@gmail.com

Analysis of Stress and Strain with Variation in Elastic Properties in Symmetric Laminated Composite Rectangular Plate

Yogesh Pratap Singh¹, Tikam Prasad², Mukesh kumar³, Atul tiwari⁴, Aviral Sharma⁵

Department of Mechanical Engineering, National Institute of Technology, Raipur

Abstract: Composite materials play a key role in aerospace and many other fields. Normally we desire a very high strength to weight ratio, so it becomes vital to study composite properties with different elastic parameters along with different fiber direction & stacking arrangements. This paper contains all possible variations of stress and strain of different laminas of a laminated angle ply composite plate with elastic properties. The study of these variations can be used to optimize material properties of composites as per given application.

Keywords: Laminate, Lamina, CLPT, Cross Ply lamination, Angle ply lamination.

I. INTRODUCTION

Composite materials are materials constituted for two or more components, which remain independent at the macroscopic level when they become part of a structure. The main advantages for the use composite materials are high strength and high stiffness to weight ratio. These reasons put composites in service like Aerospace structures, Automobiles, Boats, Pipe lines, Buildings, Bridges etc.

A laminate is constructed by stacking a number of laminas in the thickness (z) direction. Each layer is thin and may have different fiber orientation. The fiber orientation, stacking arrangements and material properties influence the response from the laminate. For Cross Ply lamination consecutive fibers are in perpendicular directions while in Angle ply consecutive fibers are at some angle.

II. THEORY OF LAMINATED PLATES

The classical laminate plate theory (CLPT) is used to analyze the mechanical behavior of the composite laminated plates. We assume that plane stress condition is valid for each ply.

This theory is the extension of the classical plate theory. The plate response is influenced by the fiber direction, stacking arrangements, material properties. In this theory, for plate analysis the Kirchhoff's plate theory is assumed and contains the assumptions as follows. This theory deals the mechanics of composite laminated plates using stress strain relations.

A. Assumptions

Straight lines perpendicular to the mid surface before deformation is straight after deformation.

The transverse normals do not experience elongation.

Transverse normal's rotate such that they remain perpendicular to the mid surface after deformation.

B. Assumptions

The layers are perfectly bonded together.

The material of each layer is linearly elastic and has three planes of material symmetry.

Each layer is of uniform thickness.

The strains and displacements are small.

The transverse shear stresses on the top and bottom of surfaces of the laminate are zero.

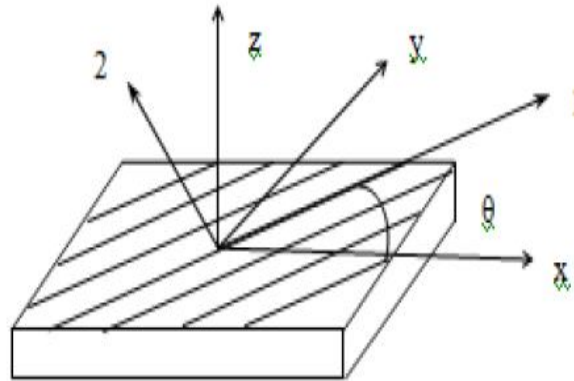


Figure 1: composite lamina

The above figure shows a composite lamina. The direction along the fiber axis is referred 1. The direction transverse to the fiber axis but in the plane of the lamina is referred 2. The direction transverse to both the fiber axis and the plane of the lamina (out of page) is referred 3.

The 1-2 co-ordinate system can be considered to be local co-ordinates based on the fiber direction. However this system is inadequate as fibers can be placed at various angles with respect to each other and the structure. Therefore a new co-ordinate system needs to be defined that takes into account the angle the fiber makes with its surroundings. This new system is referred to as global co-ordinates (x-y system) and is related to the local coordinates (1-2 system) by the angle θ . A composite material is not isotropic and therefore its stresses and strains cannot be related by the simple Hooke's Law. This law has to be extended to two-dimensions and redefined for the local and global co-ordinate systems. The result is Equations (1) and (2).

$$\begin{bmatrix} \sigma_1 \\ \sigma_2 \\ \tau_{12} \end{bmatrix} = \begin{bmatrix} Q_{11} & Q_{12} & 0 \\ Q_{21} & Q_{22} & 0 \\ 0 & 0 & Q_{66} \end{bmatrix} \begin{bmatrix} \epsilon_1 \\ \epsilon_2 \\ \gamma_{12} \end{bmatrix} \quad (1)$$

$$\begin{bmatrix} \sigma_x \\ \sigma_y \\ \tau_{xy} \end{bmatrix} = \begin{bmatrix} \overline{Q}_{11} & \overline{Q}_{12} & \overline{Q}_{16} \\ \overline{Q}_{21} & \overline{Q}_{22} & \overline{Q}_{26} \\ \overline{Q}_{16} & \overline{Q}_{26} & \overline{Q}_{66} \end{bmatrix} \begin{bmatrix} \epsilon_x \\ \epsilon_y \\ \gamma_{xy} \end{bmatrix} \quad (2)$$

Where $\sigma_{1,2}$ are the normal stresses in directions 1 and 2; τ_{12} is the shear stress in the 1-2 plane; $\epsilon_{1,2}$ are the normal strains in directions 1 and 2; γ_{12} is the shear strain in the 1-2 plane. $[Q]$ is the reduced stiffness matrix; $\sigma_{x,y}$ are the normal stresses in directions x and y; τ_{xy} is the shear stress in the x-y plane; $\epsilon_{x,y}$ are the normal strains in directions x and y; γ_{xy} is the shear strain in the x-y plane; $[\overline{Q}]$ is the transformed reduced stiffness matrix. The elements of the $[Q]$ matrix in Equation (1) are dependent on the material constants and may be calculated using Equations (3).

$$\begin{aligned} Q_{11} &= \frac{E_1}{1-\nu_{12}\nu_{21}} & Q_{22} &= \frac{E_2}{1-\nu_{12}\nu_{21}} \\ Q_{12} &= \frac{\nu_{21}E_1}{1-\nu_{12}\nu_{21}} & Q_{66} &= G_{12} \end{aligned} \quad (3)$$

Where $E_{1,2}$ are Young's modulus in directions 1 and 2; G_{12} is the shear modulus in the 1-2 plane; $\nu_{12,21}$ are Poisson's ratios in the 1-2 and 2-1 planes The matrix in Equation (2) may be determined by Equation (4).

$$[\overline{Q}] = [T]^{-1}[Q][R][T][R]^{-1} \quad (4)$$

Where $[T]$ is the transformation matrix; $[R]$ is the Reuter matrix. These matrices are given by:

$$[T] = \begin{bmatrix} m^2 & n^2 & 2mn \\ n^2 & m^2 & 2mn \\ -mn & mn & m^2 - n^2 \end{bmatrix} \quad [R] = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 2 \end{bmatrix} \quad (5)$$

A, B and D matrices are known as extensional, coupling and bending laminate stiffness

$$\begin{aligned} A_{ij} &= \sum_{k=1}^N (\overline{Q}_{ij})_k (z_k - z_{k-1}) \\ B_{ij} &= \frac{1}{2} \sum_{k=1}^N (\overline{Q}_{ij})_k (z_k^2 - z_{k-1}^2) \\ D_{ij} &= \frac{1}{3} \sum_{k=1}^N (\overline{Q}_{ij})_k (z_k^3 - z_{k-1}^3) \end{aligned} \quad (6)$$

Here k is no of layer and Z_k terms are through thicknesses. The orthotropic layers are oriented such that the complete laminate is symmetric across the middle surface. Due to this symmetry, the [B] matrix that relates the bending-extension coupling is effectively zero, $[B]_{ij}=0$. The Z_k terms are defined from the middle surface of the laminate as shown in Figure 2

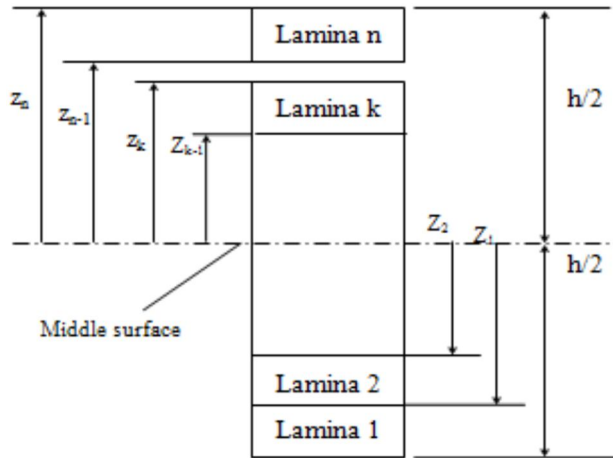


Figure 2

C. Effective Elastic properties of laminates

It is important to calculate the Effective elastic properties of a Laminate, those are the effective extensional modulus in the x direction, the effective extensional modulus in the y direction, the effective Poisson’s ratios and the effective shear modulus in the x-y plane . These constants allow us to do classical mechanics of laminates like stress analysis and buckling analysis.

$$\begin{aligned} \overline{E}_x &= \frac{1}{a_{11}h} & \overline{E}_y &= \frac{1}{a_{22}h} & \overline{G}_{xy} &= \frac{1}{a_{66}h} \\ \overline{\nu}_{xy} &= \frac{a_{12}}{a_{11}} & \overline{\nu}_{yx} &= \frac{a_{21}}{a_{22}} \end{aligned} \quad (7)$$

Here a_{ij} is elements of compliance matrix, h are the laminate thickness. In order to calculate the engineering properties of a symmetric laminate using above equations one needs to calculate the extensional stiffness matrix [A] and then invert it to obtain the compliance matrix [a]

$$[a] = [A^{-1}] \quad (8)$$

III. PROBLEM STATEMENT

Our aim is to study variation of stress-strain with Elastic properties induced at various laminas of a Symmetrical Angle ply Rectangular Composite laminate in ANSYS.

IV. ANALYSIS CONDITIONS

We have used ACP MODULE in ANSYS 18 for our analysis. Followings are the details of Analysis conditions:

- A. Plate of Dimension 150 × 80 mm, fixed at 80mm end.
- B. (45°, -45°, -0°, -45°, 45°) symmetrical layup for the plate each being 0.3 mm thick as shown in figure 3(a-e)

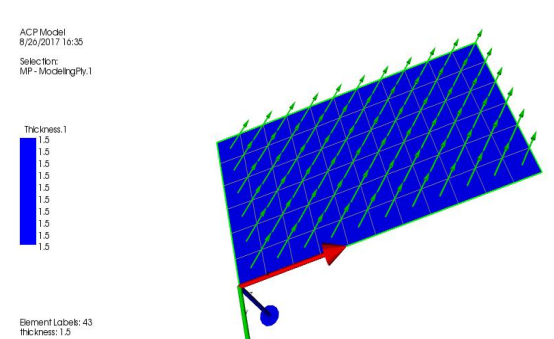


Figure 3 (a): 45°

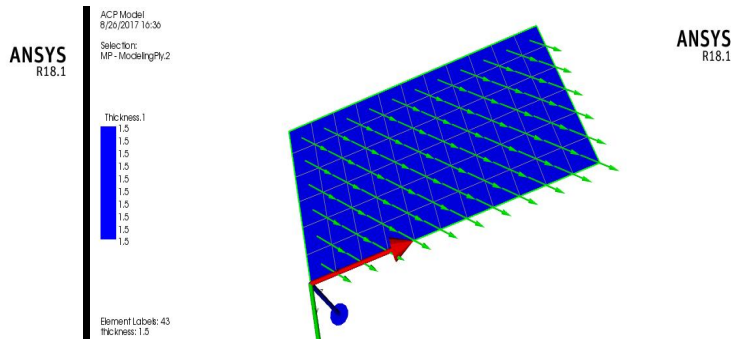


Figure 3 (b): - 45°

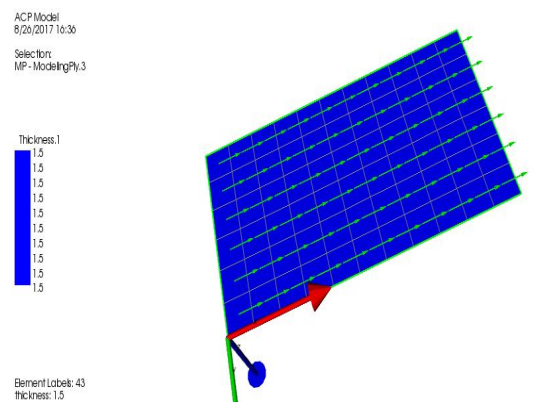


Figure 3 (c): 0°

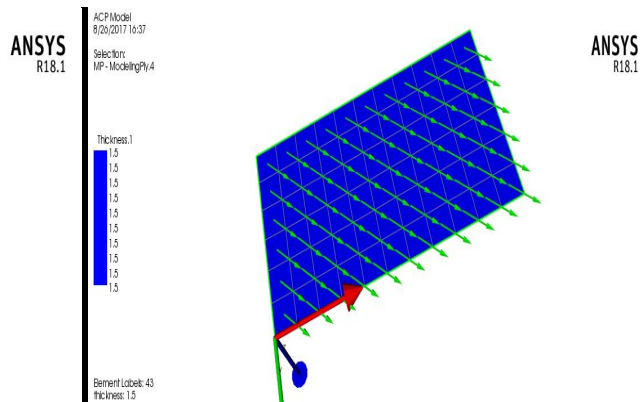


Figure 3 (d): -45°

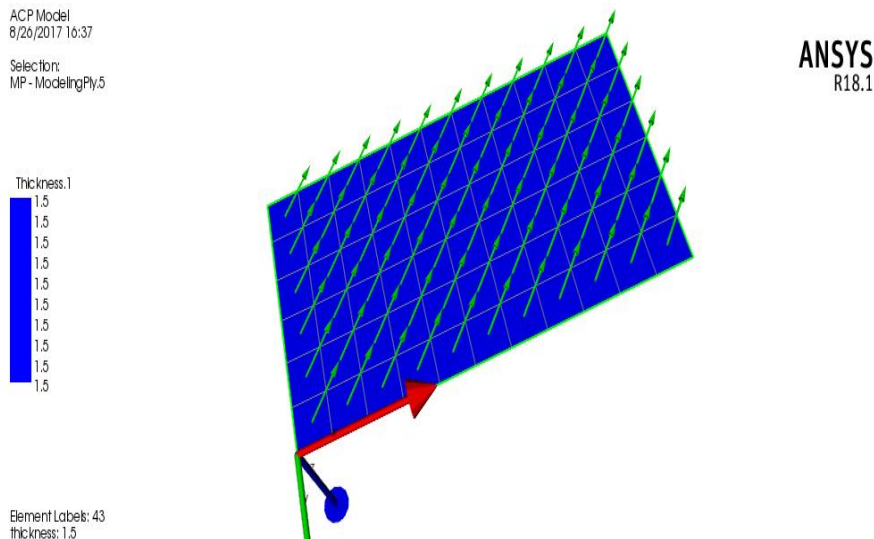


Figure 3 (e): 45°

C. Material applied is Epoxy Carbon UD with properties shown in figure 4

| Properties of Outline Row 3: Epoxy Carbon UD (230 GPa) Prepreg | | | | |
|--|---|----------|--------------------|-----|
| | A | B | C | D E |
| 1 | Property | Value | Unit | |
| 2 | Density | 1.49E-09 | mm ⁻³ t | |
| 3 | Orthotropic Secant Coefficient of Thermal Expansion | | | |
| 4 | Coefficient of Thermal Expansion | | | |
| 5 | Coefficient of Thermal Expansion X direction | -4.7E-07 | C ⁻¹ | |
| 6 | Coefficient of Thermal Expansion Y direction | 3E-05 | C ⁻¹ | |
| 7 | Coefficient of Thermal Expansion Z direction | 3E-05 | C ⁻¹ | |
| 8 | Orthotropic Elasticity | | | |
| 9 | Young's Modulus X direction | 1.21E+05 | MPa | |
| 10 | Young's Modulus Y direction | 8600 | MPa | |
| 11 | Young's Modulus Z direction | 8600 | MPa | |
| 12 | Poisson's Ratio XY | 0.27 | | |
| 13 | Poisson's Ratio YZ | 0.4 | | |
| 14 | Poisson's Ratio XZ | 0.27 | | |

Figure 4: Epoxy Carbon UD

D. Small transverse load of 100 N is applied over top of the plate.

V. RESULTS & CONCLUSIONS

A. Stress

- 1) Variation of stress with variation in Poisson's ratio is shown in figure 5(a-c)
- 2) With increase in value of Poisson's ratio in xy (plane of fibers), stress decreases and stress is symmetrically distributed across the middle lamina.(e.g. stress value for lamina 1& 5 and 2 & 4 are same due to symmetry)
- 3) With change in value of Poisson's ratio in yz or zx plane, stress remains same for a particular lamina and stress is symmetrically distributed across the middle lamina.(e.g. stress value for lamina 1& 5 and 2 & 4 are same due to symmetry).
- 4) Stress is least for middle lamina and maximum for outer laminas.

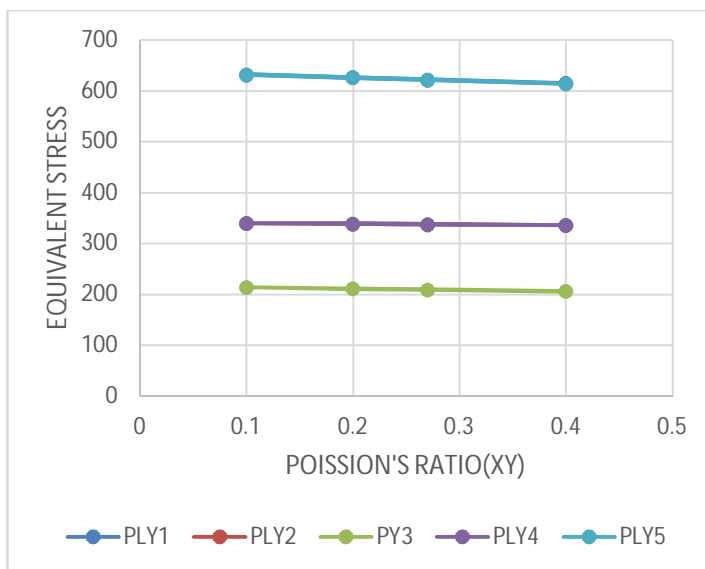


Figure 5(a)

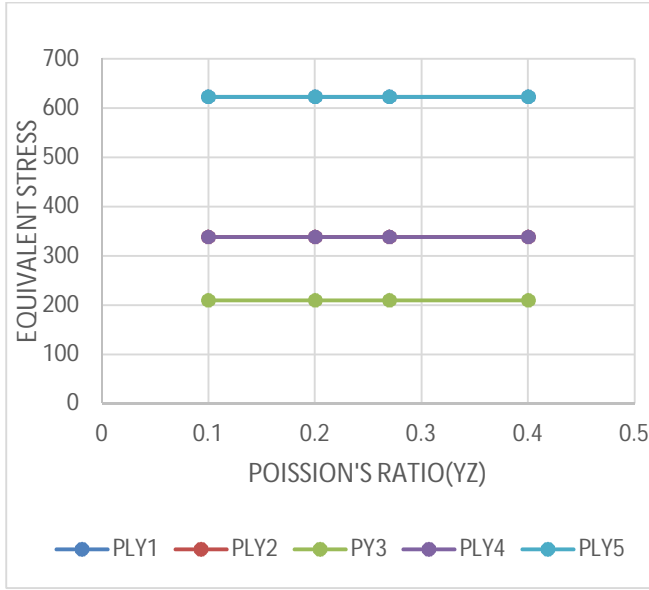


Figure 5(b)

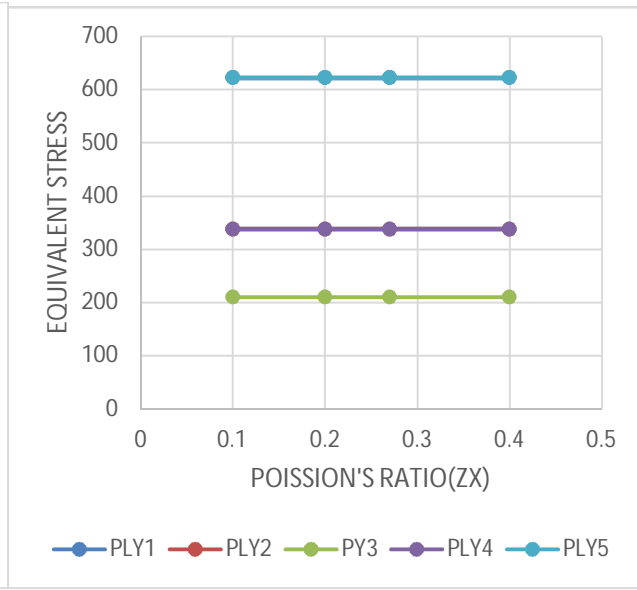


Figure 5(c)

5) Variation of stress with variation in Young's Modulus is shown in figure 6(a-c)

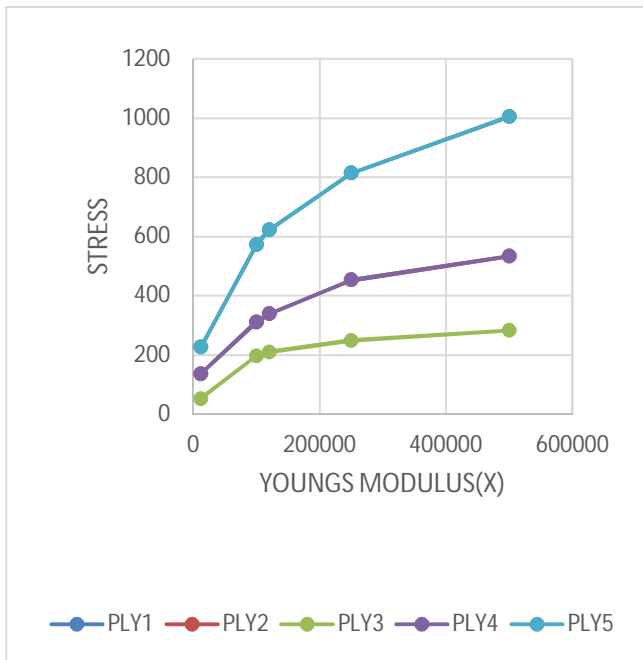


Figure 6(a)

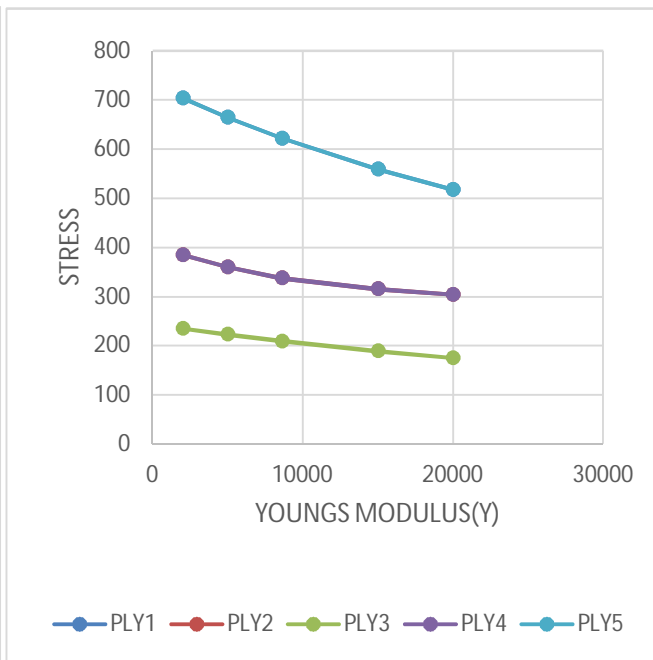


Figure 6(b)

- a) With increase in value of Young's Modulus in y direction, stress decreases and stress is symmetrically distributed across the middle lamina.(e.g. stress value for lamina 1& 5 and 2 & 4 are same due to symmetry)
- b) With increase in value of Young's Modulus in x direction, stress increases and stress is symmetrically distributed across the middle lamina.(e.g. stress value for lamina 1& 5 and 2 & 4 are same due to symmetry)
- c) With change in value of Young's Modulus in z direction, stress remains same for particular lamina and stress is symmetrically distributed across the middle lamina (e.g. stress value for lamina 1& 5 and 2 & 4 are same due to symmetry).
- d) Stress is least for middle lamina and maximum for outer laminas.

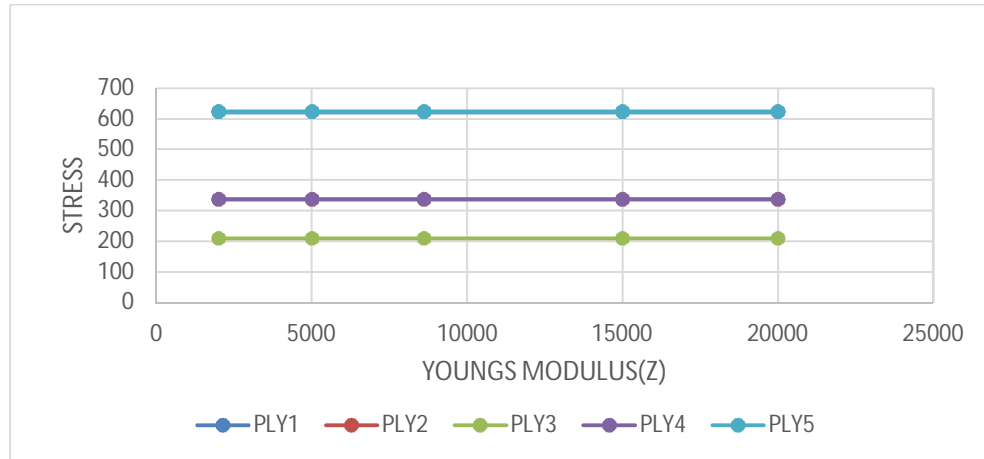


Figure 6(c)

6) Variation of stress with variation in Density is shown in figure 7

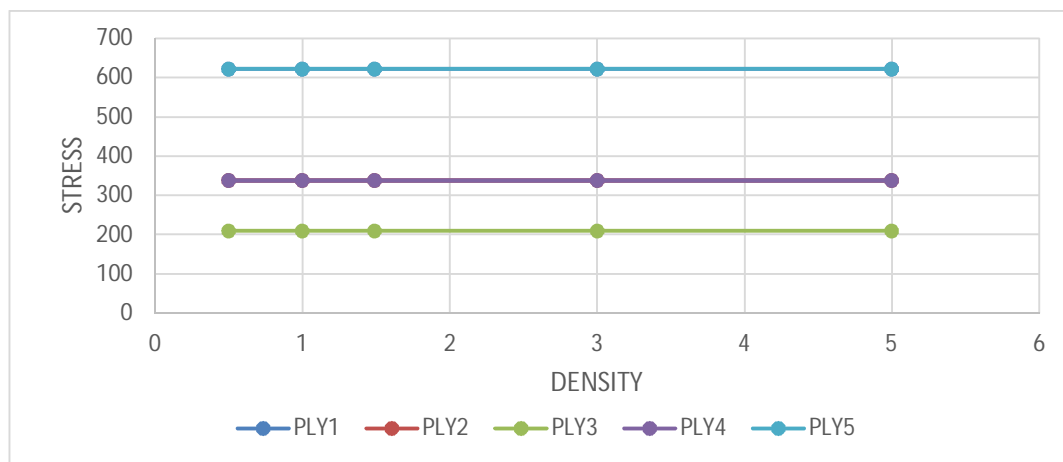


Figure 7

- 7) With change in value of Density of Material, stress remains same for particular lamina and stress is symmetrically distributed across the middle lamina (e.g. stress value for lamina 1 & 5 and 2 & 4 are same due to symmetry).
- 8) Stress is least for middle lamina and maximum for outer laminas.

Figure 8(a-c) shows stress Analysis in ANSYS for Poisson's Ratio=0.4

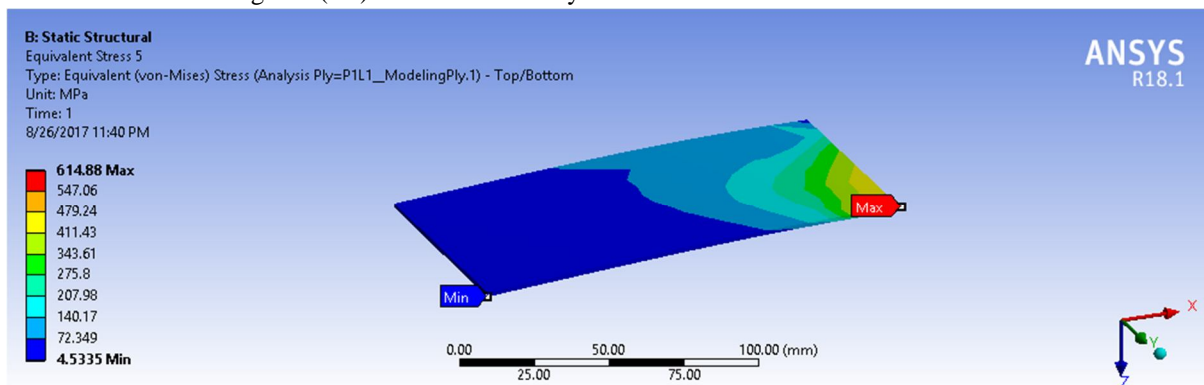


Figure 8(a): stress for lamina 1 & 5

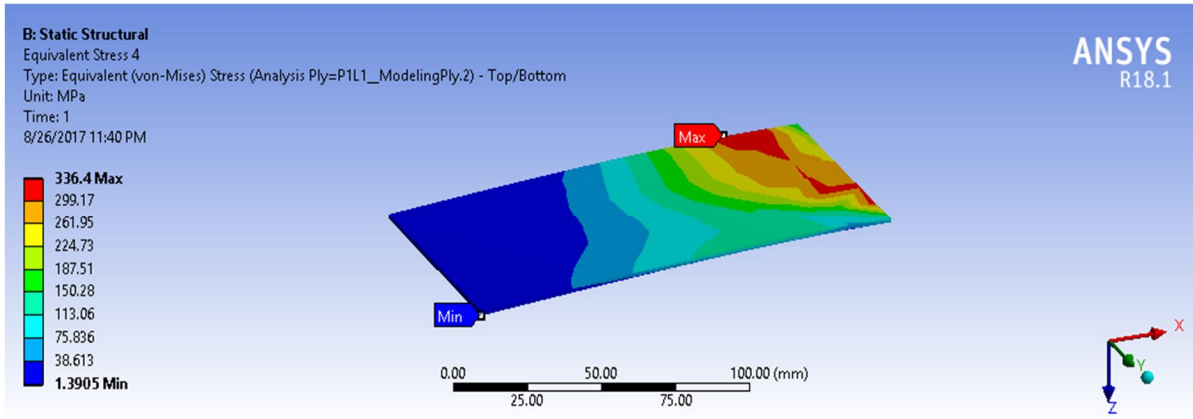


Figure 8(b): stress for lamina 2 & 4

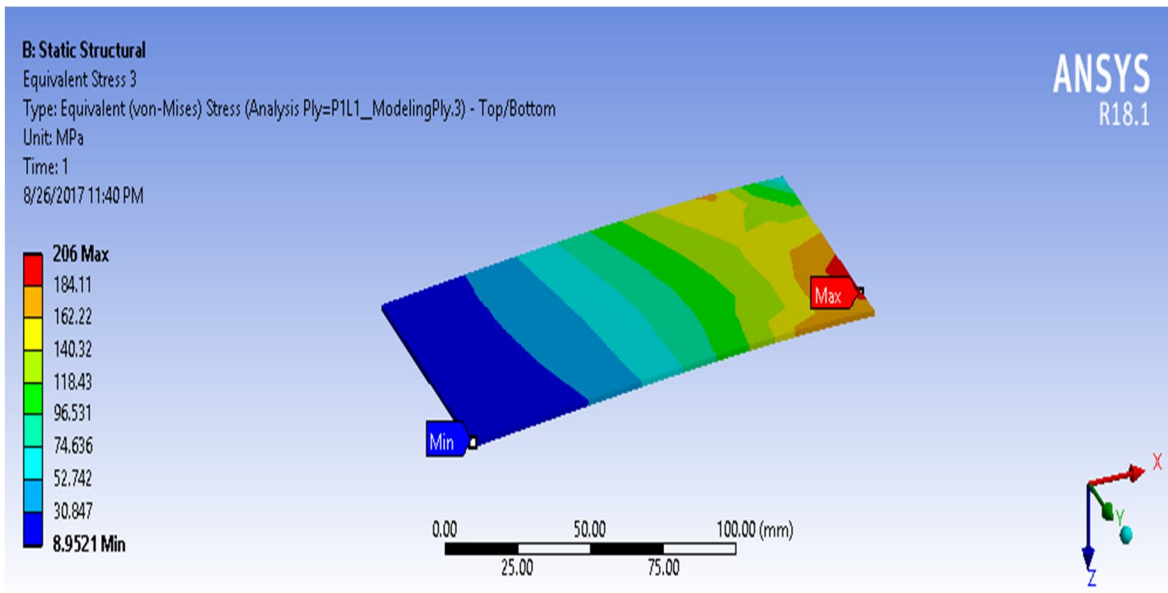


Figure 8(c): stress for lamina 3(middle)

B. STRAIN :

1) Variation of strains with variation in Poisson's ratio is shown in figure 9(a-c)

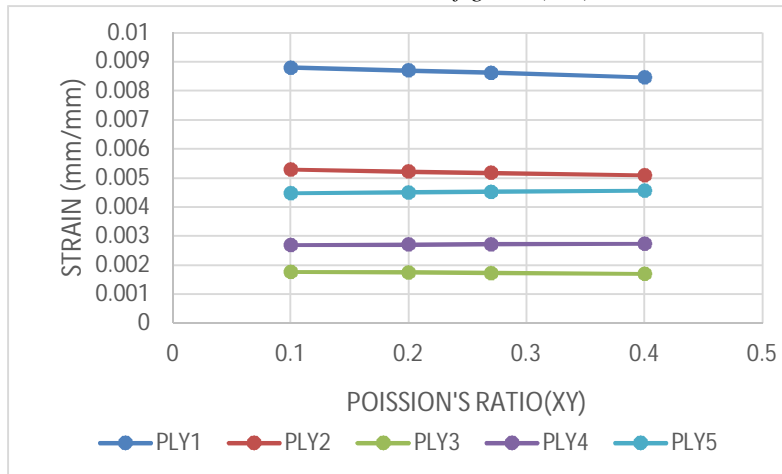


Figure 9(a)

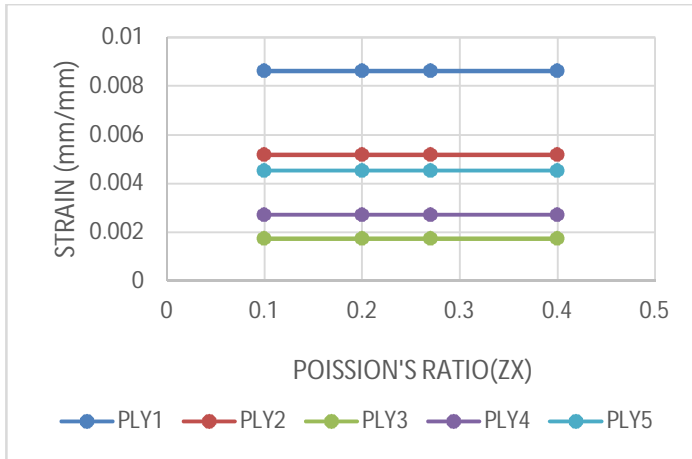


Figure 9(b)

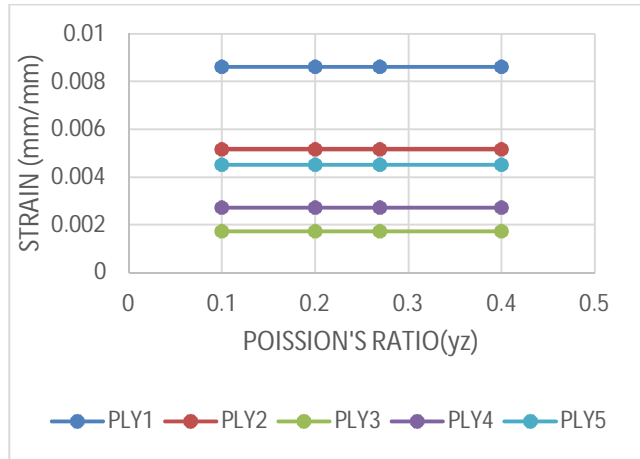


Figure 9(c)

- 2) Variation of strain with variation in Poisson's ratio is shown in figure 9(a-c)
- With increase in value of Poisson's ratio in xy (plane of fibers), strain decreases for lamina 1, 2& 3, and increases for lamina 4 and 5 since 1&2 and 4&5 are in opposite side of middle lamina.
 - With change in value of Poisson's ratio in yz or zx plane, strain remains same for a particular lamina.
 - Strain is least for middle lamina and maximum for first lamina.

- 3) Variation of strains with variation in Young's modulus is shown in figure 10(a-c)

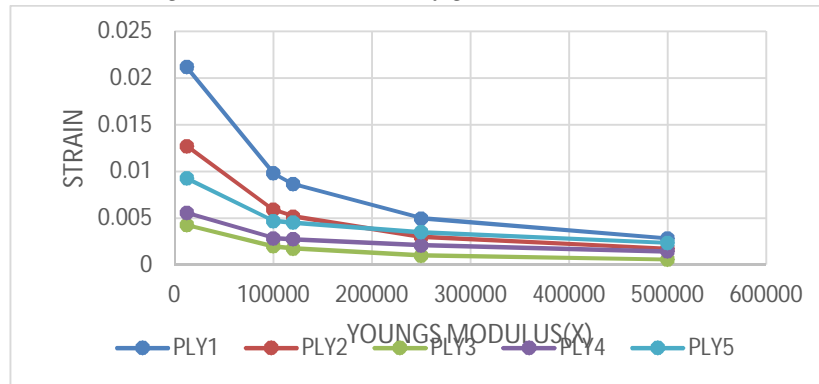


Figure 10(a)

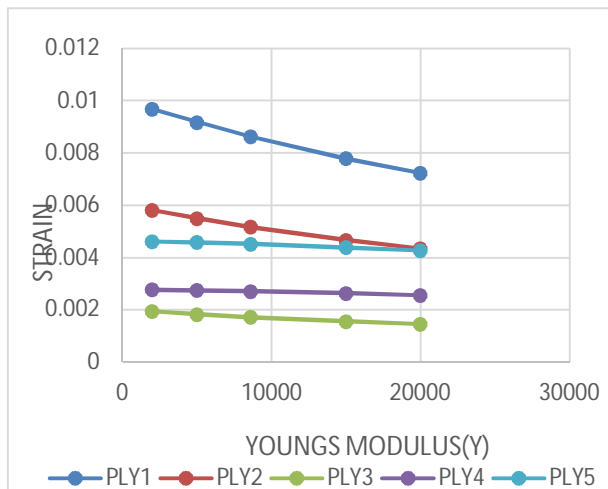


Figure 10(b)

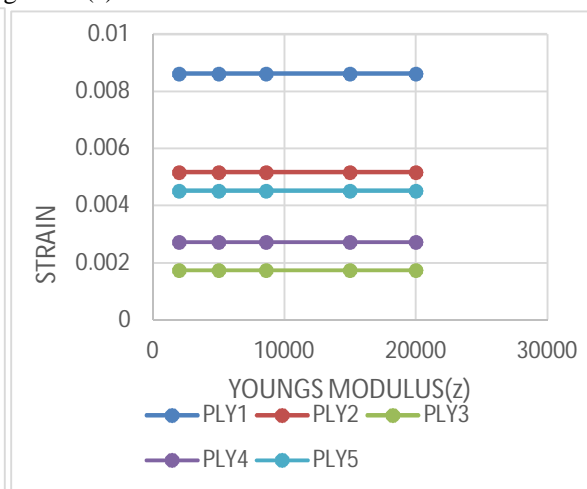


Figure 10(c)

- a) With increase in value of Young's Modulus in y and x direction, strain decreases.
 - b) With change in value of Young's Modulus in z direction, strain remains same for particular lamina.
 - c) Strain is least for middle lamina and maximum for first lamina.
- 4) Variation of strains with variation in Density is shown in figure 11
- a) With change in value of Density of Material, strain remains same for particular lamina.
 - b) Strain is least for middle lamina and maximum for first lamina.

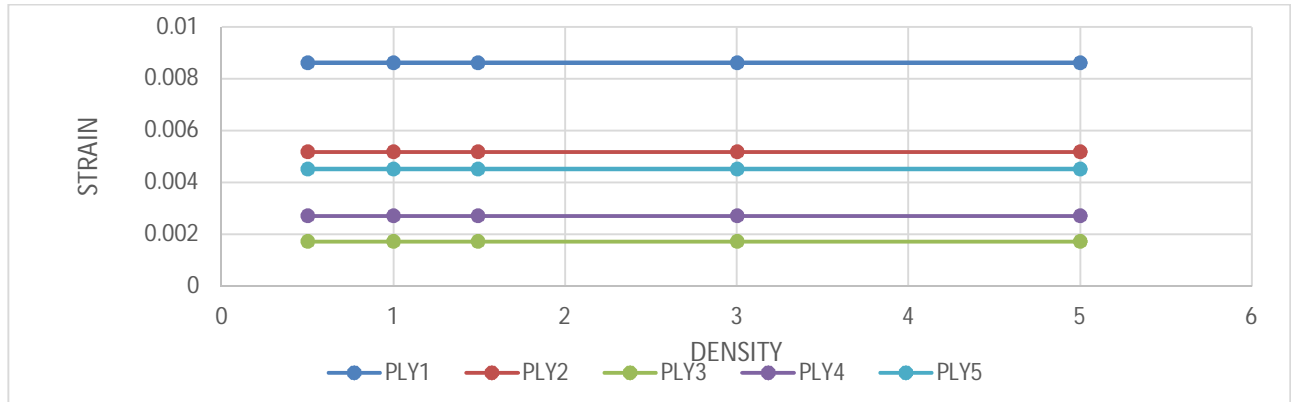


Figure 11

Figure 12(a-e) shows strain Analysis in ANSYS for Poisson's Ratio=0.4

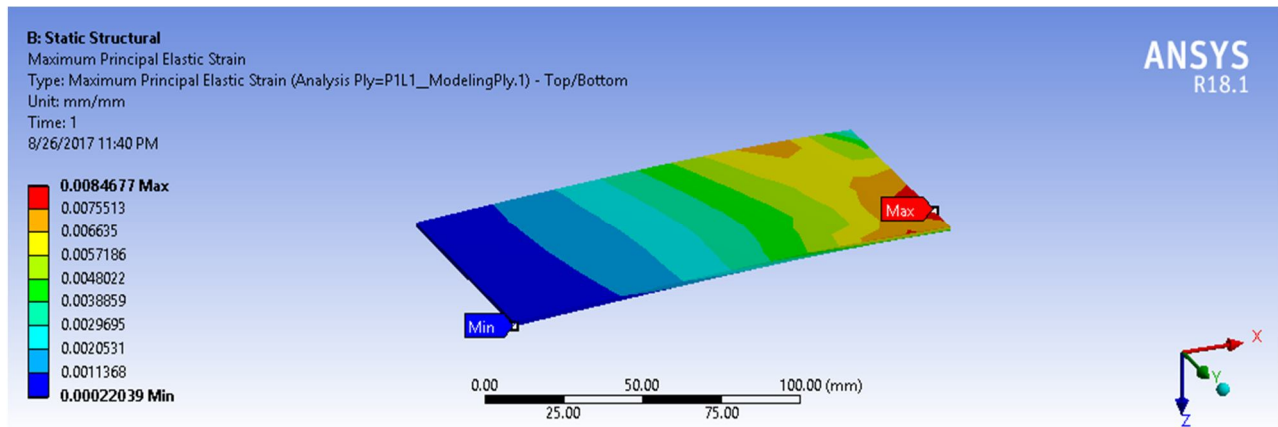


Figure 12(a): strain for lamina 1

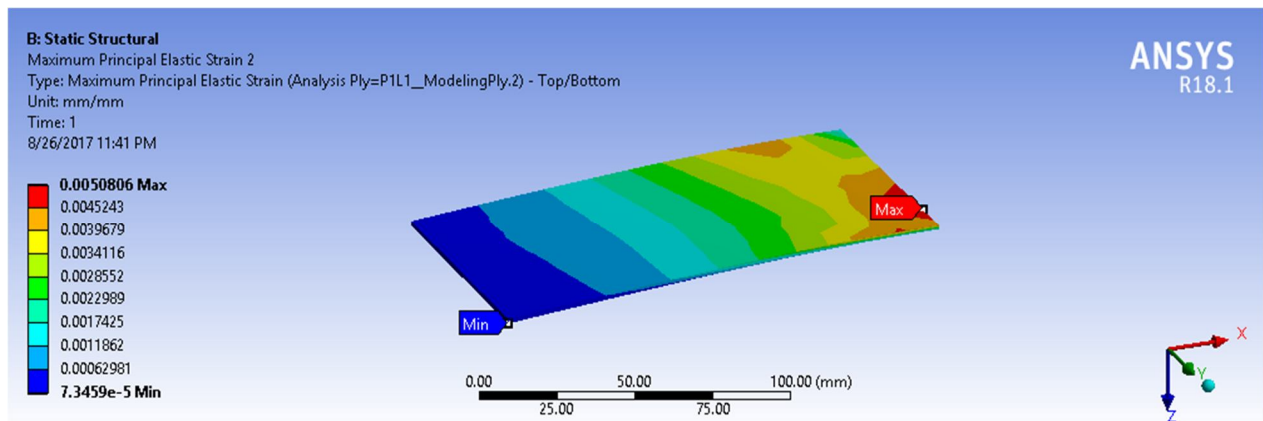


Figure 12(b): strain for lamina 2

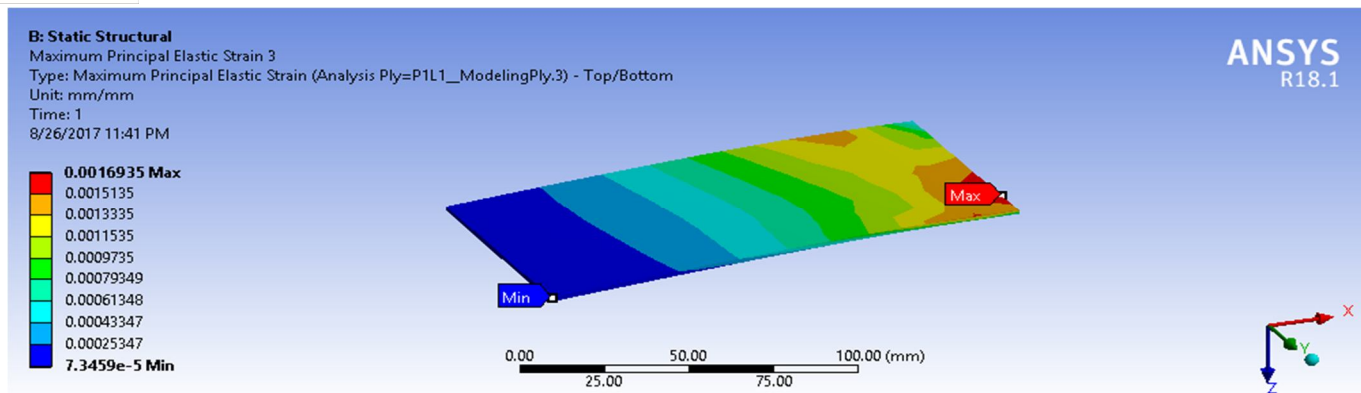


Figure 12(c): strain for lamina 3

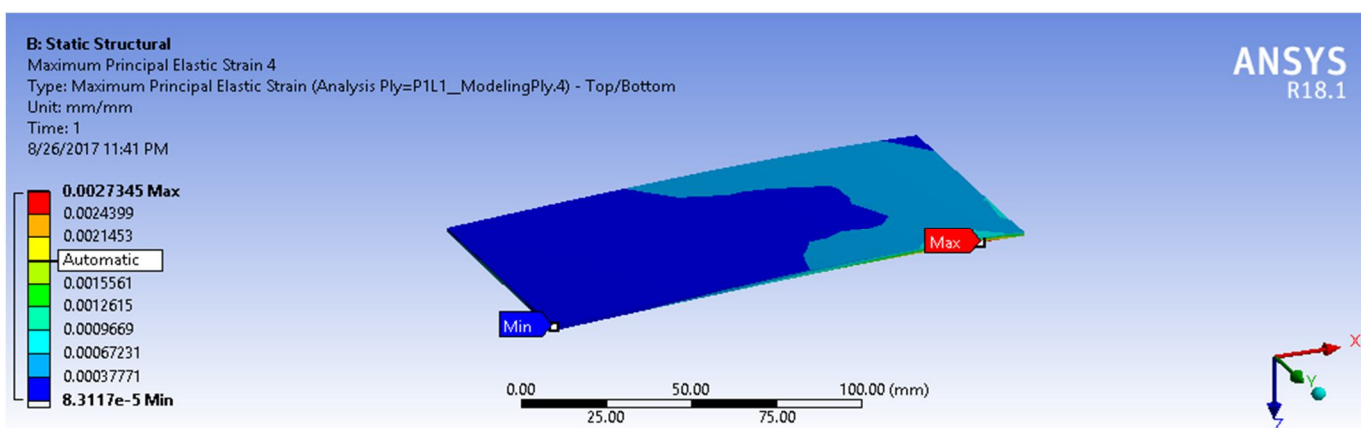


Figure 12(d): strain for lamina 4

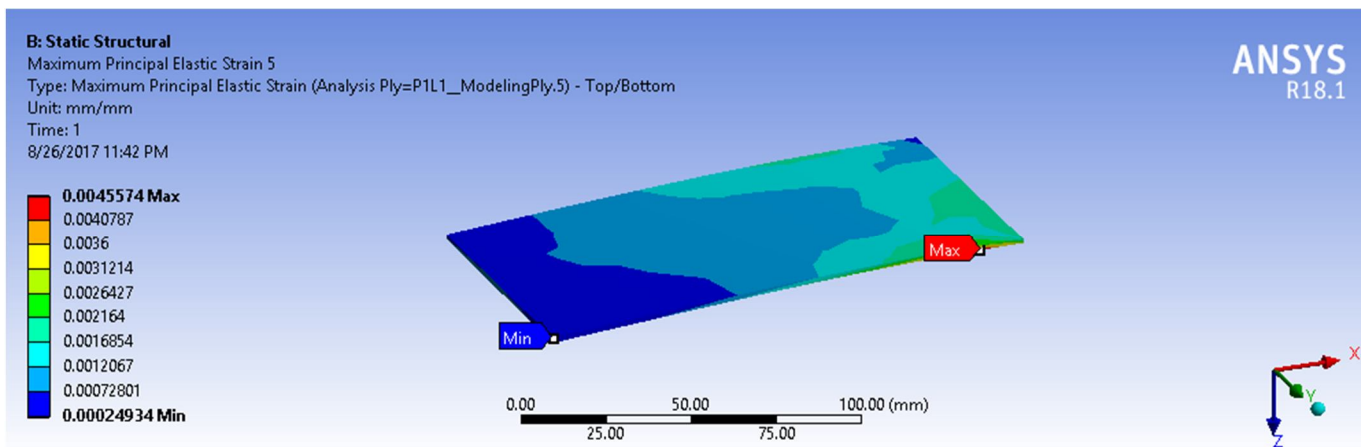


Figure 12(e): strain for lamina 5

VI. FURTHER WORKS THAT CAN BE DONE

Other than what analysis we have done, we can also work on following:

- A. Variation of stress and strains in different lamina with changing thermal Conditions.
- B. Variation of stress and strains in different lamina with change in orientation and stacking of laminas.



REFERENCES

- [1] JN Reddy “Mechanics of Laminated Composite Plates and Shells”
- [2] The basic mechanics of of composite materials are from “Mechanics of Composite materials by Robert M.Jones”
- [3] Engineering mechanics of composite materials by Isaac M.Daniel Ori ishai
- [4] K. Pradeep Chand, K. Chaitanya, “Study the Effects of Free Vibration and Effective Elastic Properties with Variation of Layer Orientation of Symmetric Laminate Plates”, ijsr ,Volume 5 Issue 5, May 2016, Paper ID: NOV163792
- [5] Tariq Salem Alshahbouni, “Stress Analysis of Laminated Composite Beam by Using MATLAB Software”, ijsr, Volume 6 Issue 7, July 2017, Paper ID: ART20174775.



10.22214/IJRASET



45.98



IMPACT FACTOR:
7.129



IMPACT FACTOR:
7.429



INTERNATIONAL JOURNAL FOR RESEARCH

IN APPLIED SCIENCE & ENGINEERING TECHNOLOGY

Call : 08813907089  (24*7 Support on Whatsapp)